

# Island wakes

Madeira Archipelago case study

<http://wakes.uma.pt>

# Outline

- Introduction
- Remote Sensing data
- Barotropic (2D) numerical study
- Baroclinic (3D) numerical study
- New hypothesis
- Future work

# People

Euclides Luis, CEMAT - IST

Dmitri Boutov, IO - FCUL

Alain Chelius, UBordeaux I

Aires dos Santos, MARETEC - IST

Juha Videman, CEMAT - IST

Pablo Sangrà, ULPGC

Rui Caldeira, CIIMAR - UP / CCM



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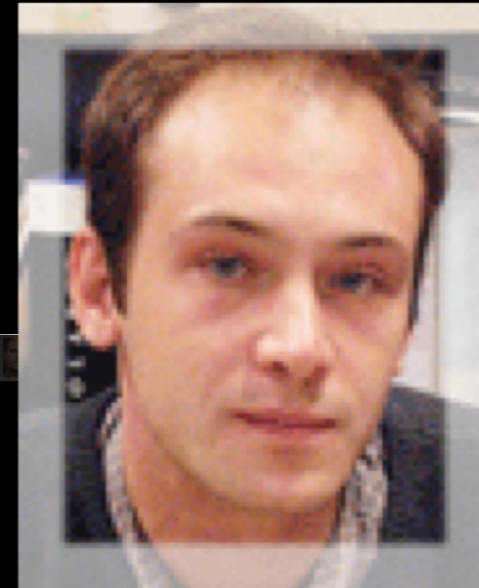
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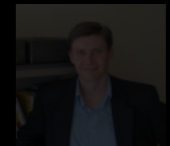
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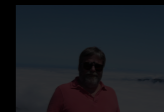
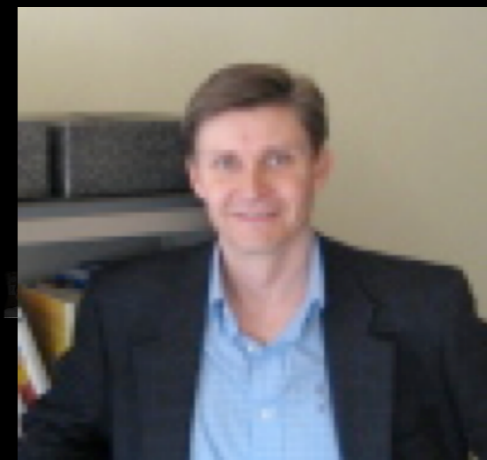
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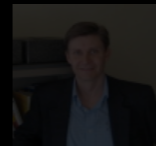
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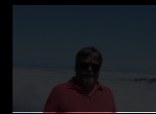
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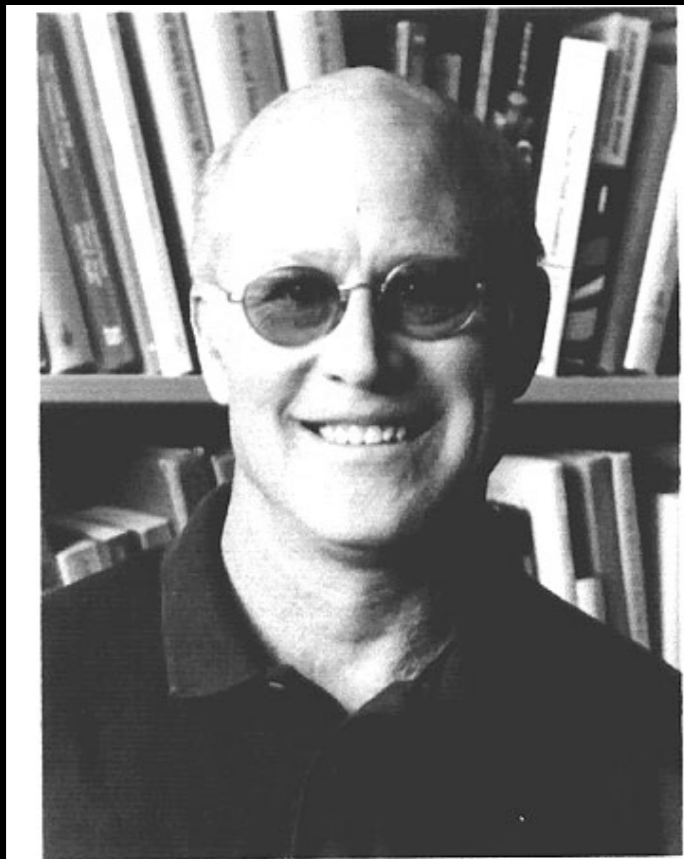
# Acknowledgements

- FCT: POCI/MAR/57265/2004
- CIIMAR
- Changming Dong, UCLA, USA

# Philosophy

**“Never trust an observation without without a supporting theory.”**

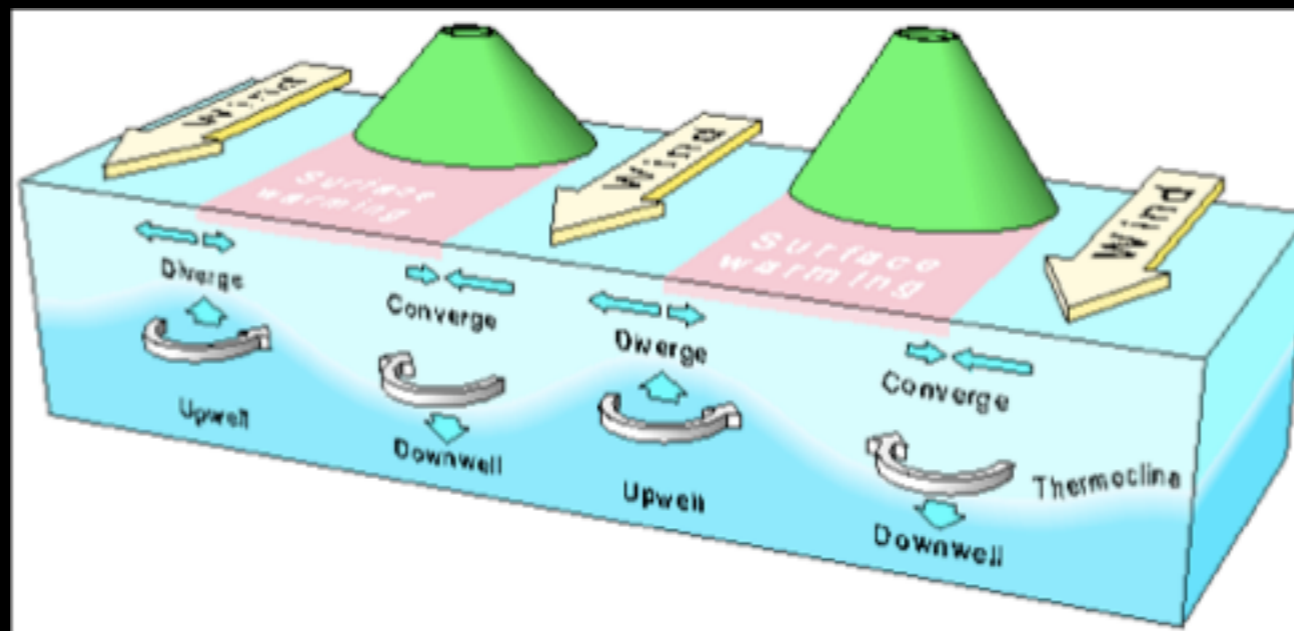
***Arthur Eddington, 1822-1944***



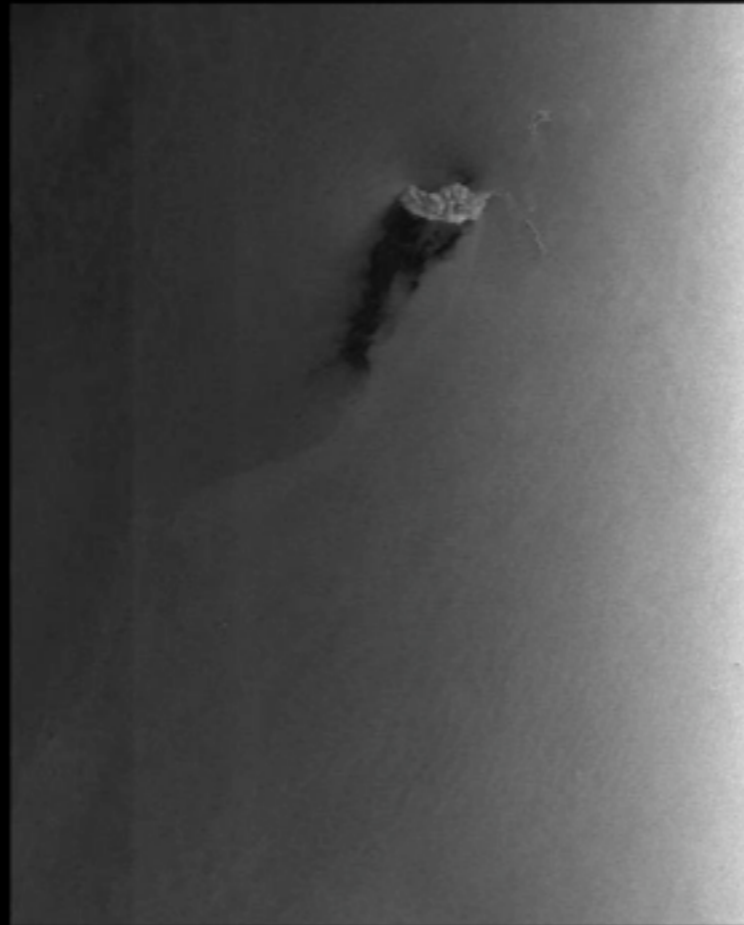
**“In geophysics, never trust a fact, or a simulation, without a supporting interpretation.”**

***James McWilliams, 2006***

# Definition



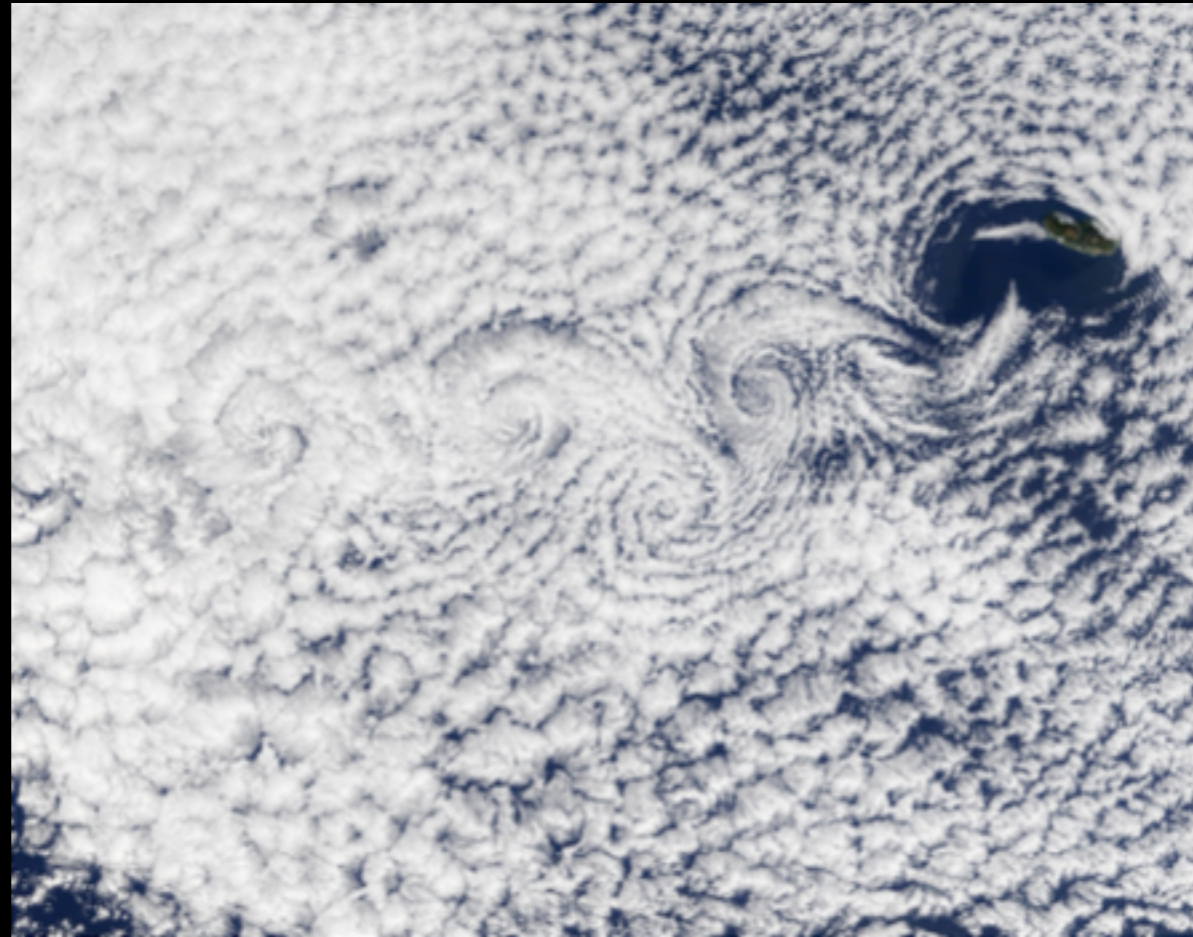
# Definition



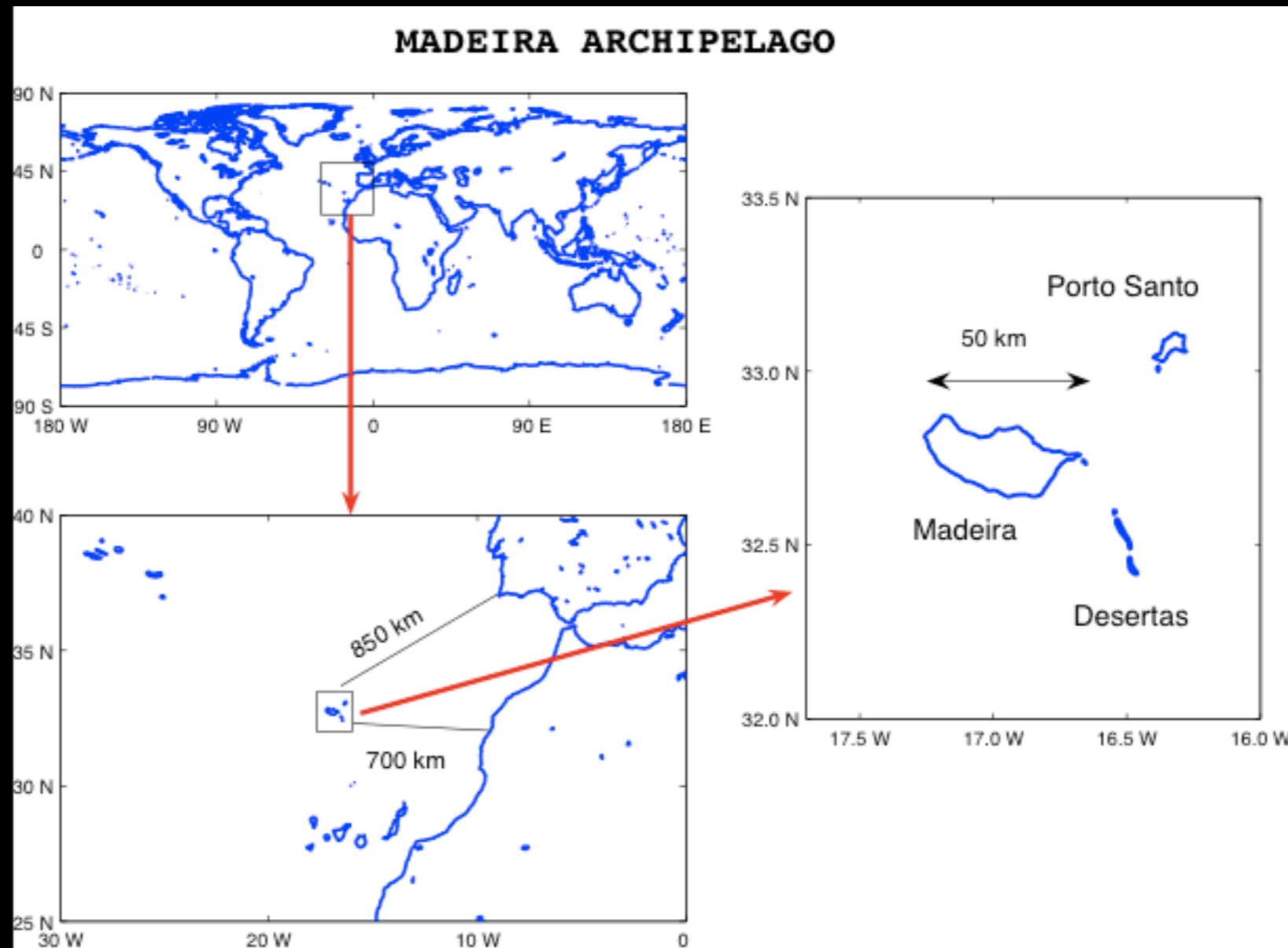
# Definition



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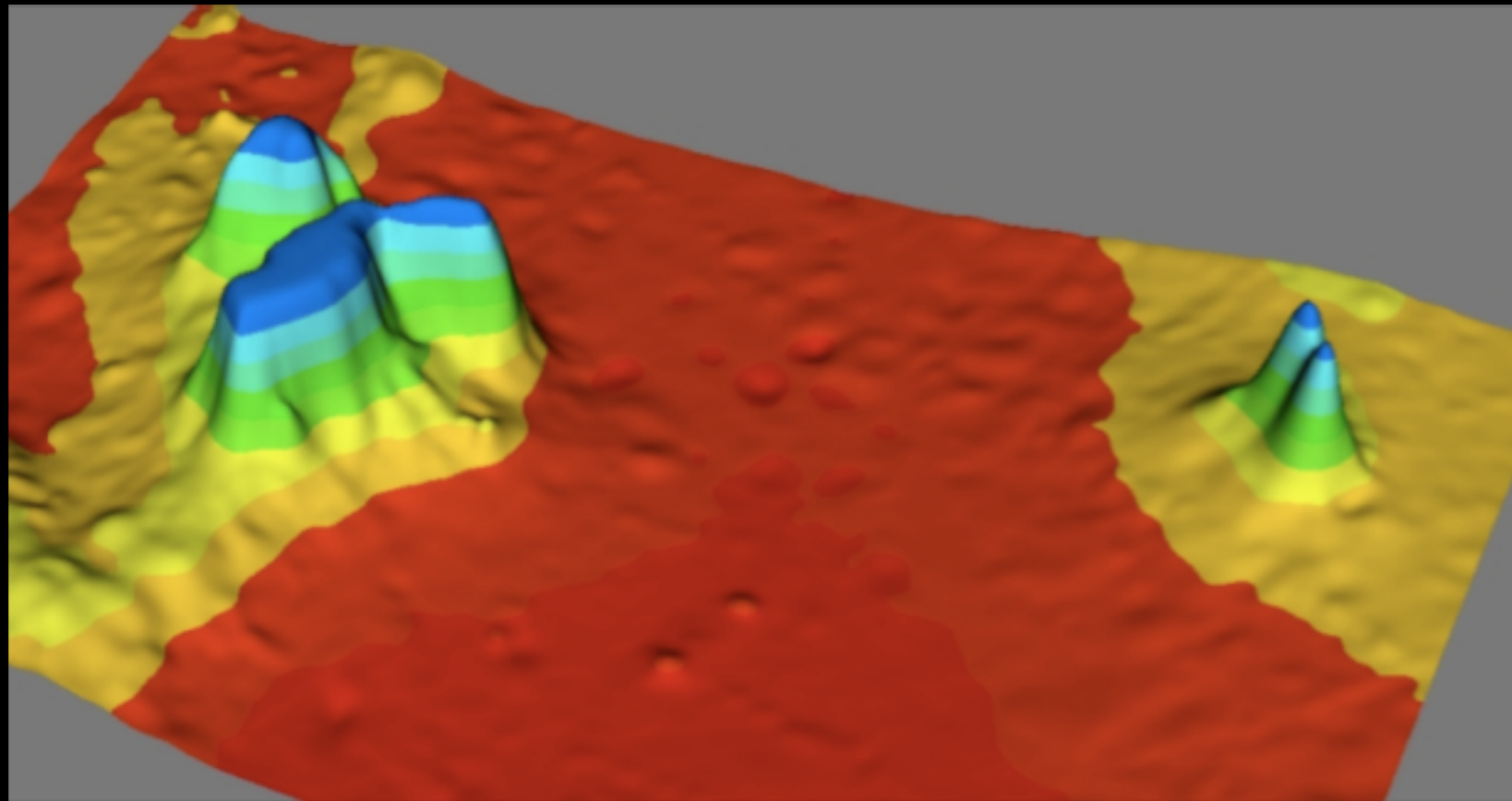


# Geographic setting





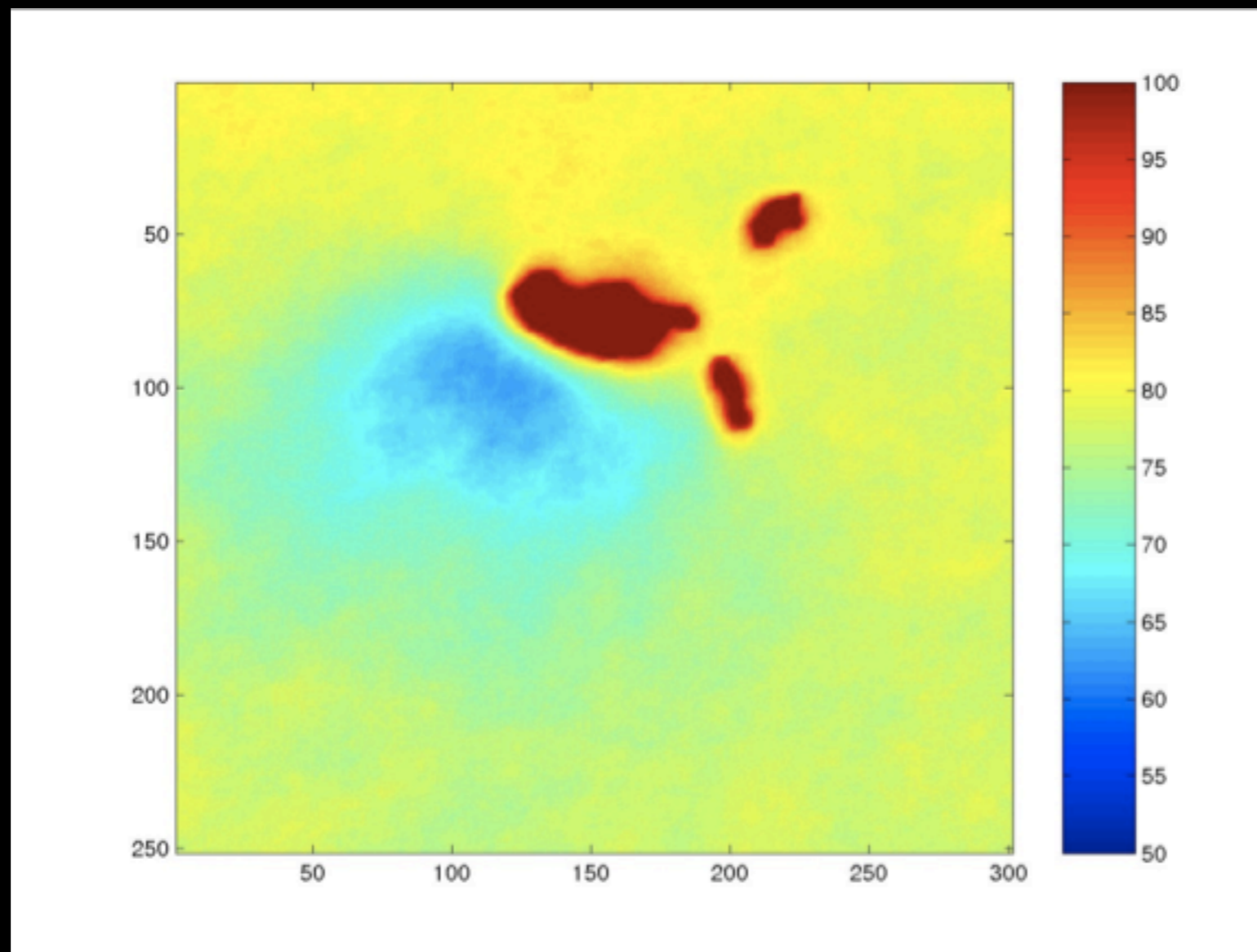
# Geographic setting



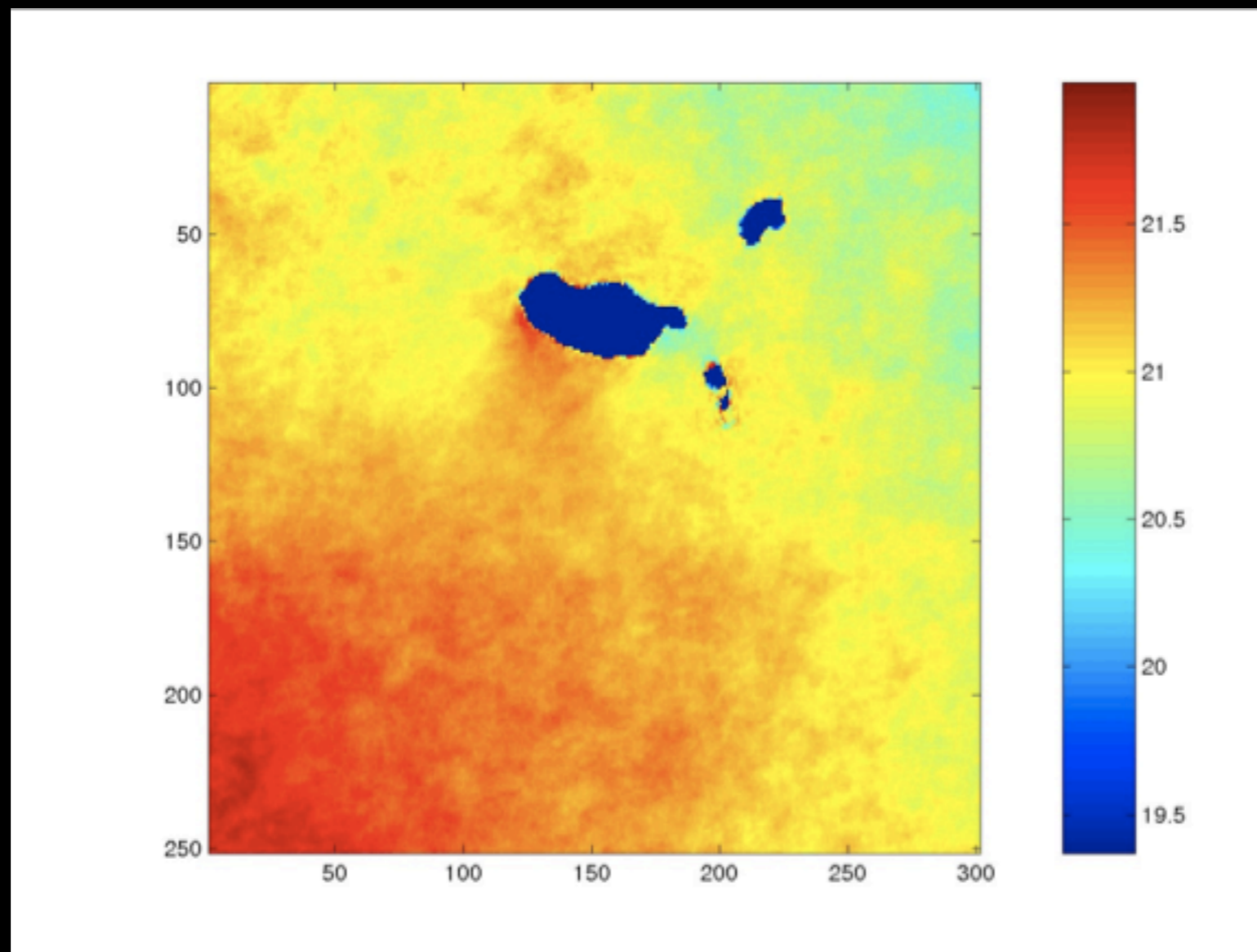
# Remote sensing data 2001-2008



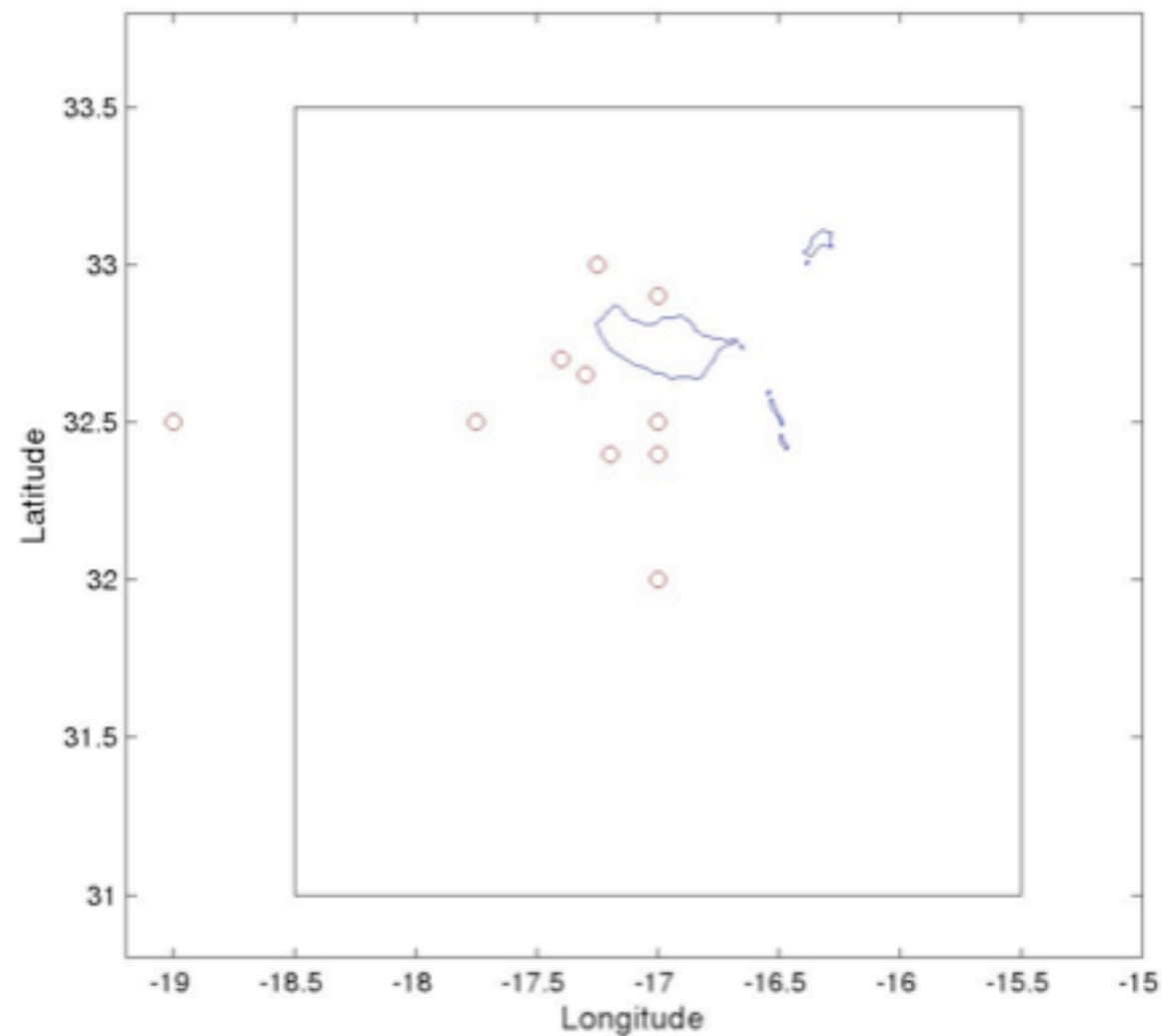
# Remote sensing data 2001-2008



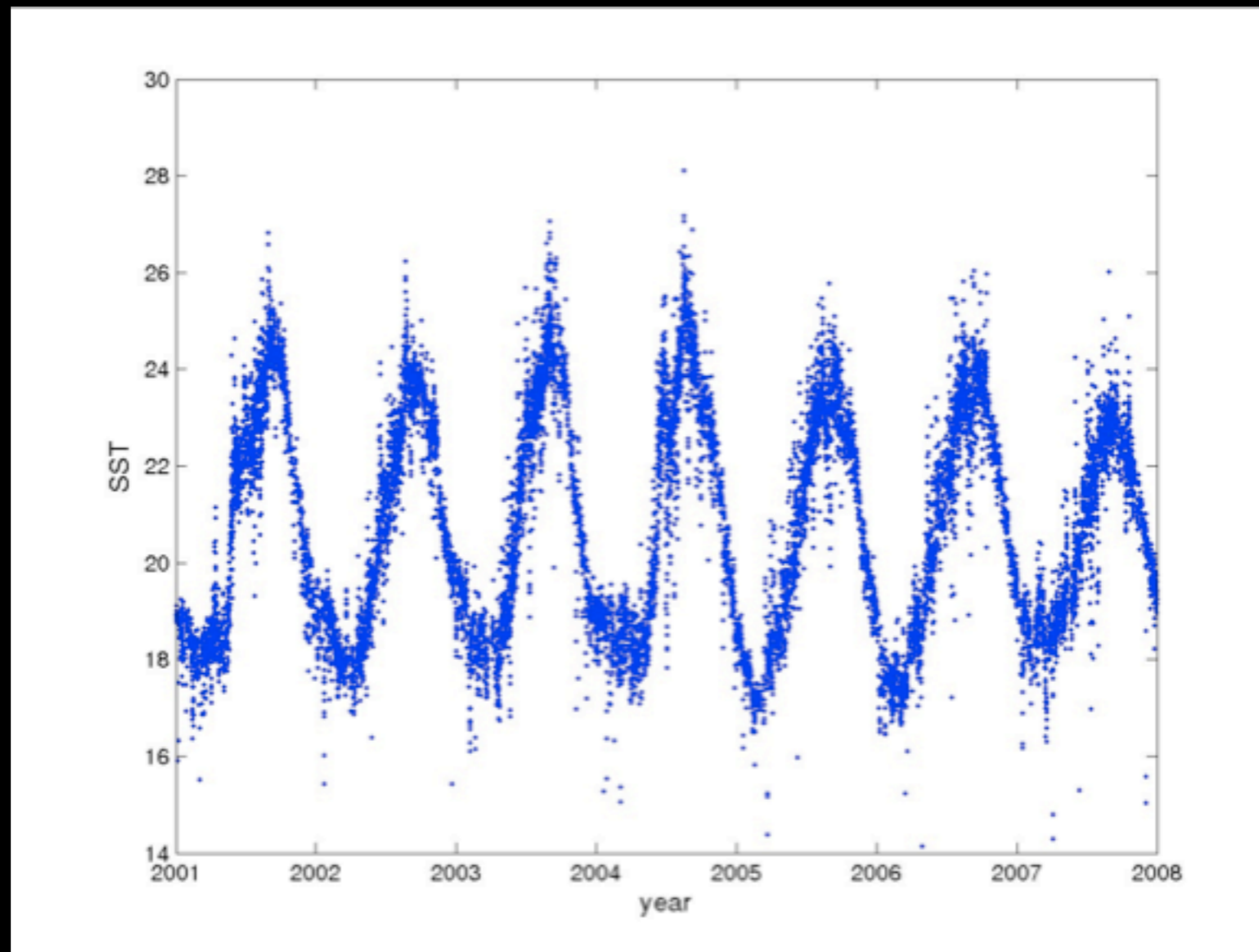
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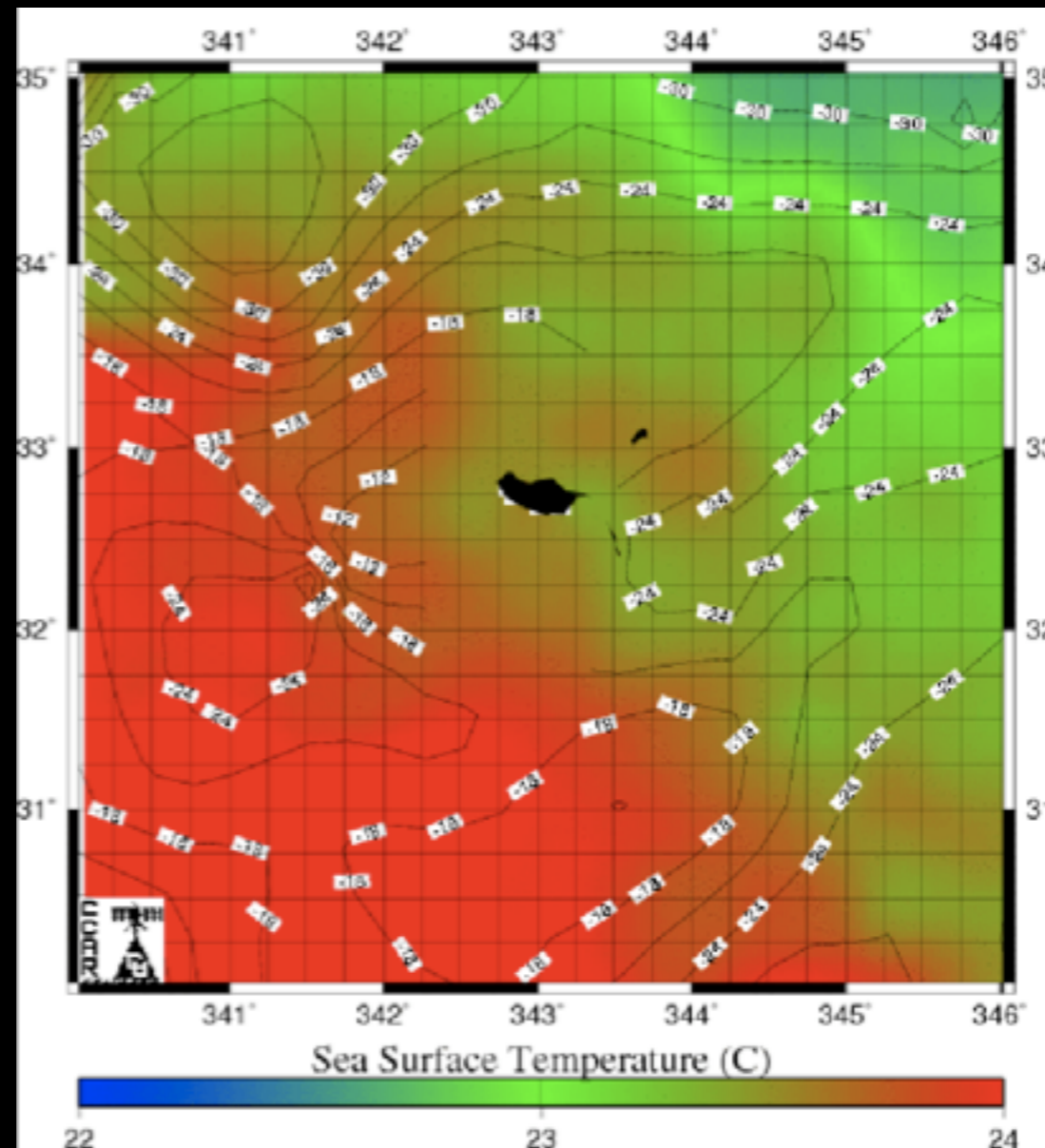


# Remote sensing data 2001-2008



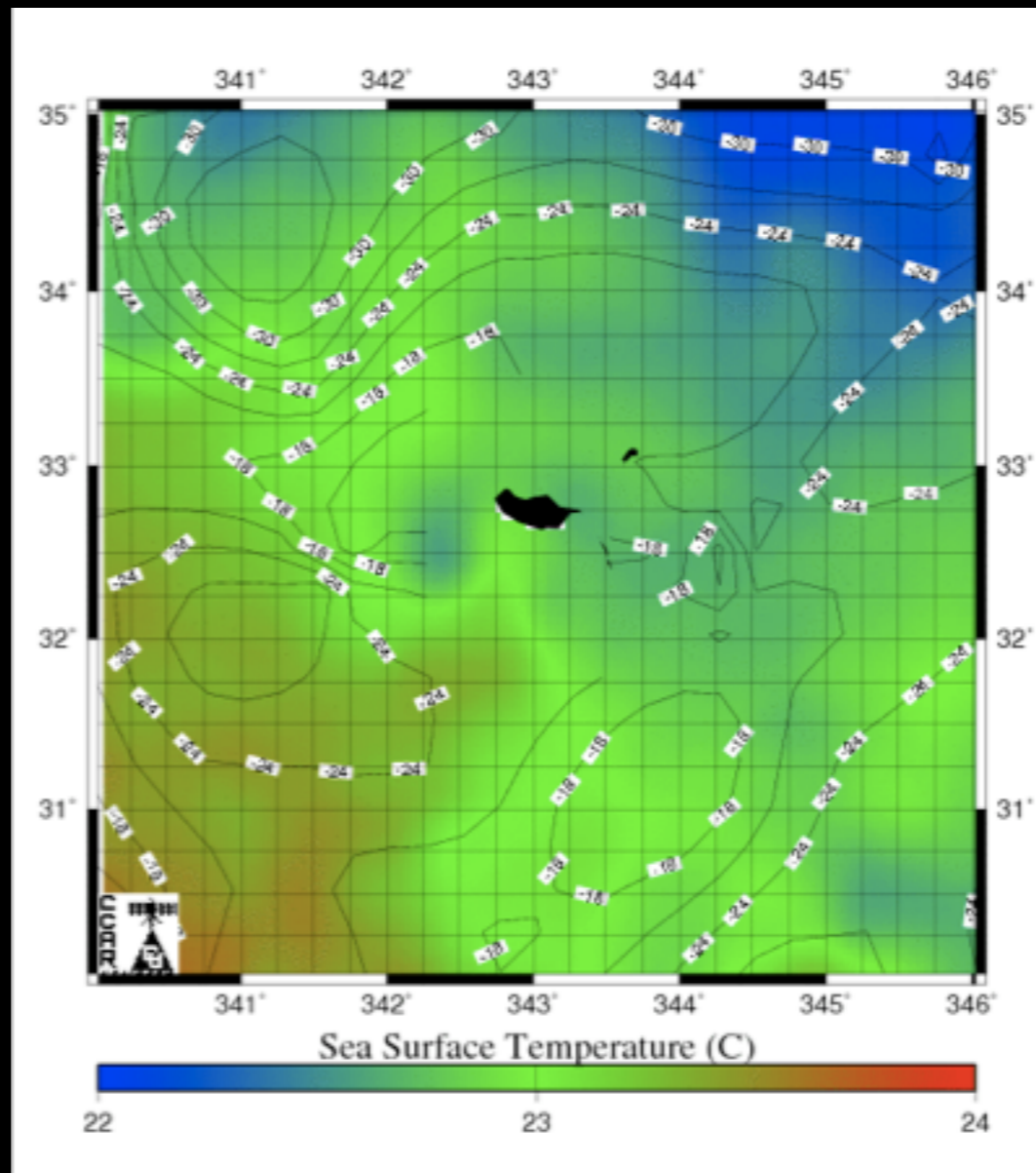
# Remote Sensing

## 09-11 2006 episode



# Remote Sensing

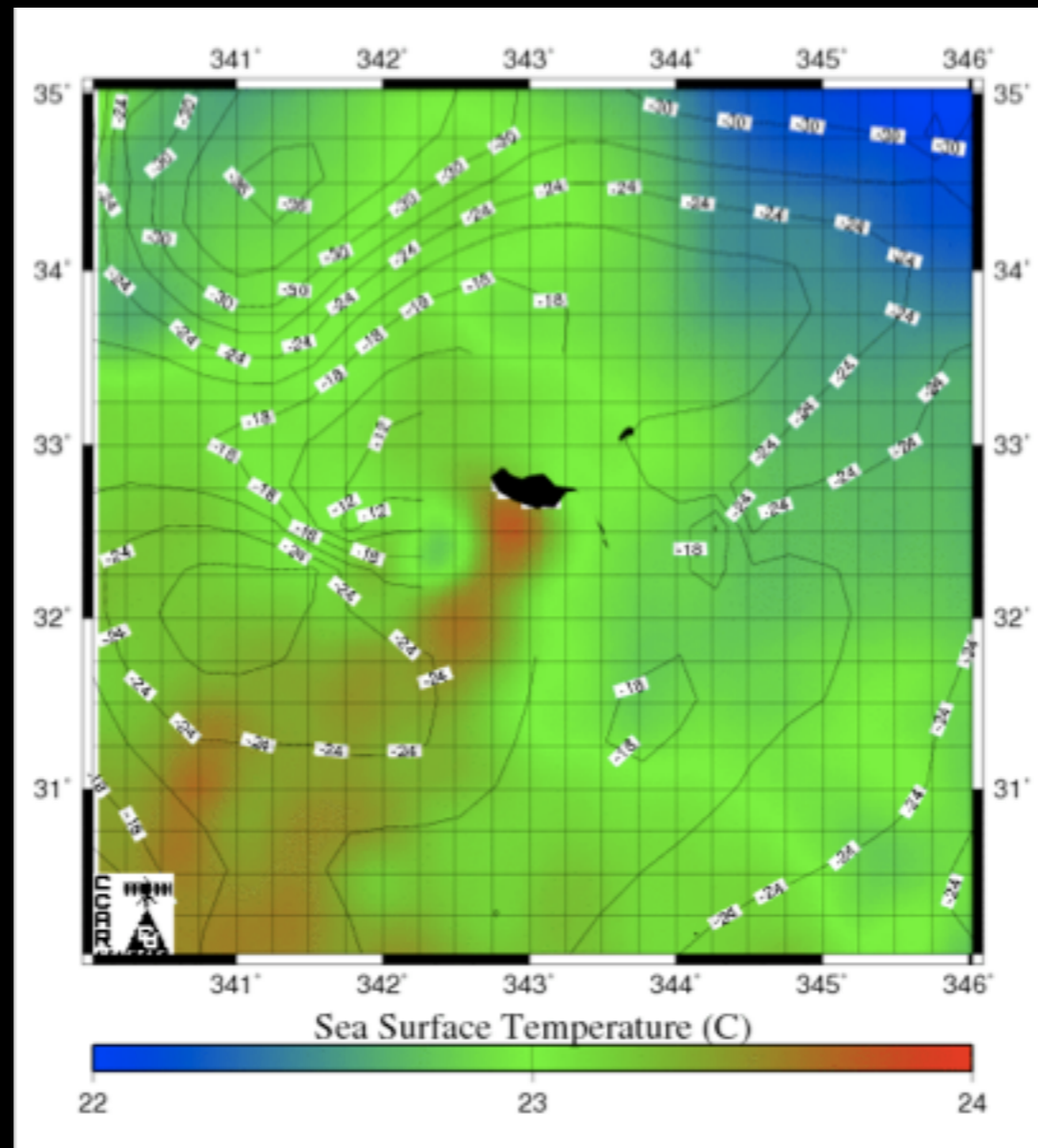
## 09-11 2006 episode





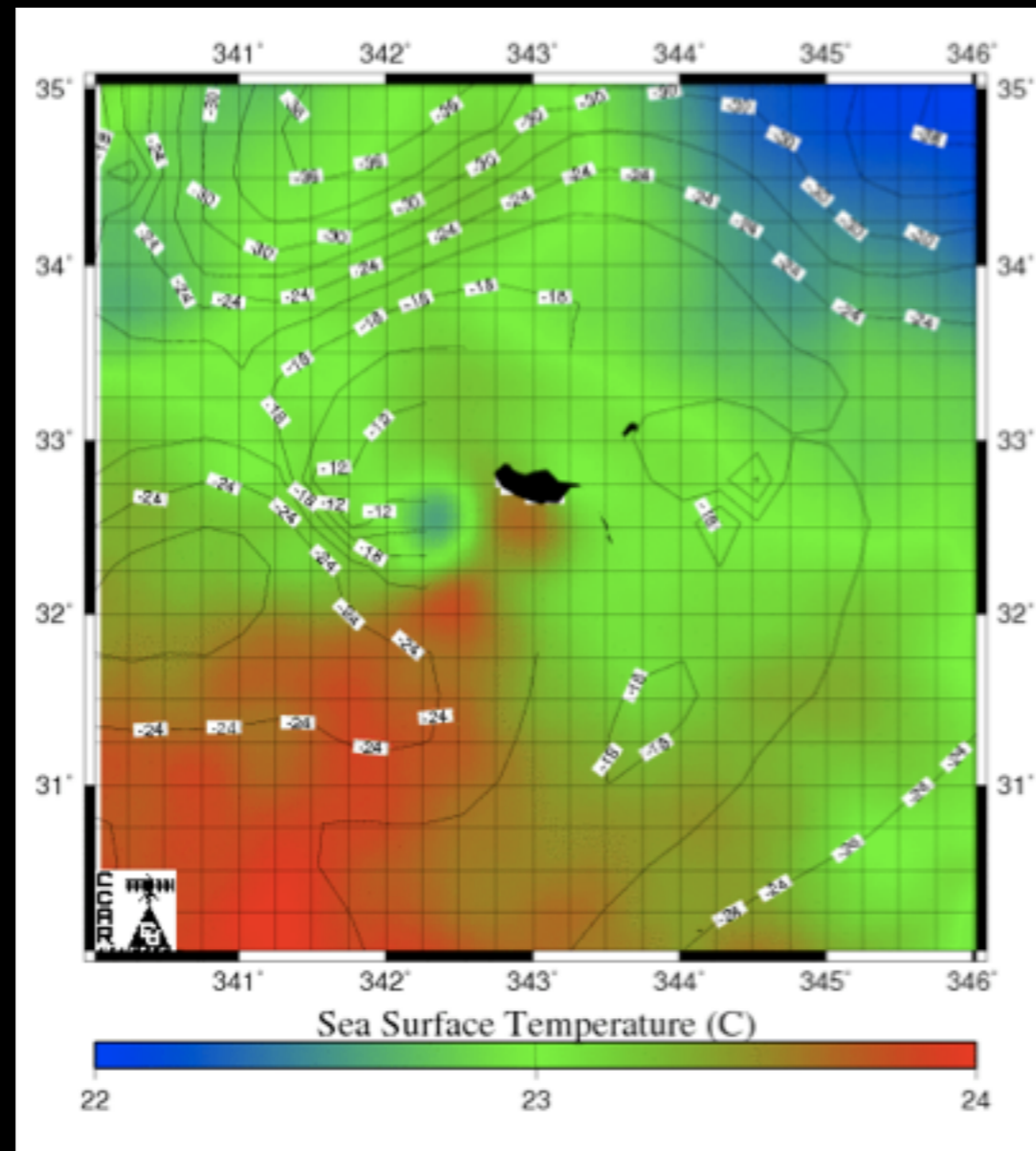
# Remote Sensing

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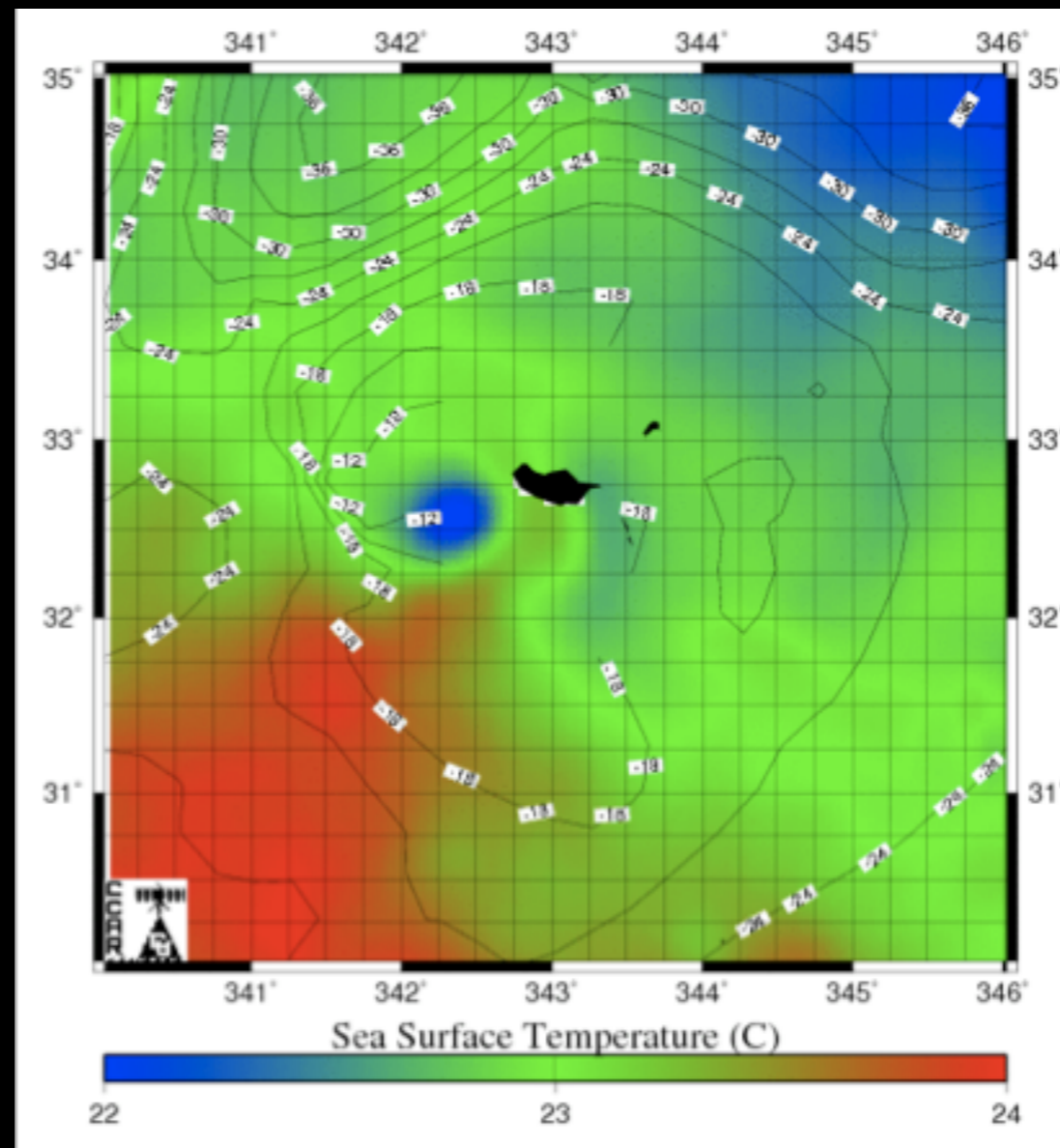
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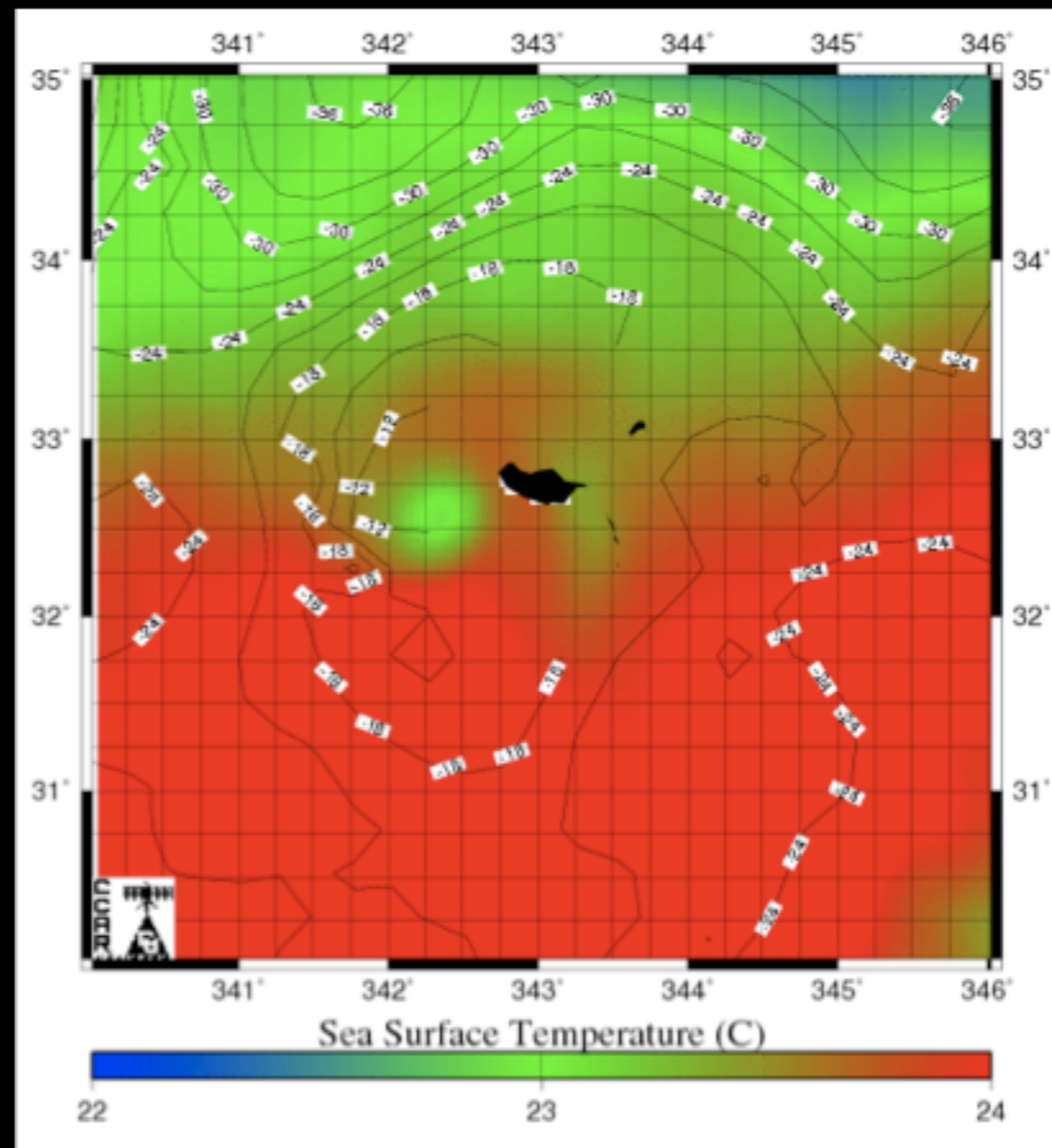
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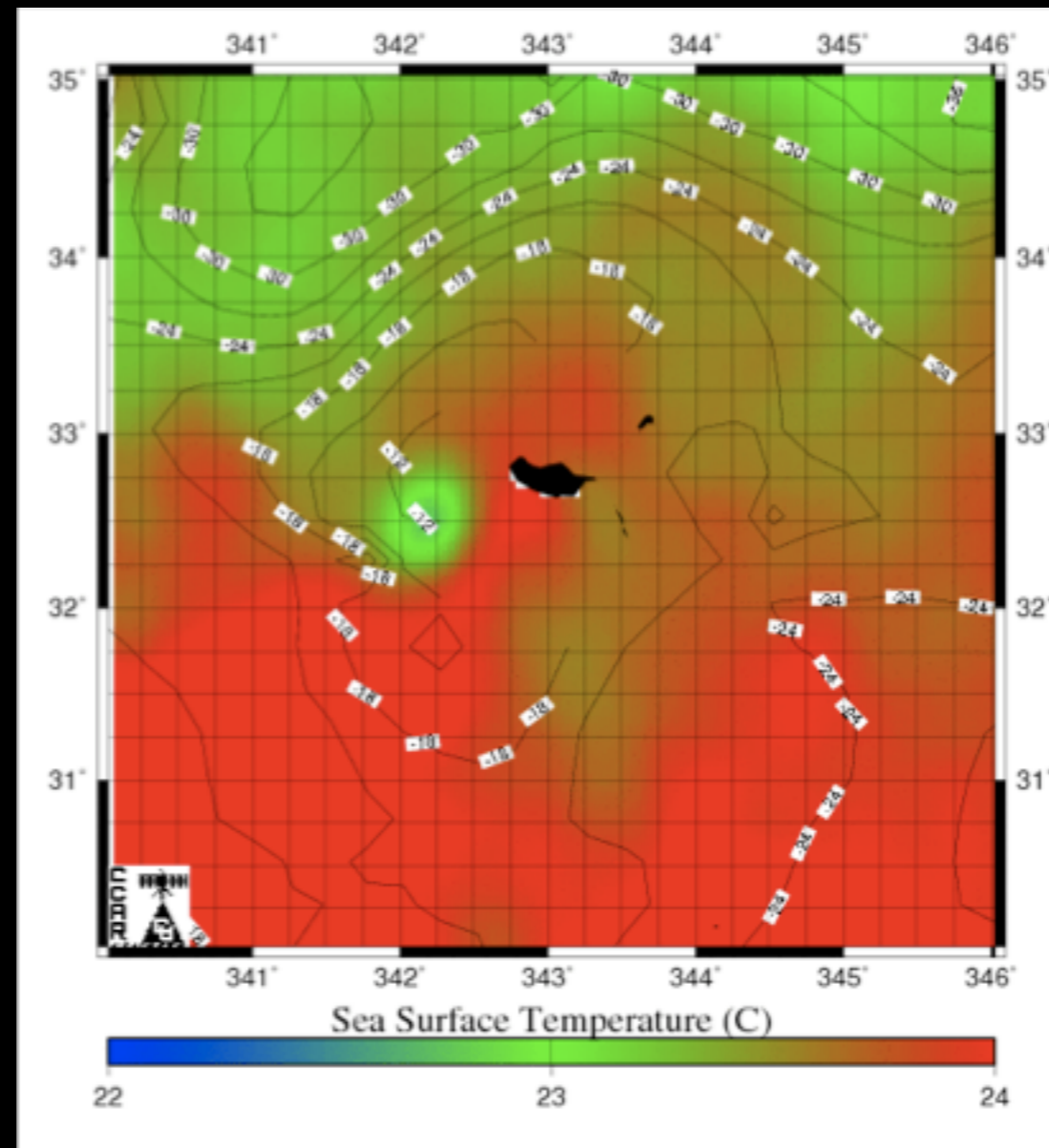
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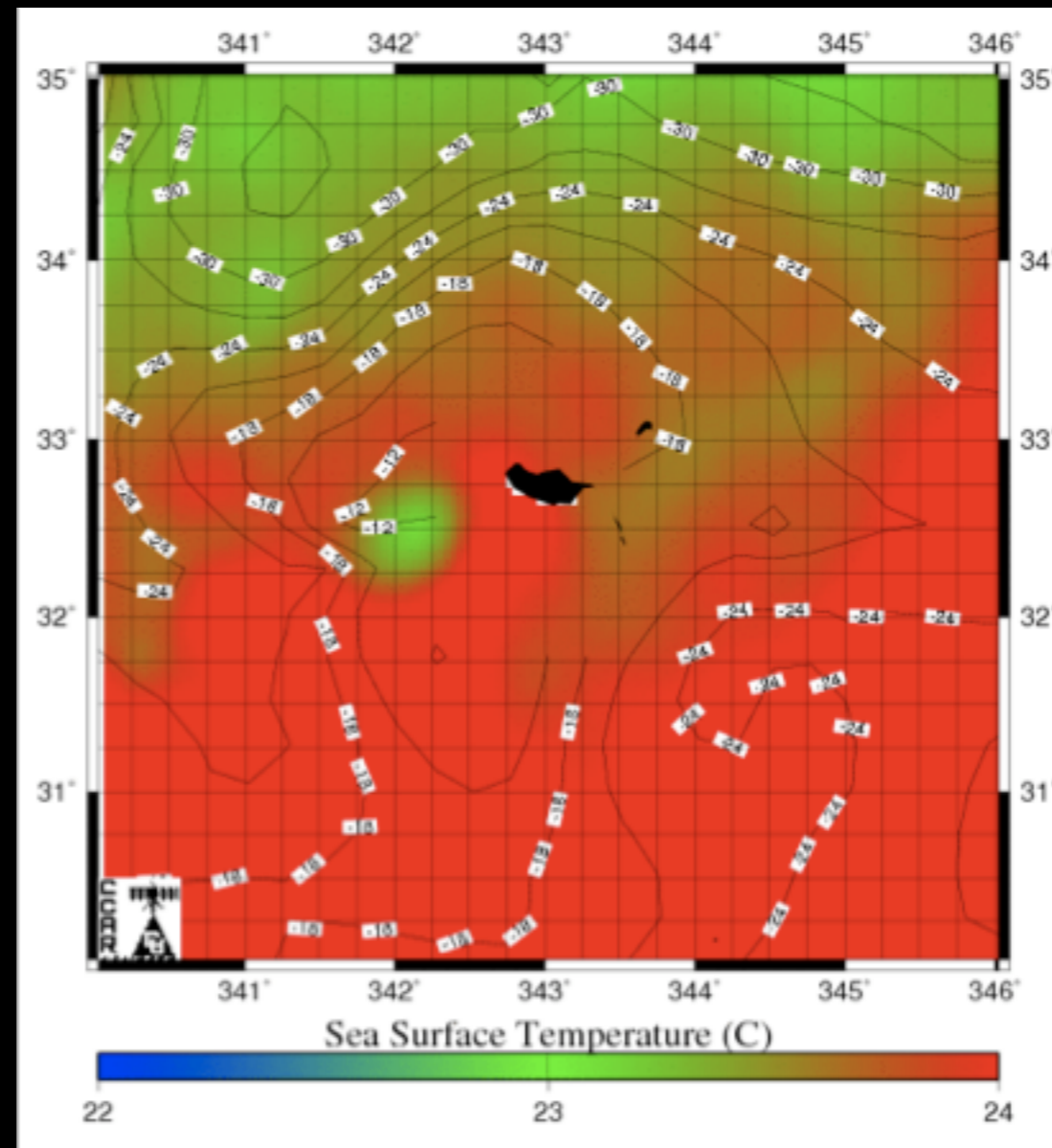
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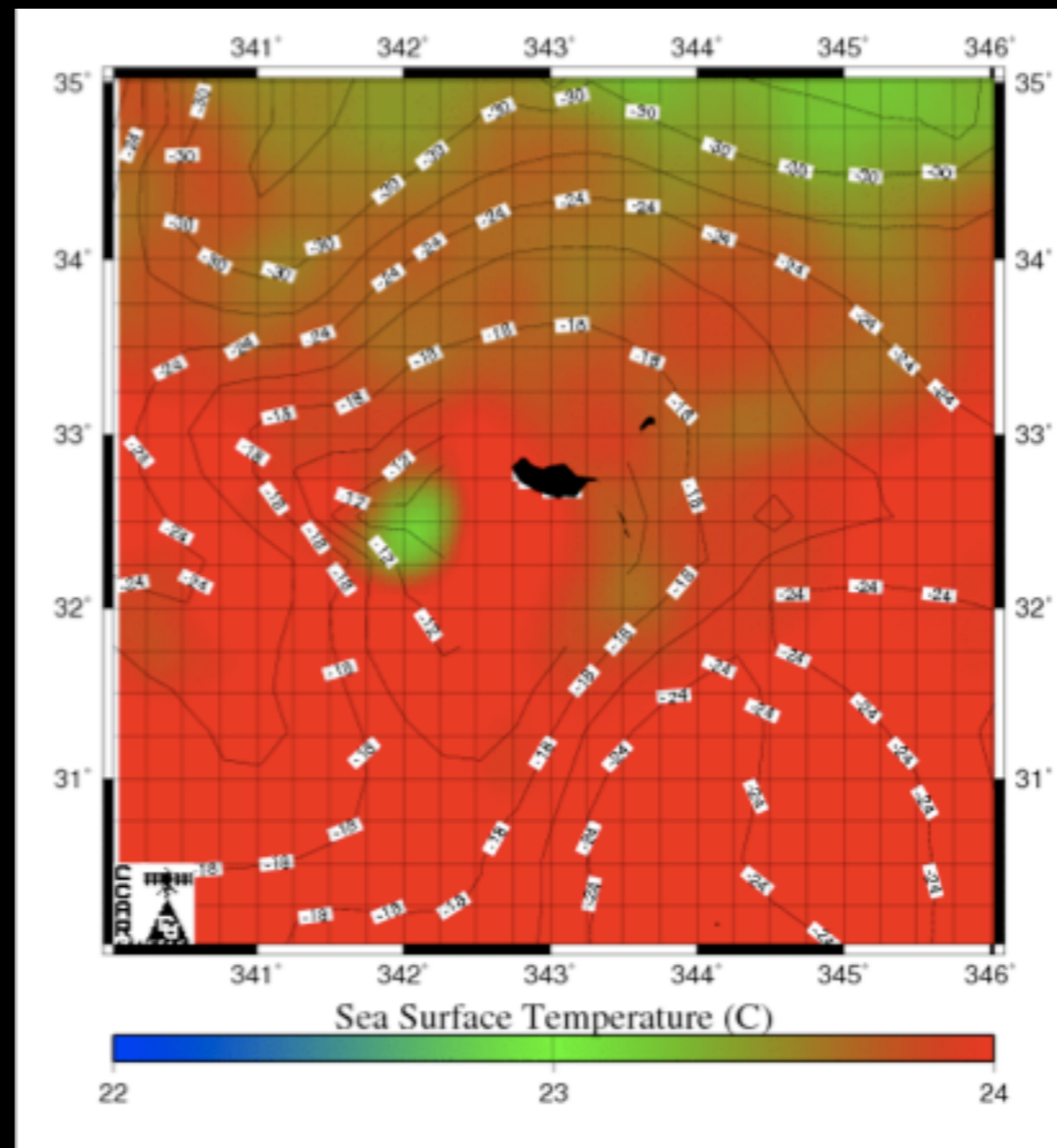
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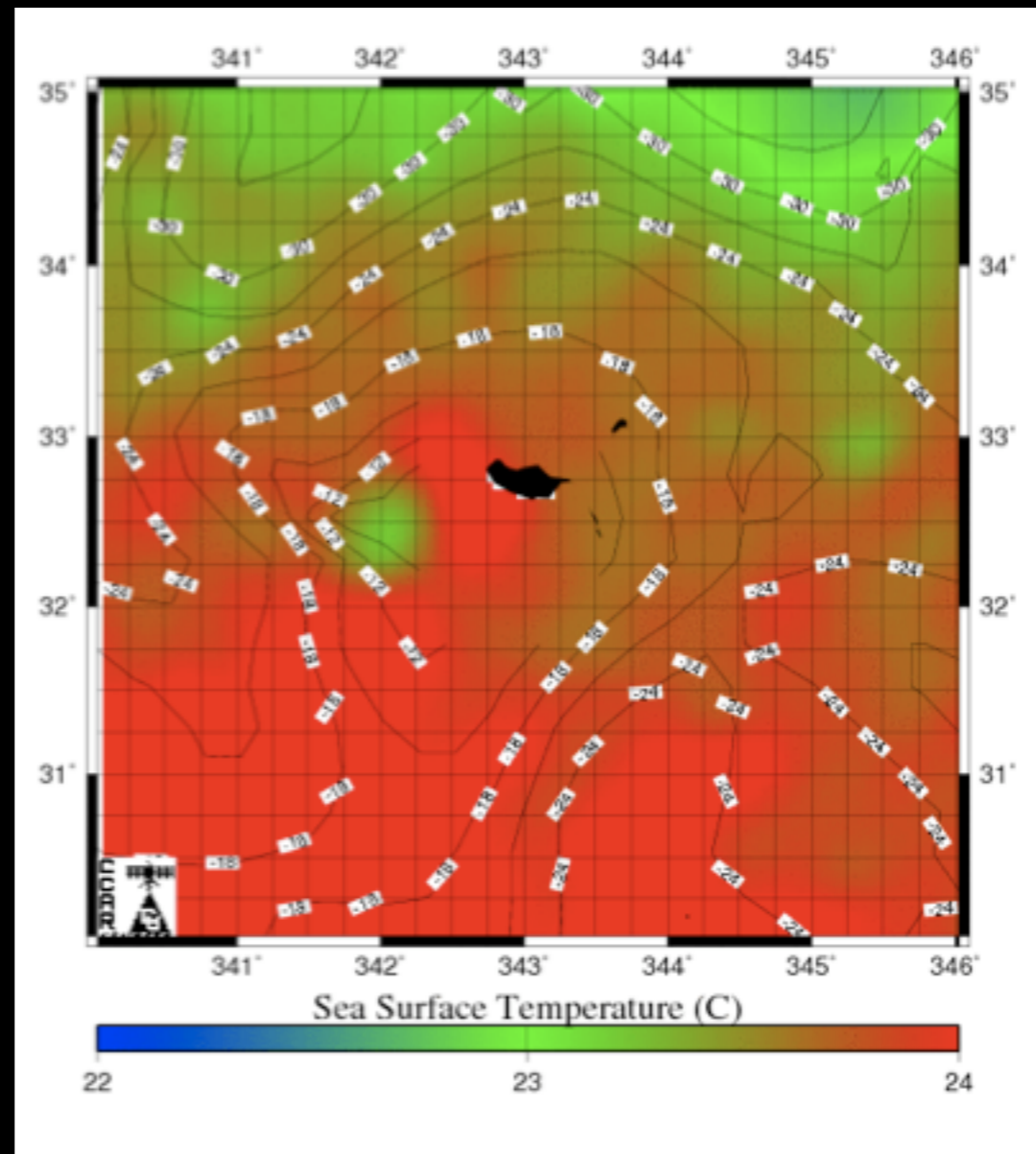
# Remote Sensing

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# Remote Sensing

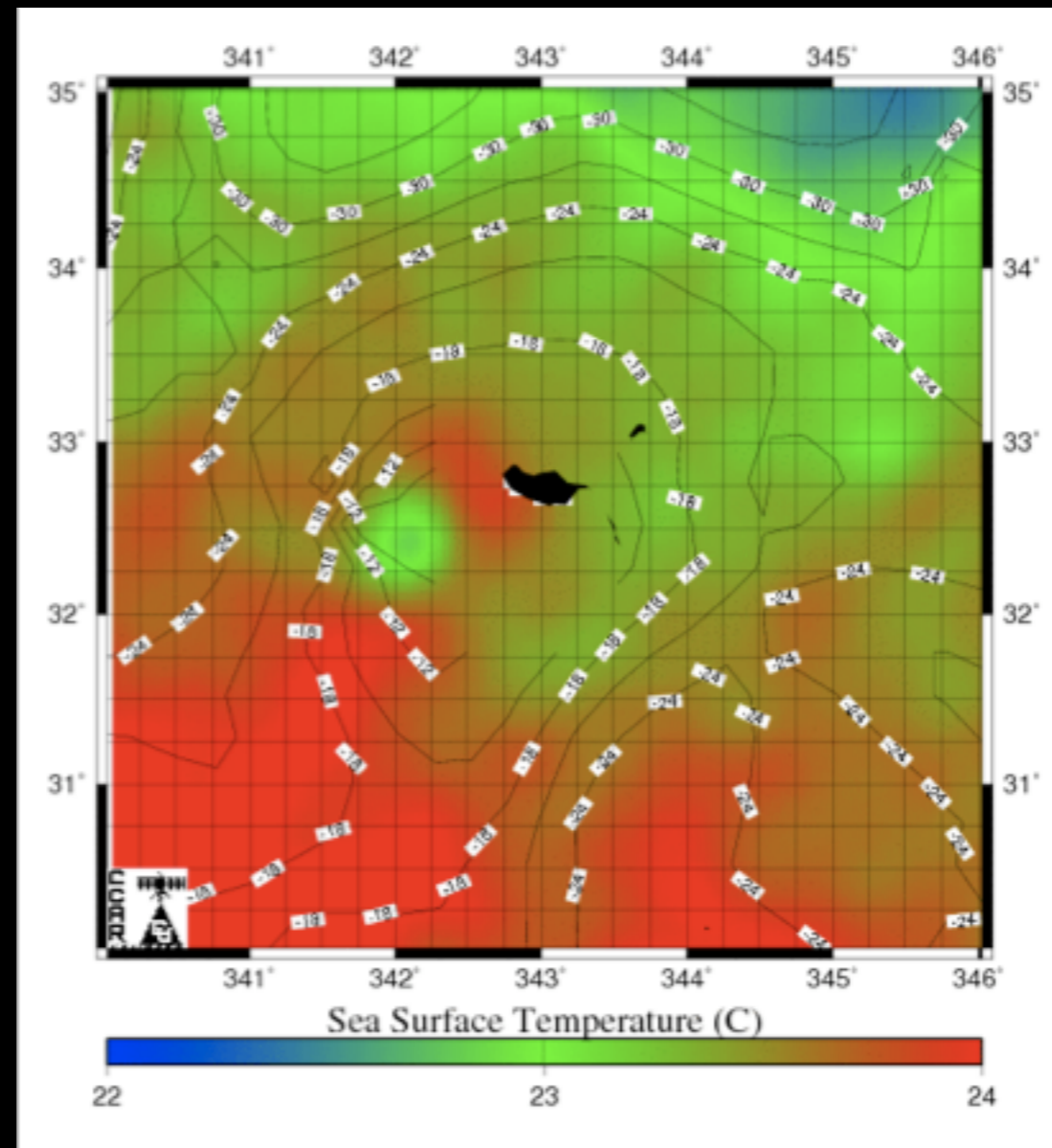
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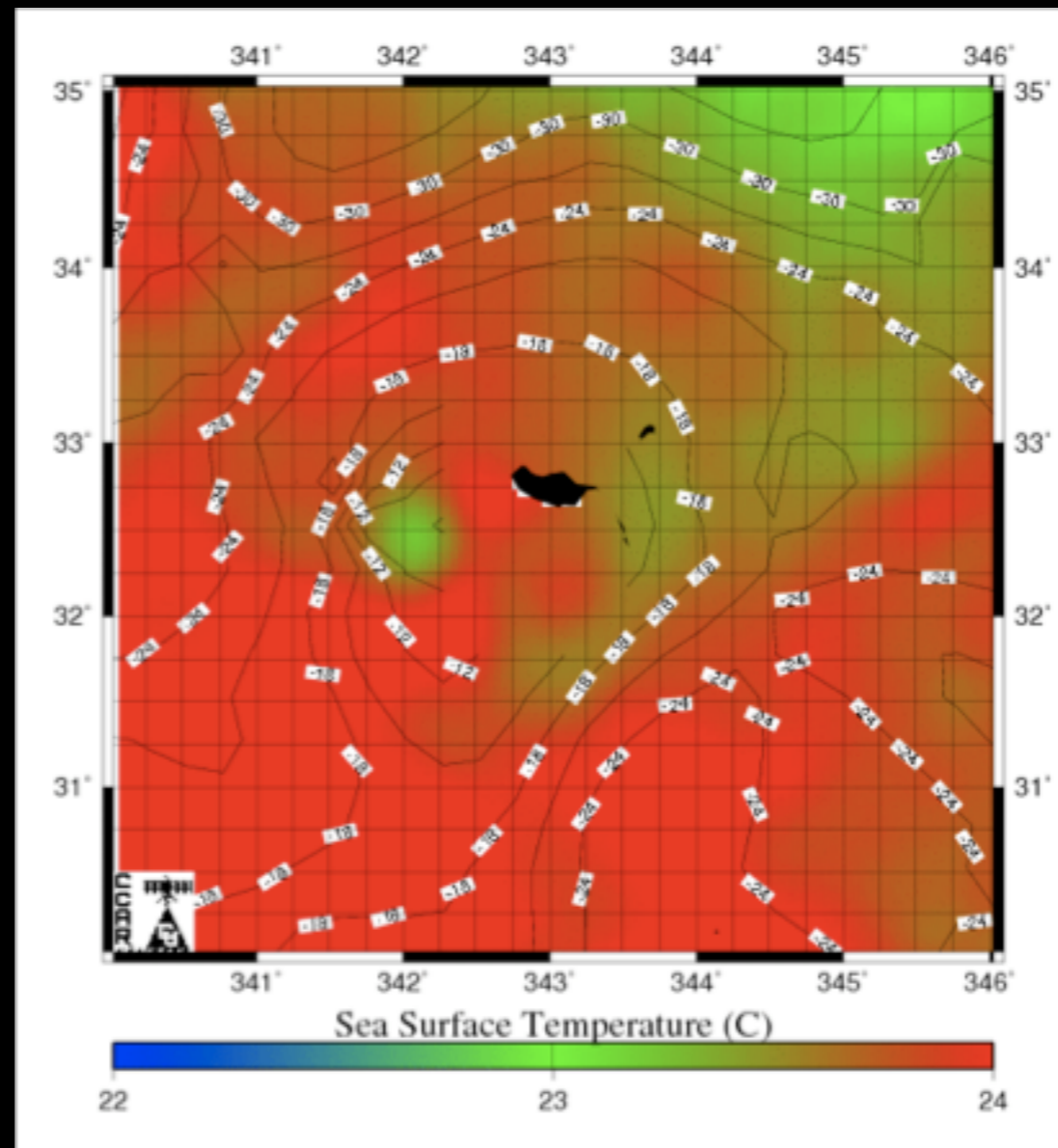
# Remote Sensing

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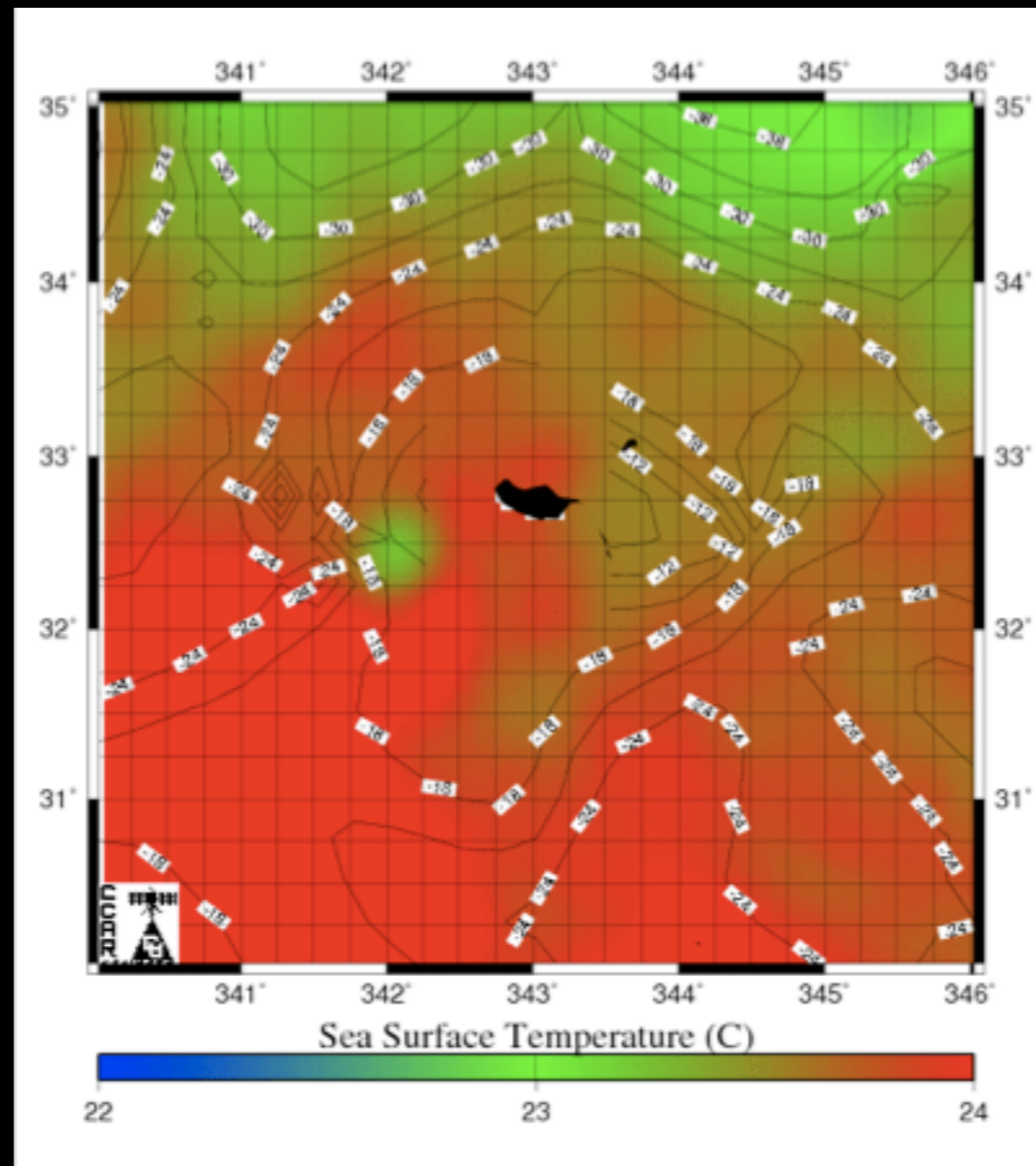
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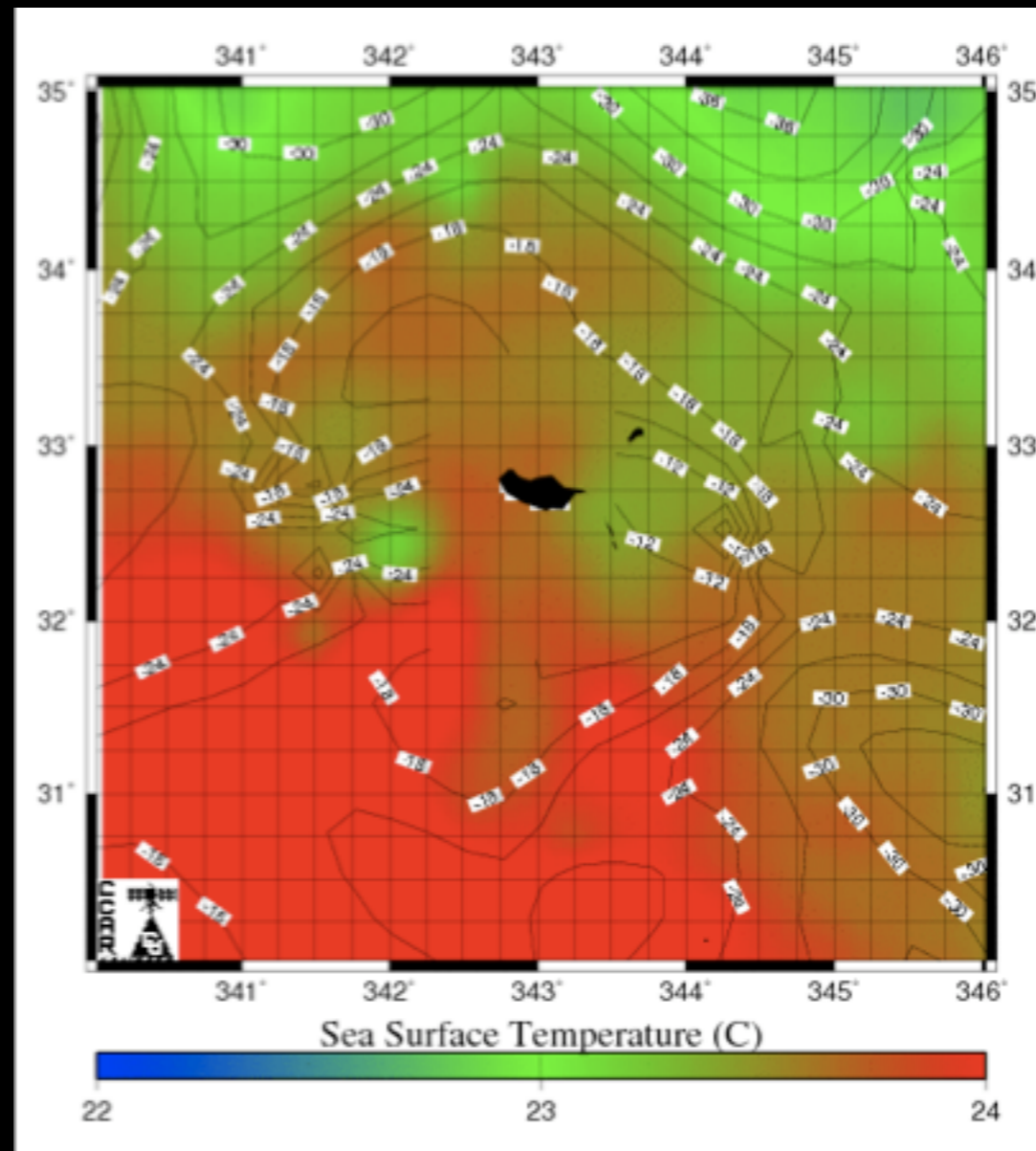
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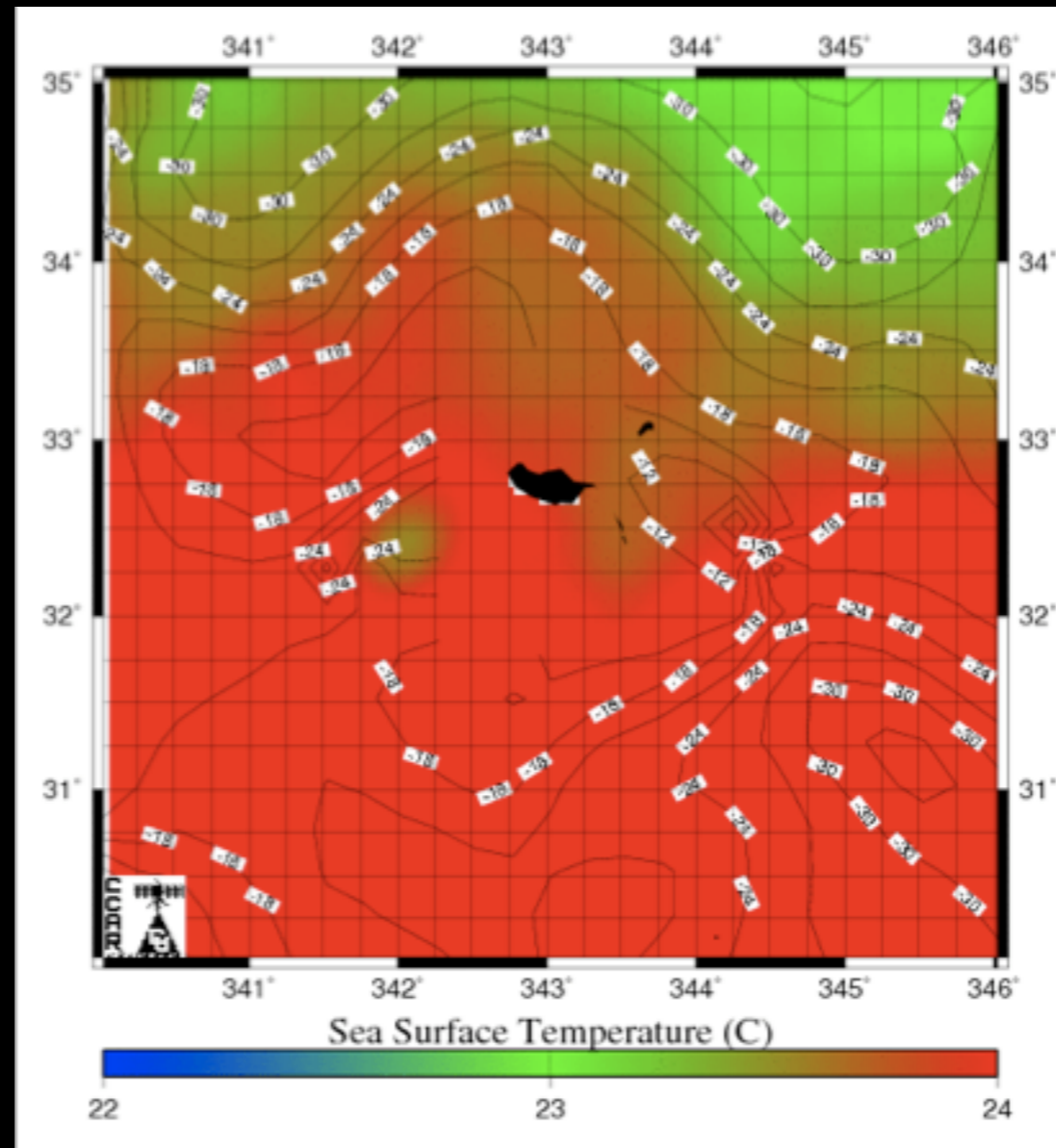
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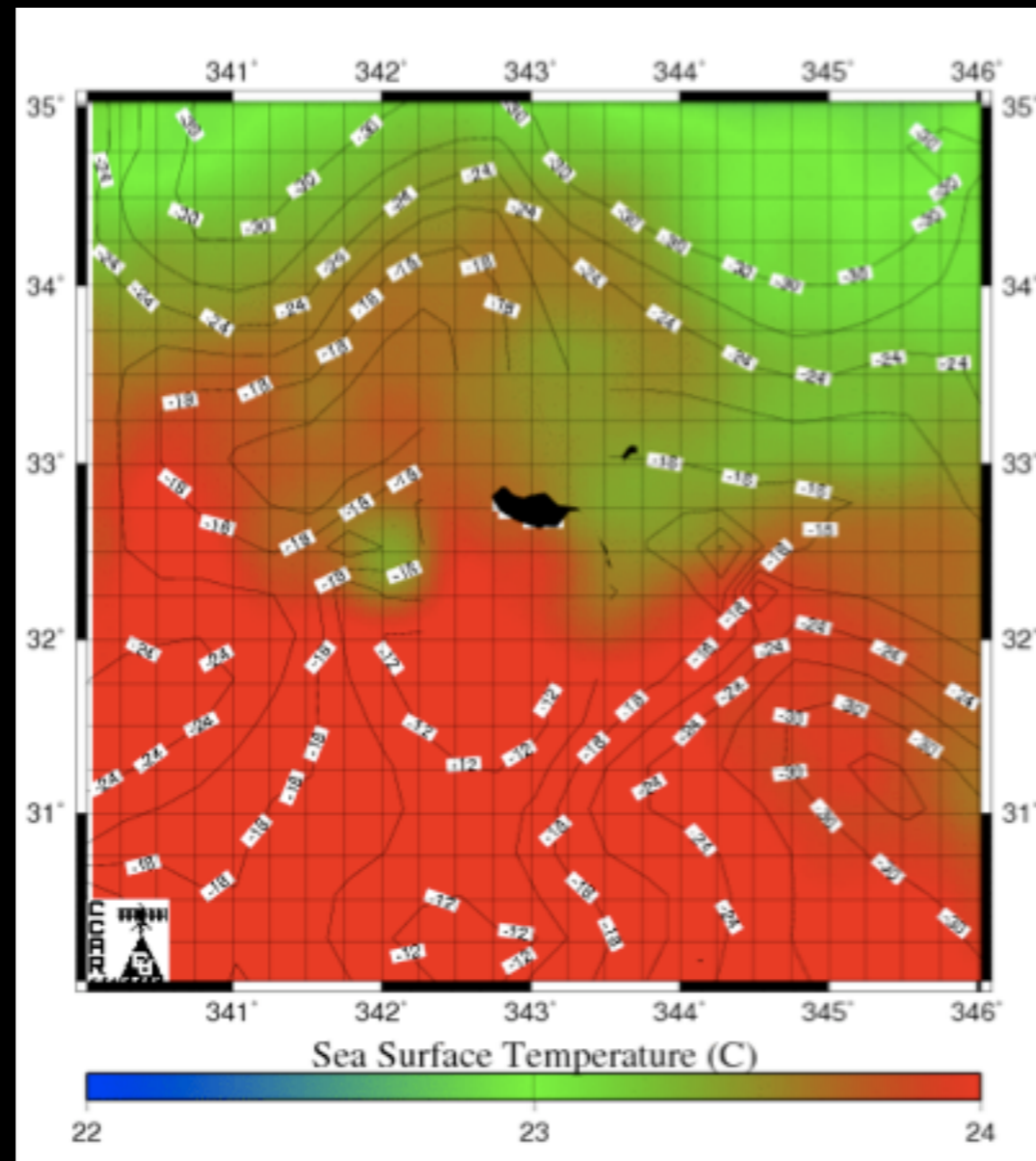
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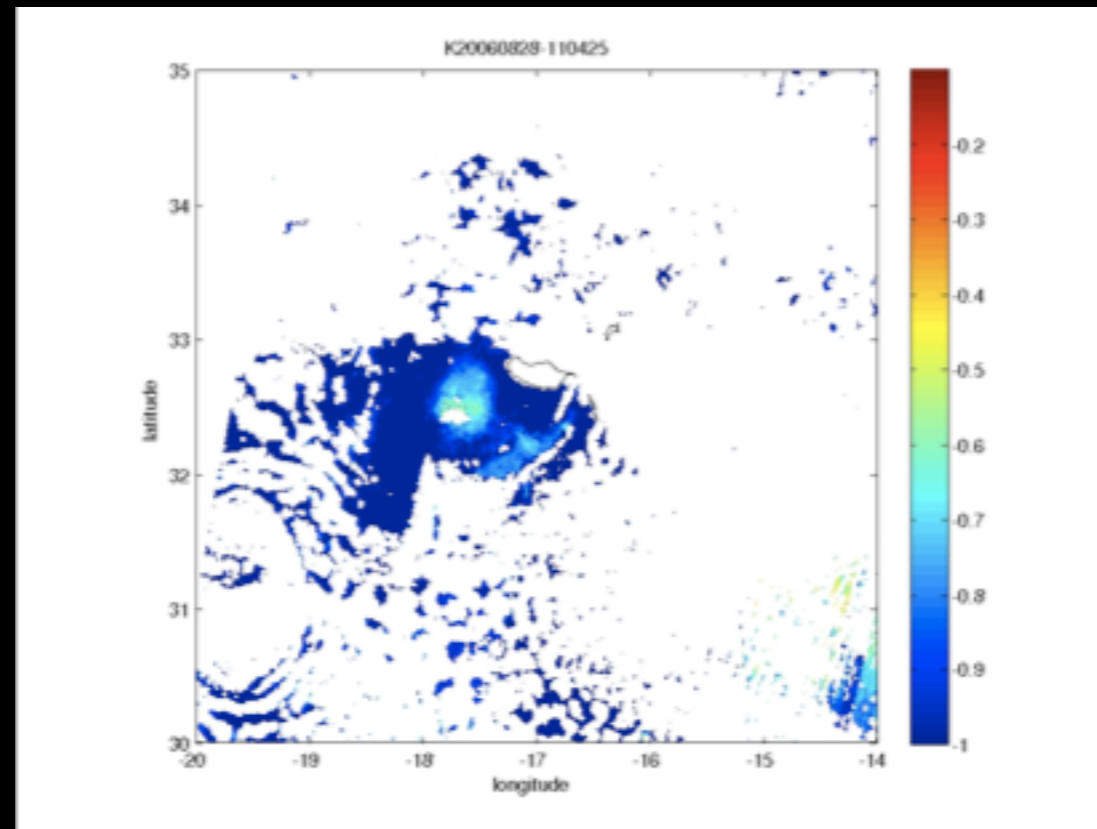
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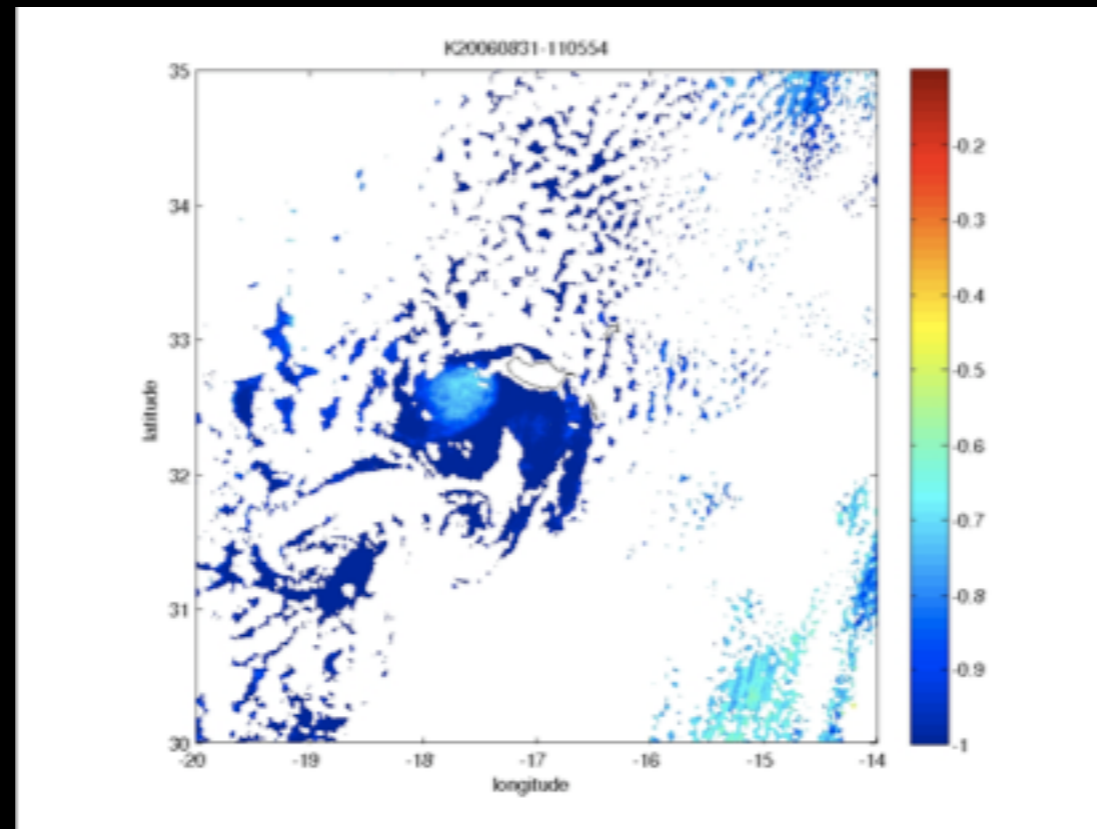
# Remote Sensing

## 09-11 2006 episode



# Remote Sensing

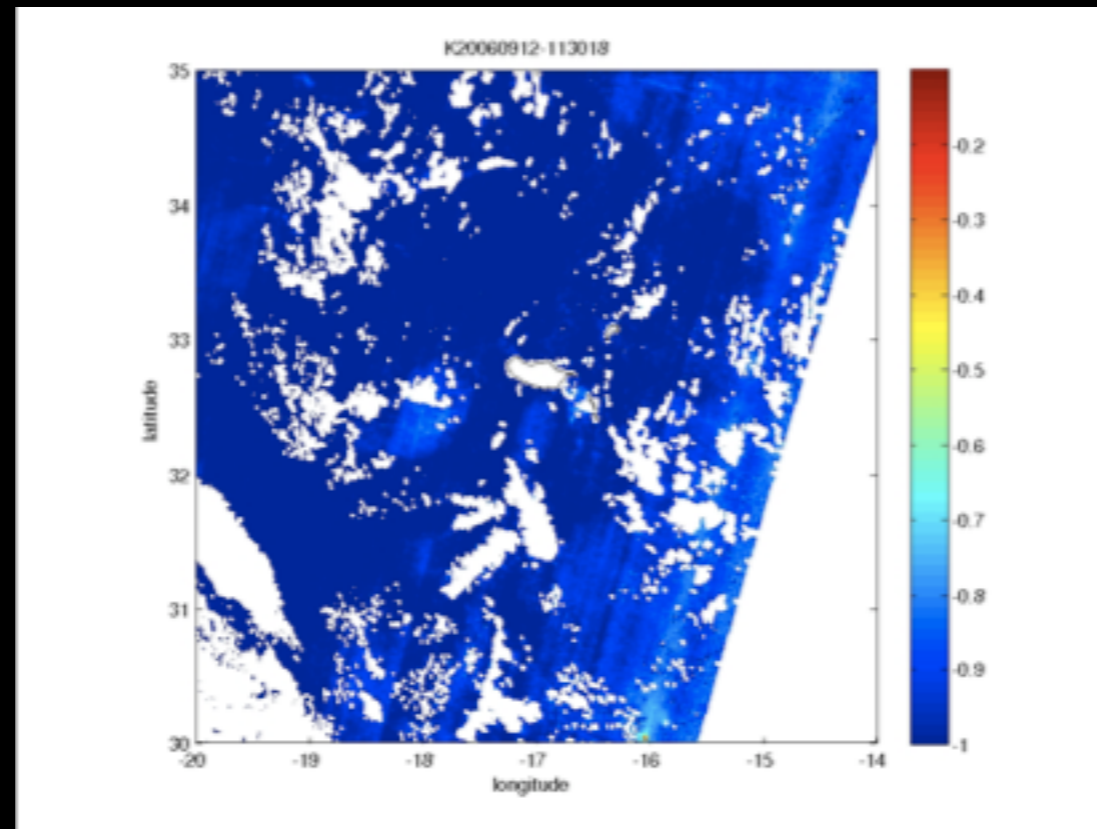
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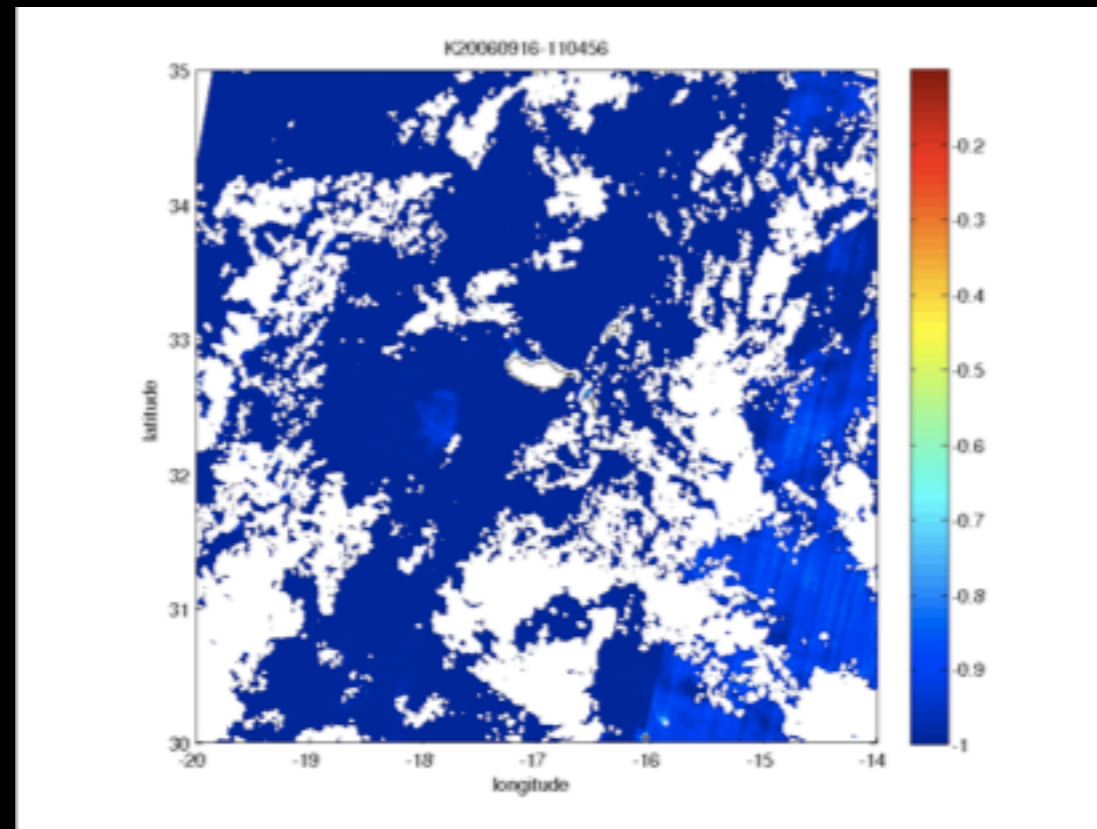
# Remote Sensing

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# Remote Sensing

## 09-11 2006 episode



# Data Interpolating Empirical Orthogonal Functions

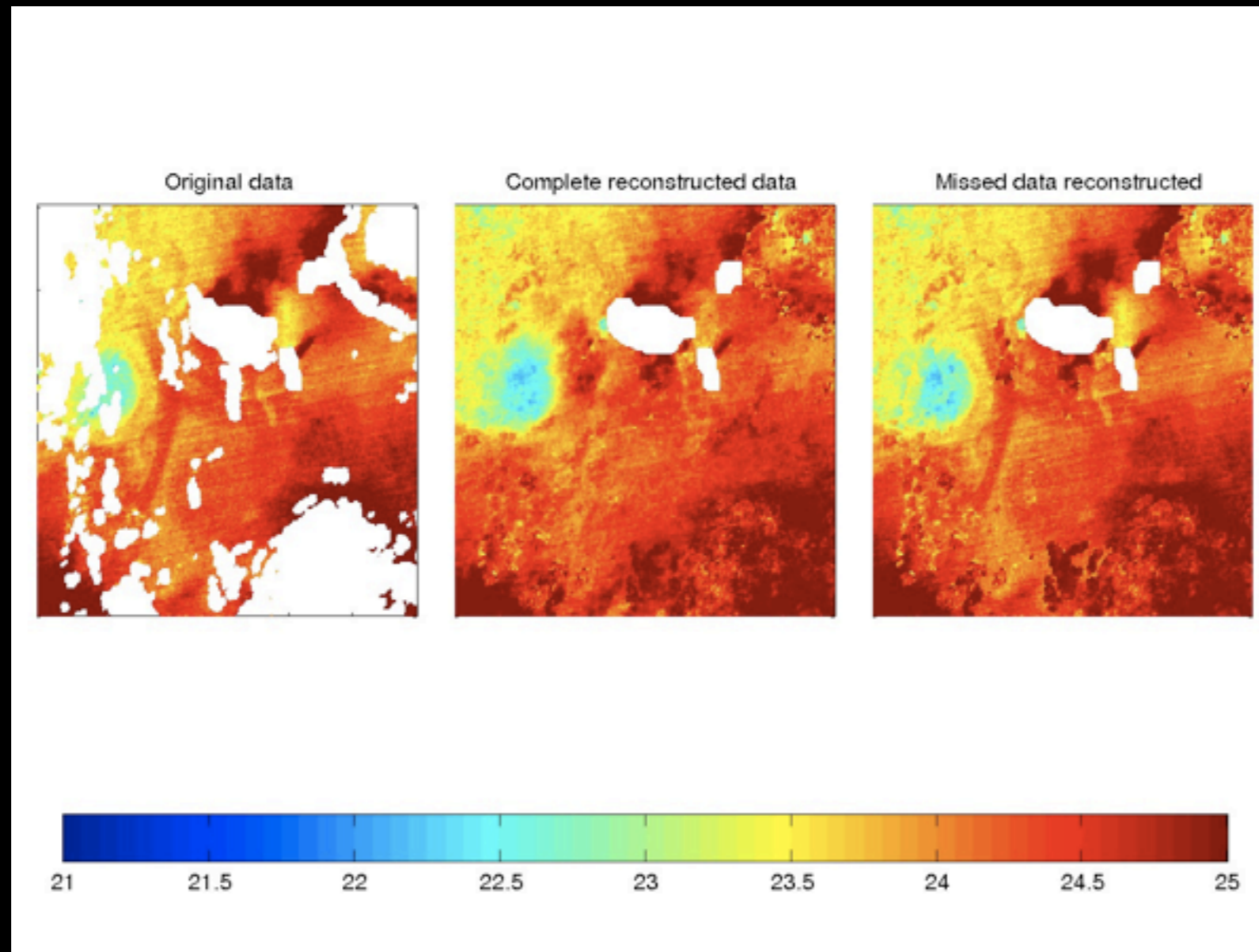
$$d(\varphi, \lambda, t) = \bar{d}(\varphi, \lambda) + \sum_{j=1}^n \underbrace{m_j(\varphi, \lambda)}_{\text{spatial comp.}} \cdot \underbrace{e_j(t)}_{\text{temporal comp.}}$$

$$\Rightarrow d(\varphi, \lambda, t) - \bar{d}(\varphi, \lambda) = \underbrace{\sum_{j=1}^k m_j(\varphi, \lambda) e_j(t)}_{\text{dominant modes}} + \underbrace{\sum_{j=k+1}^n m_j(\varphi, \lambda) e_j(t)}_{\text{secondary modes}}$$

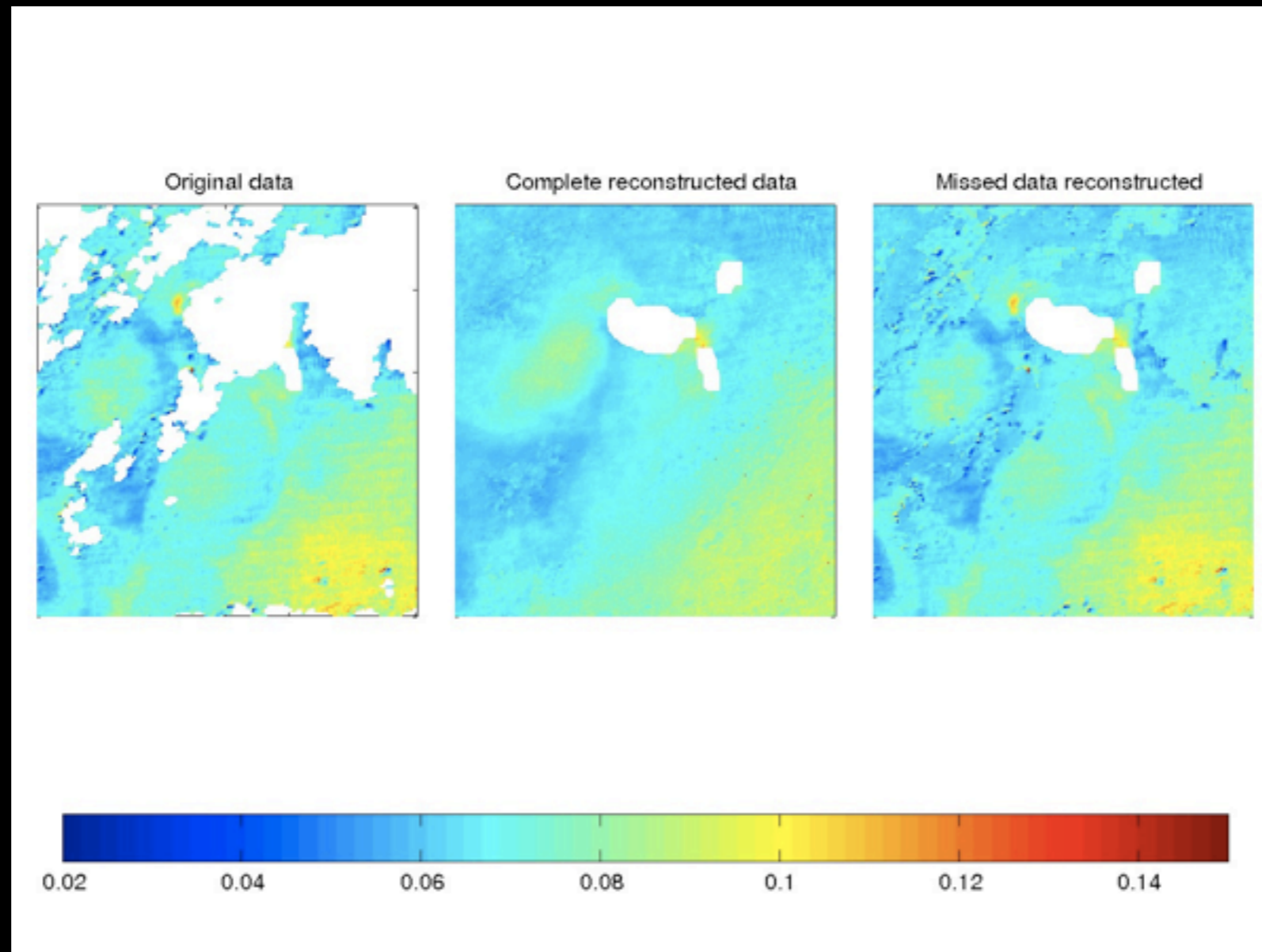
Writing time varying data  $d(\varphi, \lambda, t)$  as a matrix  $\mathcal{D} \in \mathbb{R}^{m \times n}$  where each row is associated with one point  $(\varphi, \lambda)$  and each column - with one epoch  $t$  we have linear algebra problem

$$\mathcal{D} = \mathcal{U} \mathcal{S} \mathcal{V}^T$$

# Reconstructed data

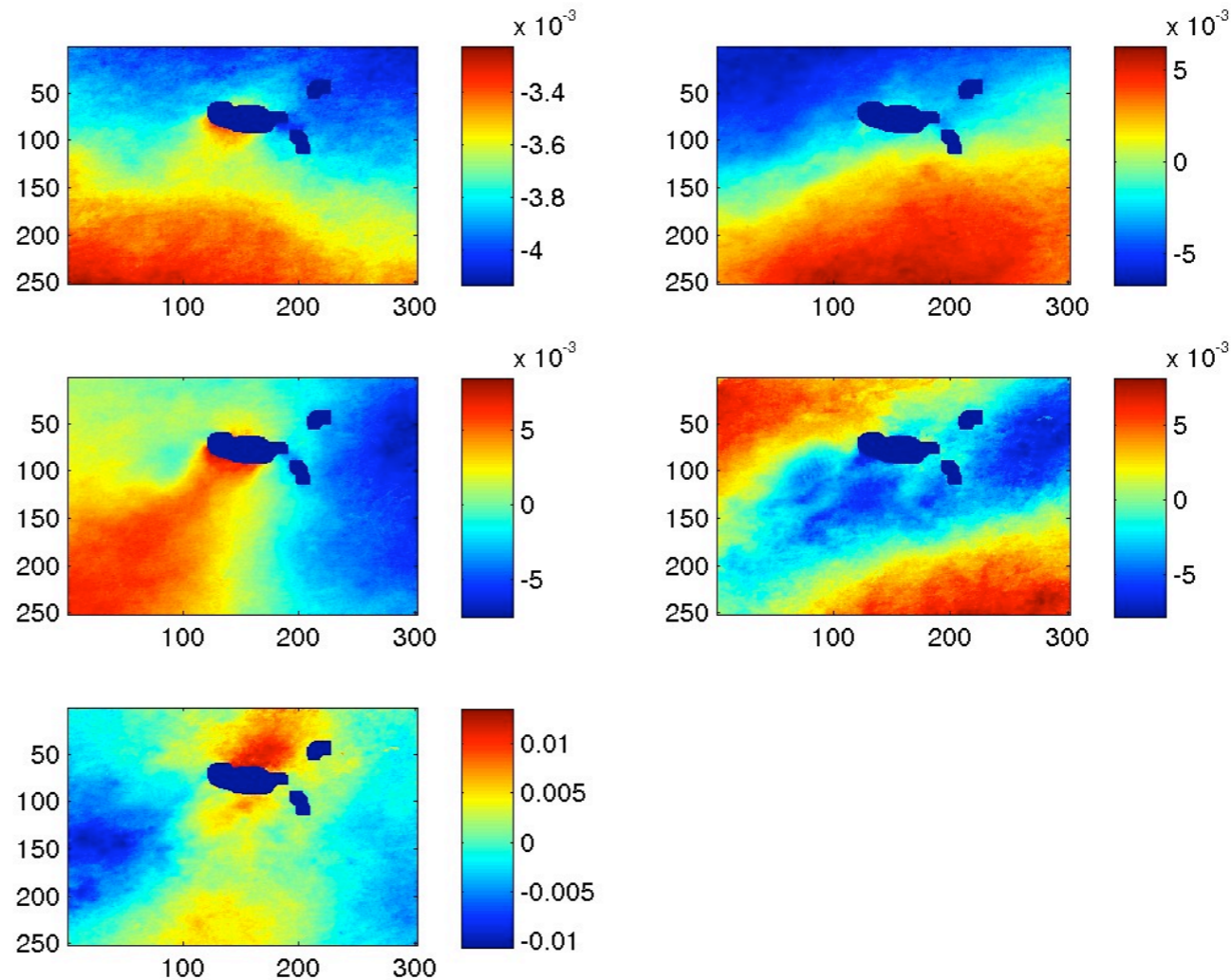


# Reconstructed data



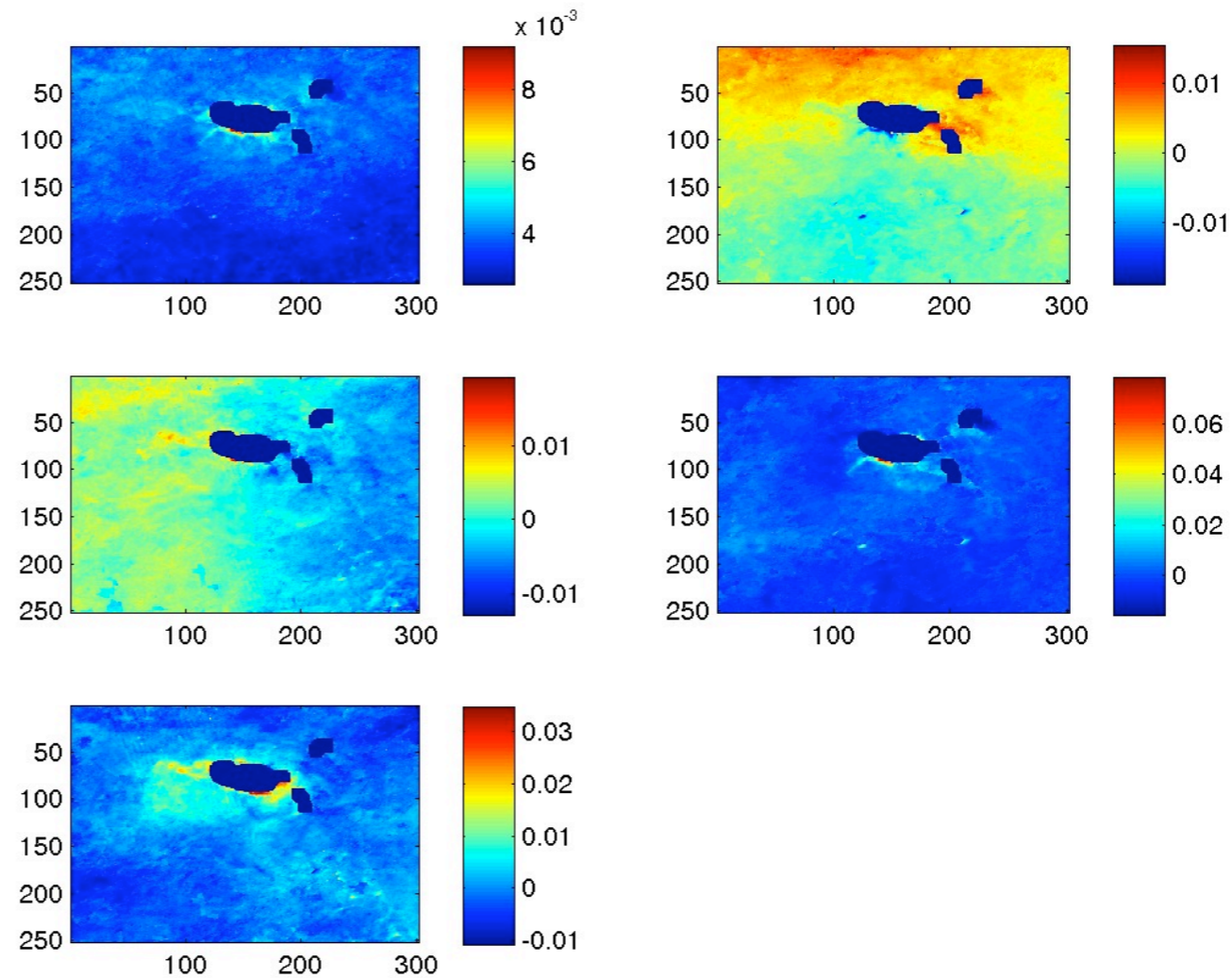
# SST Dominant modes 2005-2007

Mode 1: 60.27%  
Mode 2: 8.11%  
Mode 3: 6.51%  
Mode 4: 4.21%  
Mode 5: 3.29%



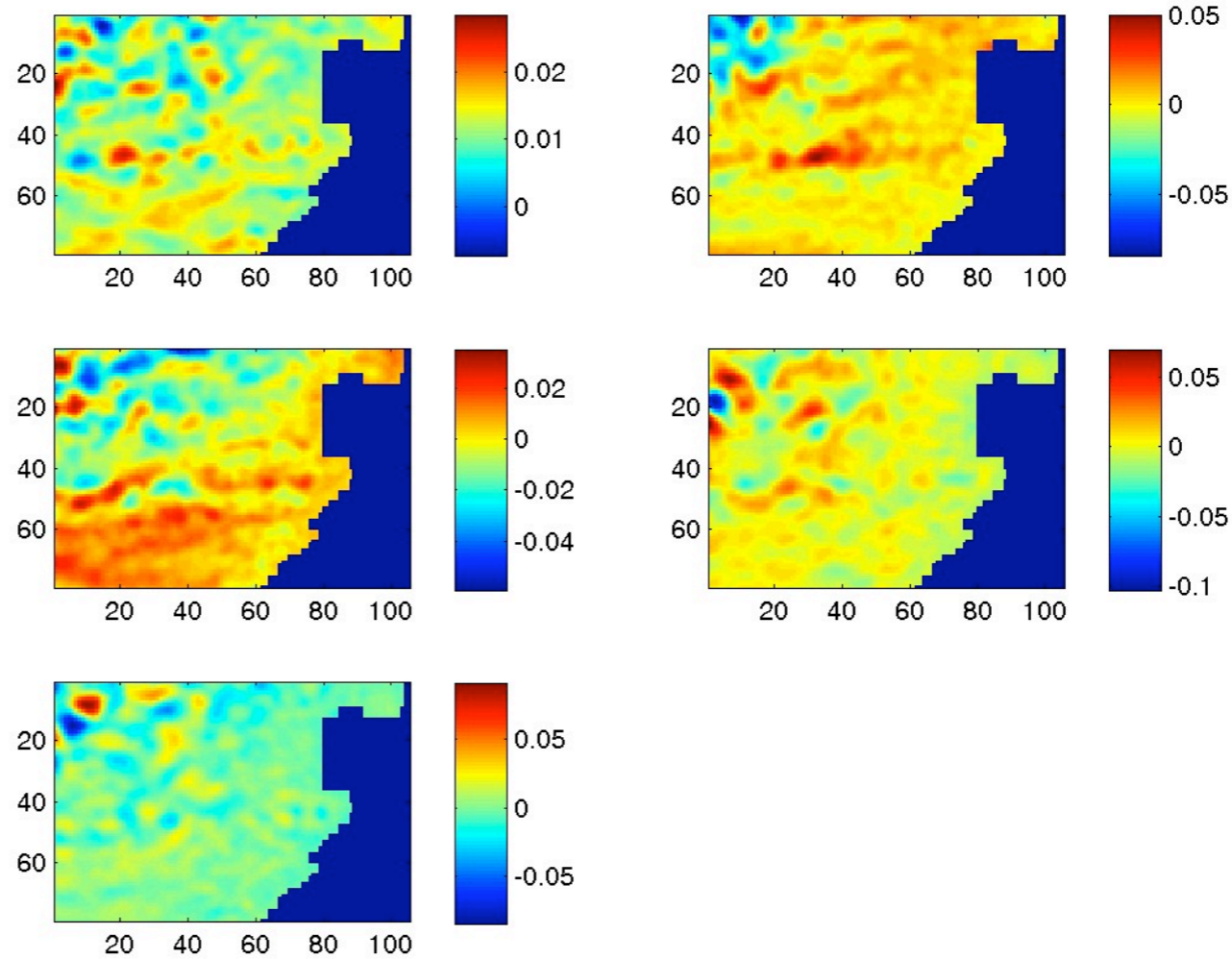
# CHL Dominant modes 2005-2007

Mode 1: 34.71%  
Mode 2: 13.02%  
Mode 3: 8.20%  
Mode 4: 6.38%  
Mode 5: 6.24%



# SLA Dominant modes 2001-2007

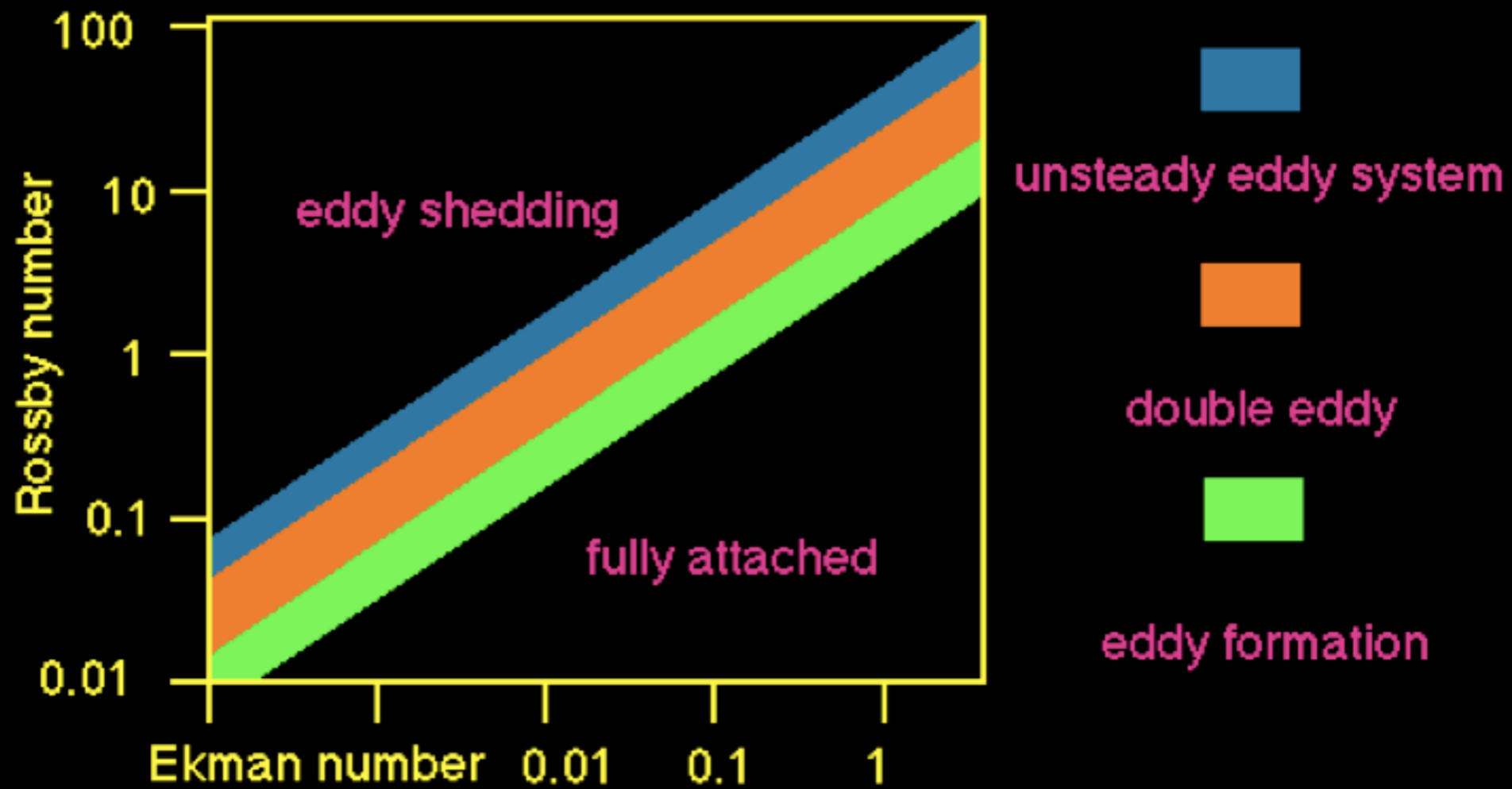
Mode 1: 16.29%  
Mode 2: 8.4%  
Mode 3: 6.6%  
Mode 4: 5.66%  
Mode 5: 5.27%





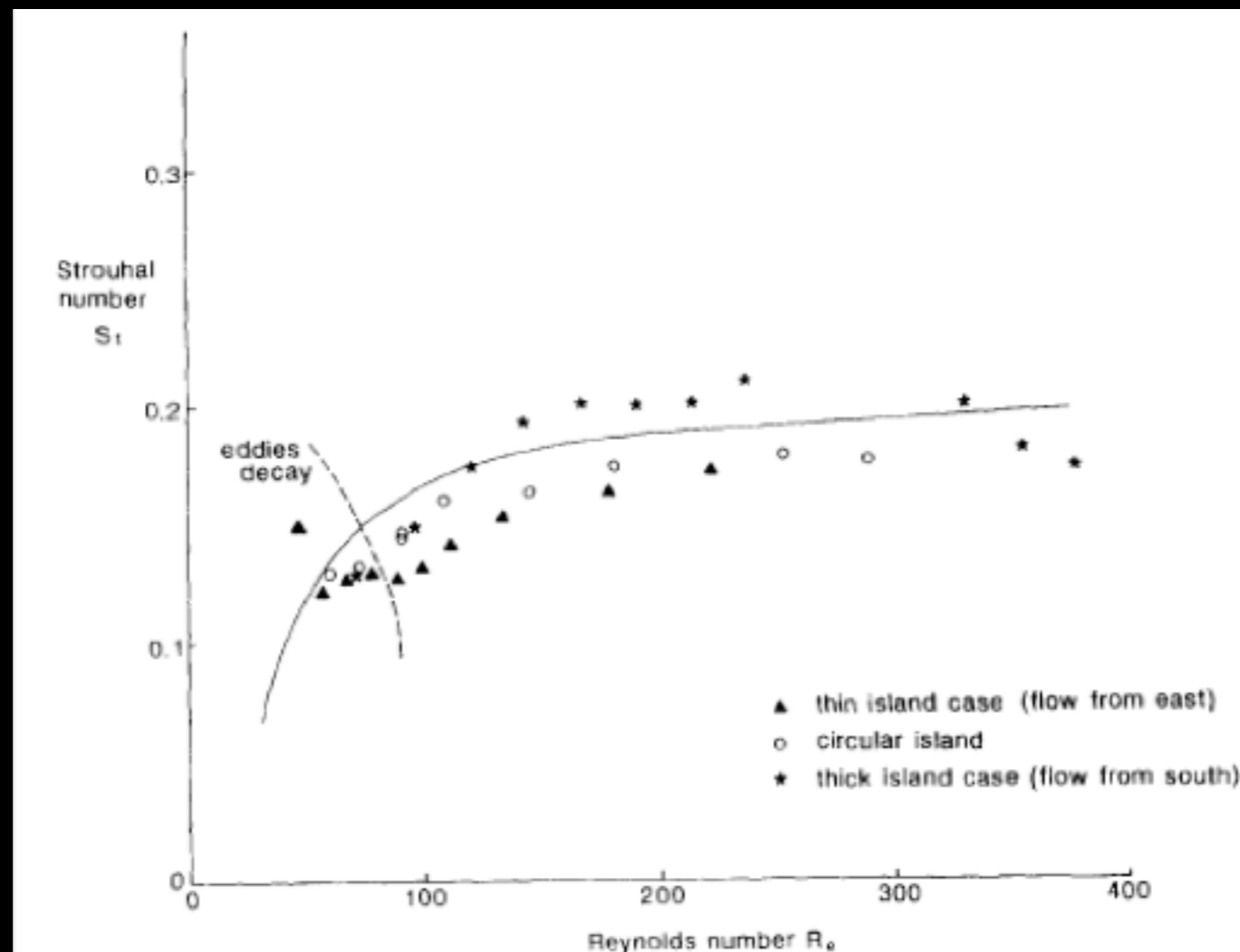
# Wake regimes

Non-dimensional parameters



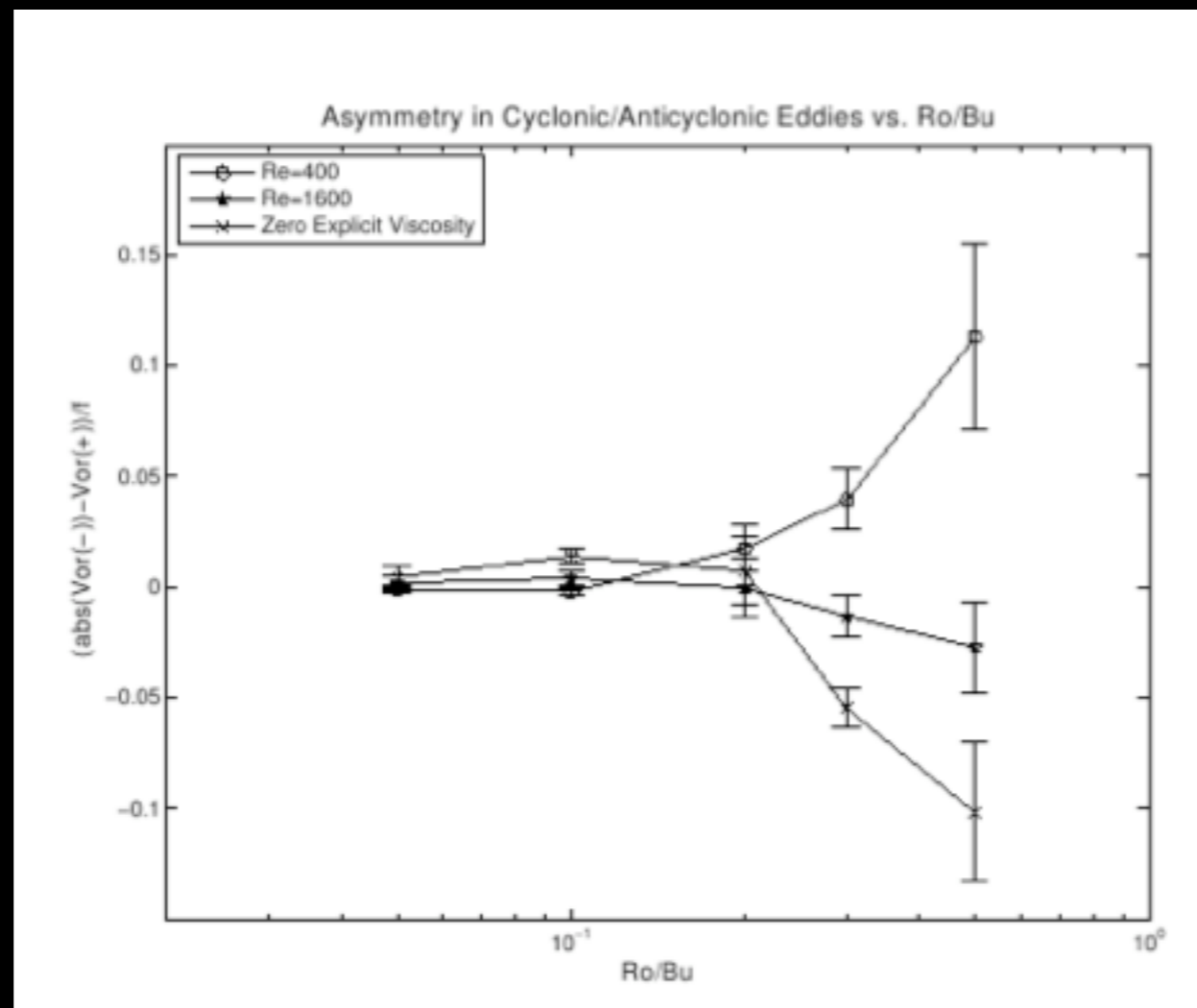
# Wake regimes

## Non-dimensional parameters



# Wake regimes

## Non-dimensional parameters



# Non-dimensional

$$Re = \frac{UL}{\nu_e}, \quad \text{Reynolds number}$$

$$Ro = \frac{U}{Lf}, \quad \text{Rossby number}$$

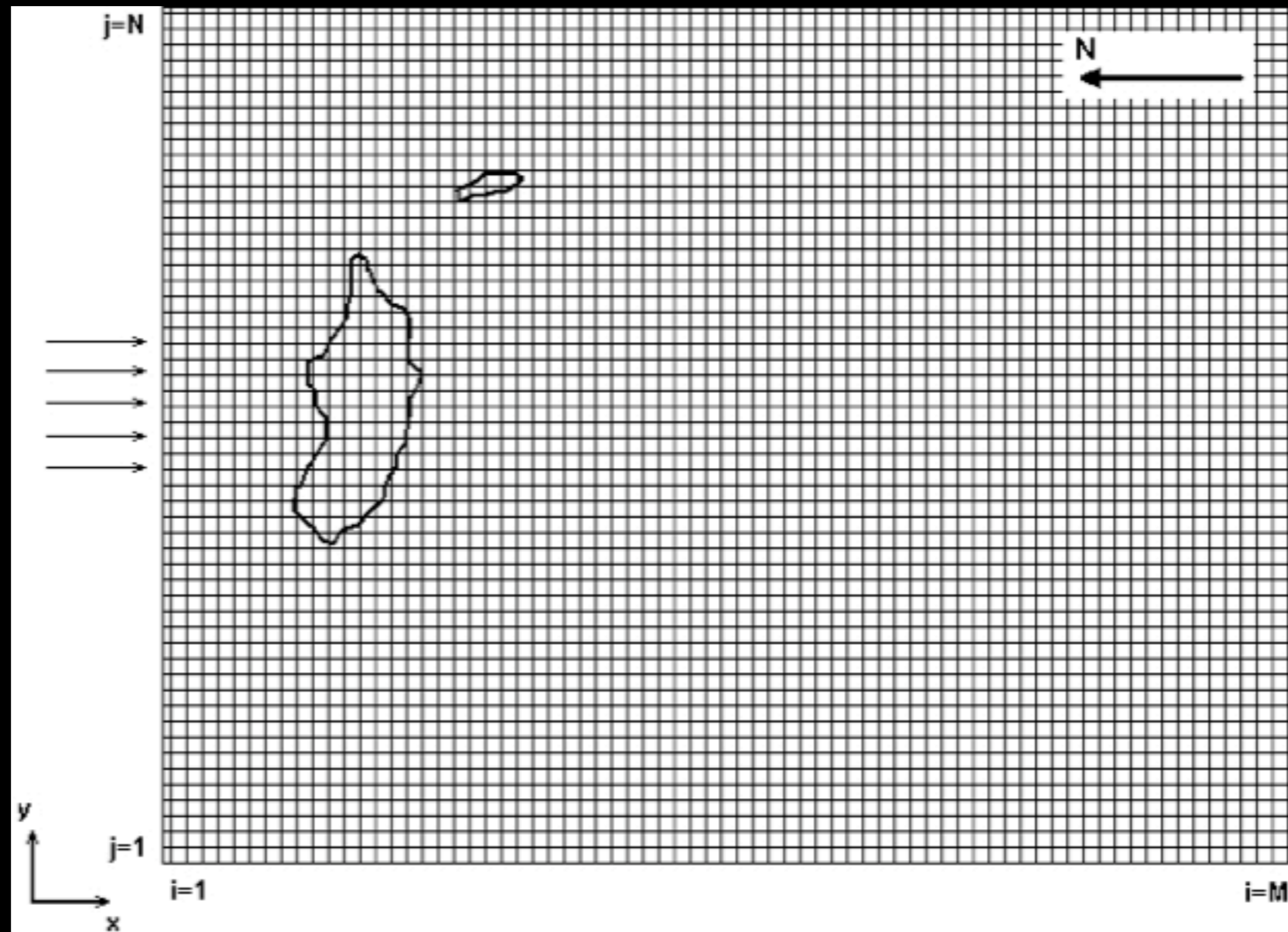
$$Fr = \frac{U}{NH}, \quad \text{Froude number}$$

$$E_k = \frac{\nu_e}{fL^2}, \quad \text{Ekman number (horizontal)}$$

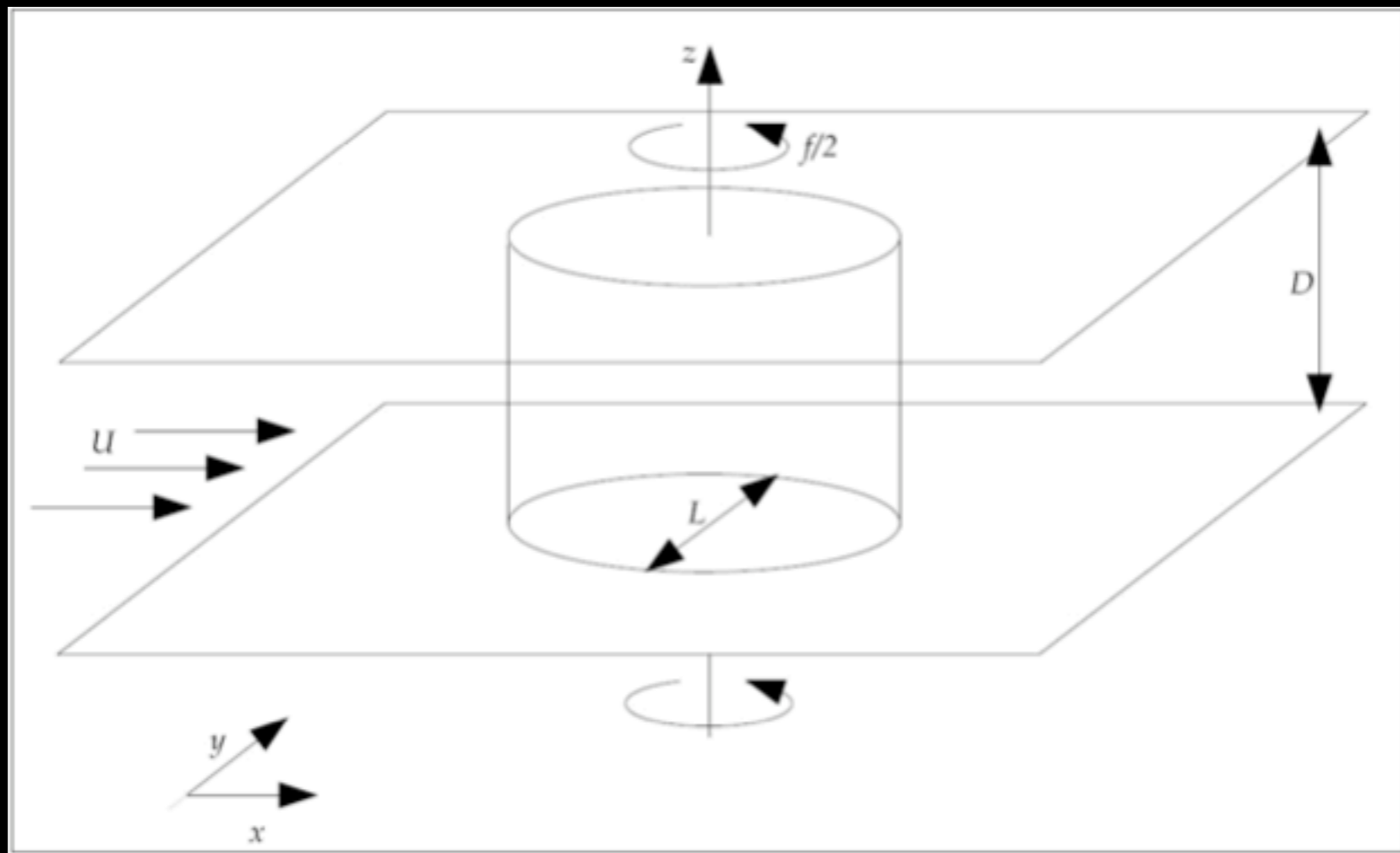
$$L_d = NH/f, \quad \text{Baroclinic deformation radius}$$

$$Bu = \left(\frac{L_d}{L}\right)^2, \quad \text{Burger number}$$

# 2D numerical study



# 2D numerical study



# 2D numerical setup

- Quasi-geostrophic approximation

$$\frac{\partial \zeta'_0}{\partial t'} + J(p'_0, \zeta'_0) = \frac{1}{Re} \nabla^2 \zeta'_0$$

- Initial conditions

$$\zeta'_0 = \nabla^2 p'_0$$

$$x' = 0, \text{ inflow} \rightarrow \begin{cases} \zeta'_0 = 0 \\ u' = -\frac{\partial p'_0}{\partial y'} = \text{cte} \end{cases}$$

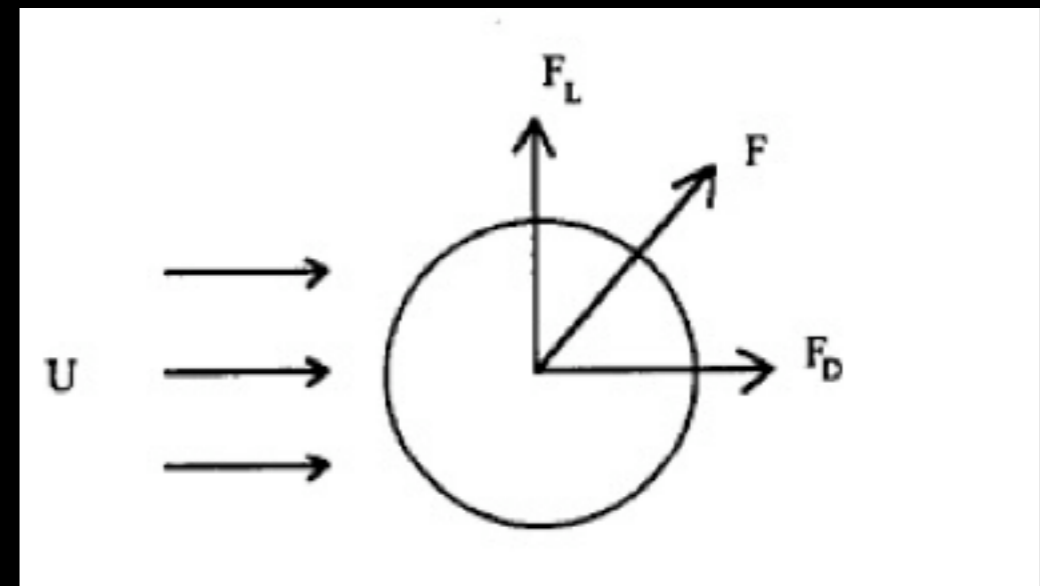
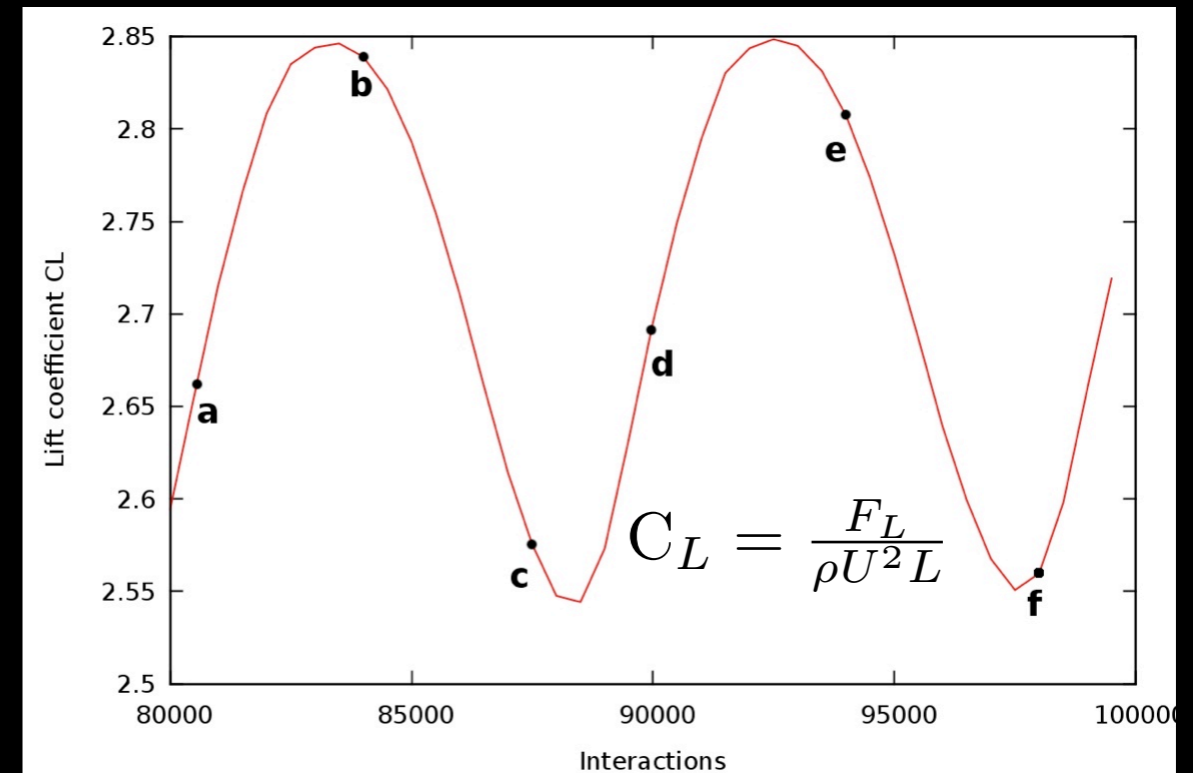
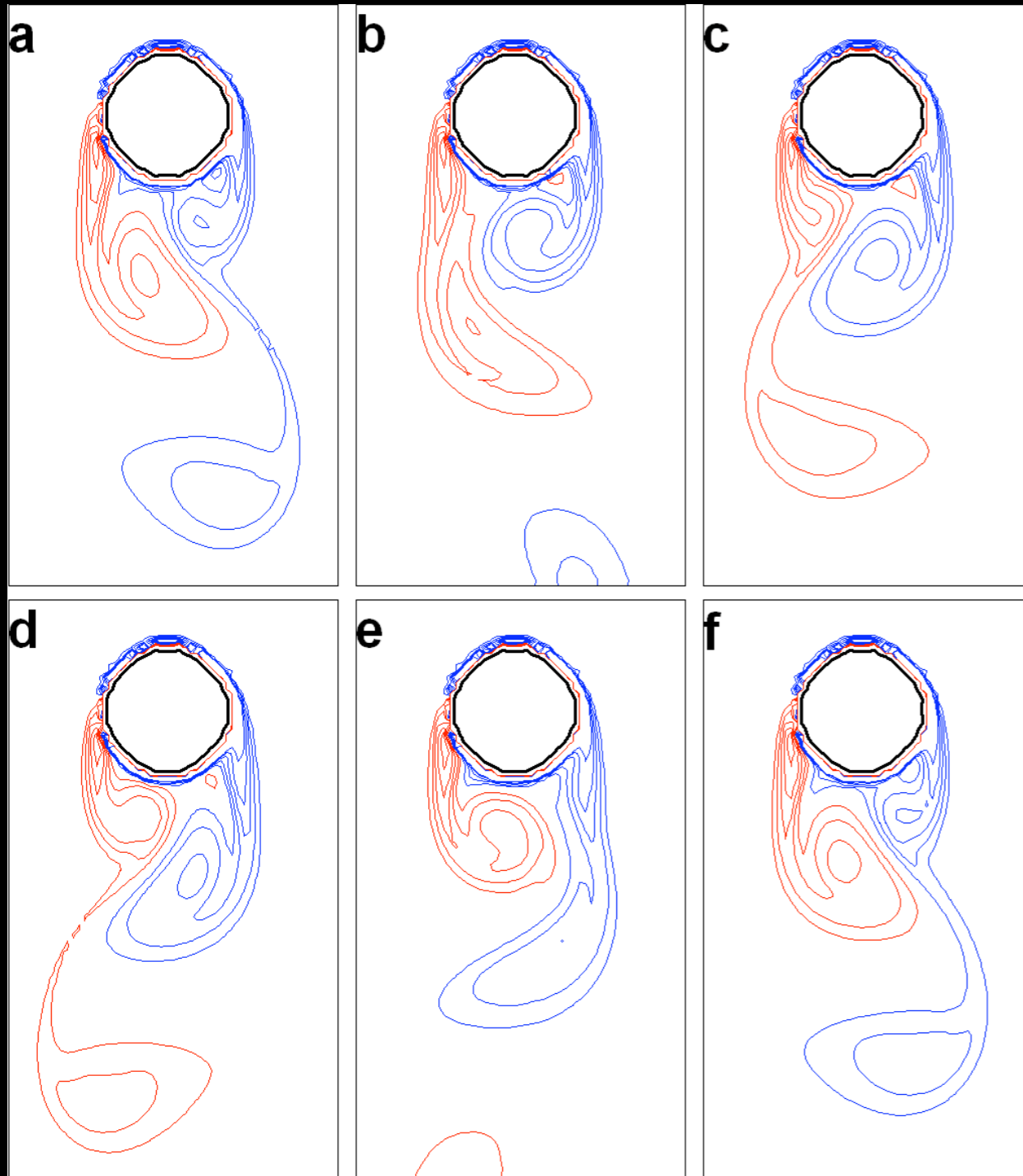
- Boundary conditions

$$\text{obstacle} \rightarrow \begin{cases} \zeta'_{\text{obs}} = 0 \\ u'_{\text{obs}} = -\frac{\partial p'_0}{\partial s} = 0 \rightarrow p'_0 = \text{cte} \end{cases}$$

$$y' = 0, y' = n \nabla y', \text{ walls} \rightarrow \begin{cases} \zeta'_0 = 0 \\ p'_0 = p'_{\text{inflow}} \end{cases}$$

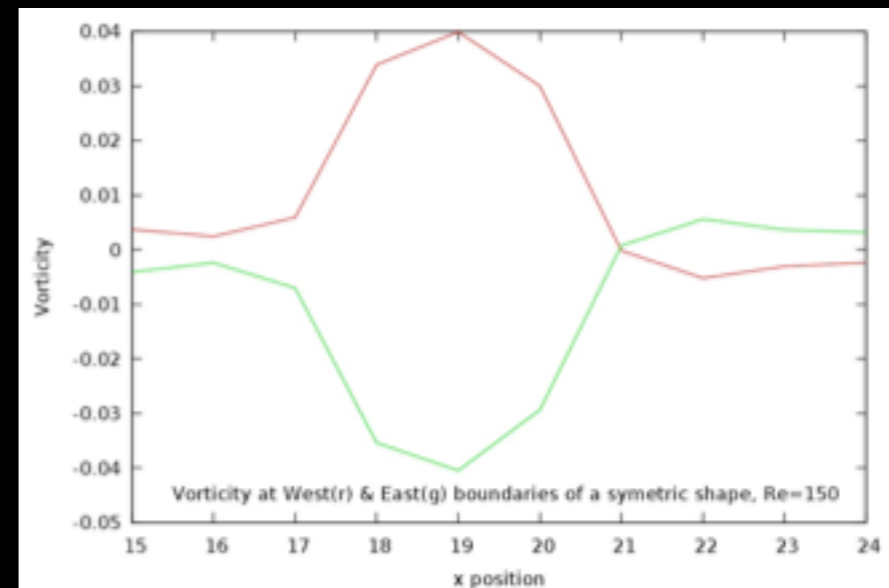
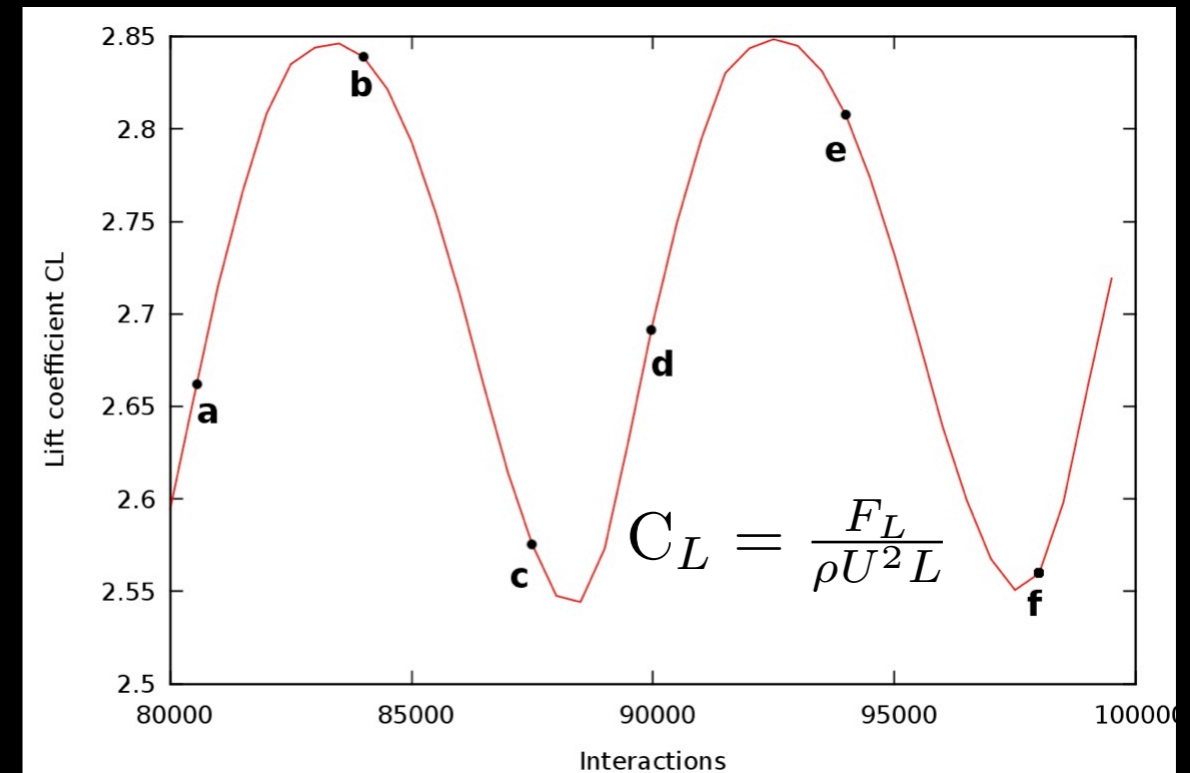
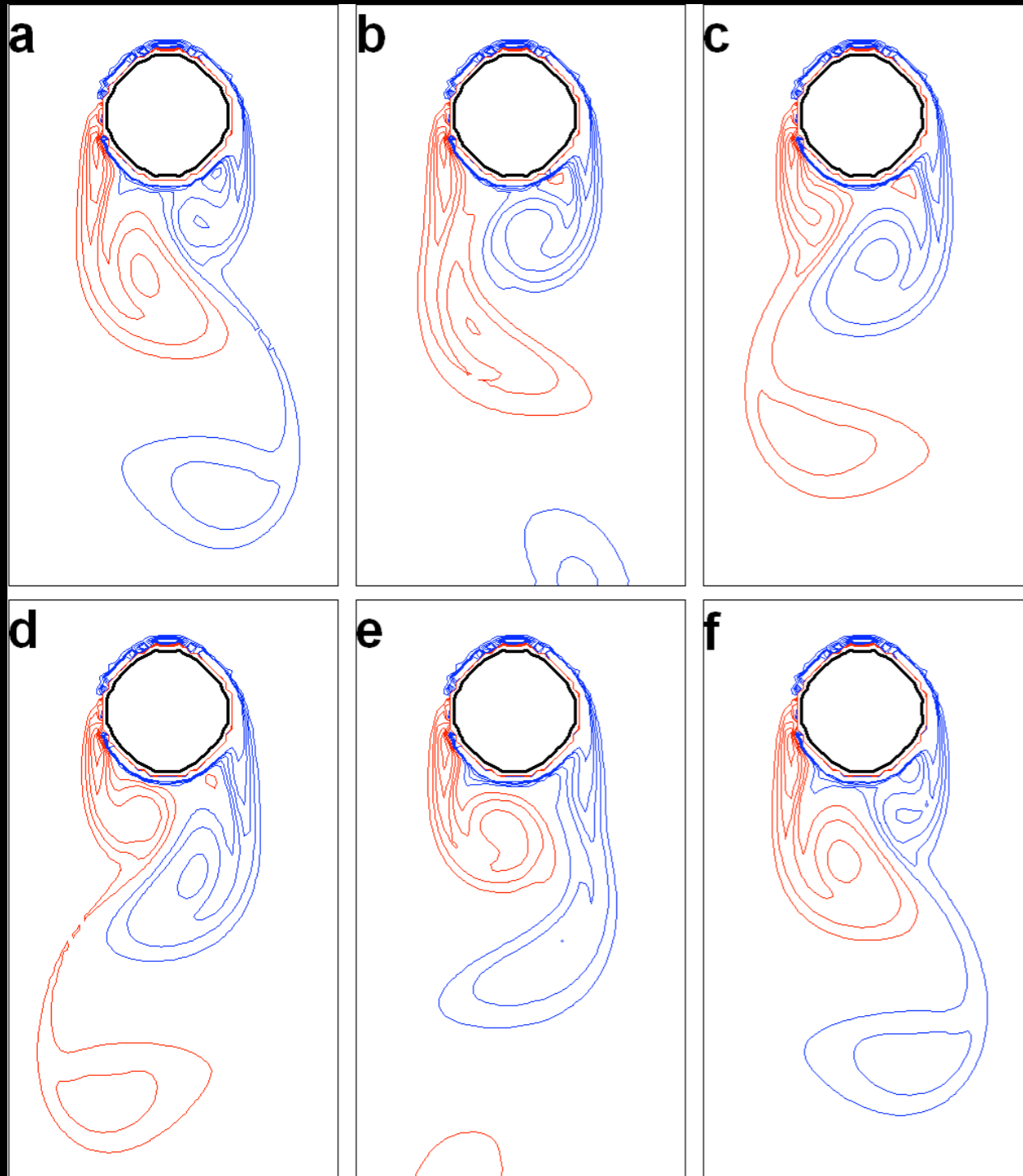
$$x' = m \nabla x', \text{ outflow} \rightarrow \text{Orlansky}$$

# 2D Symmetric case (Classical case)

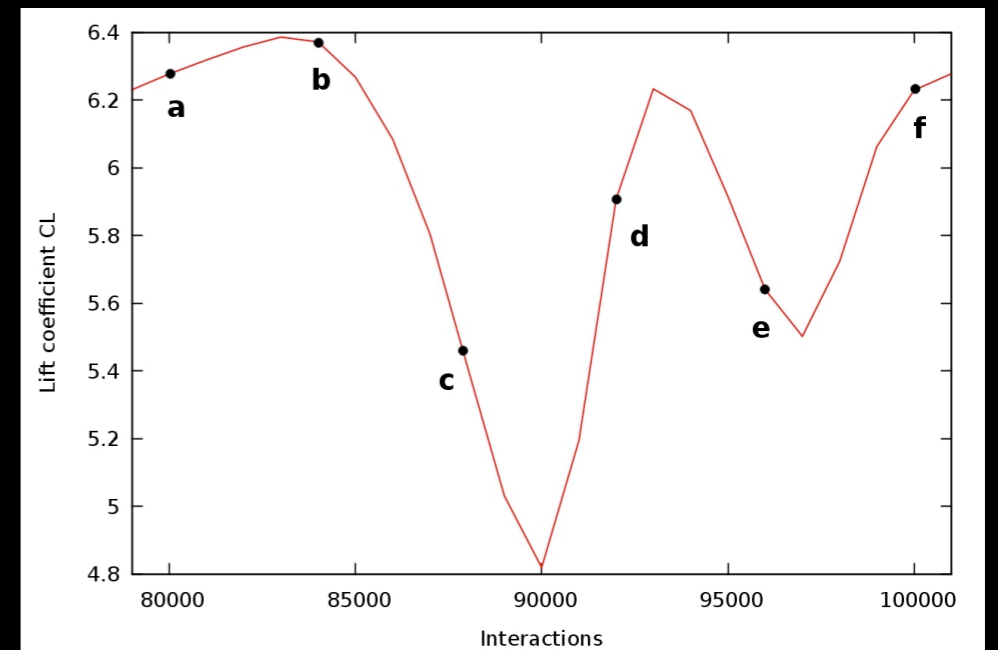
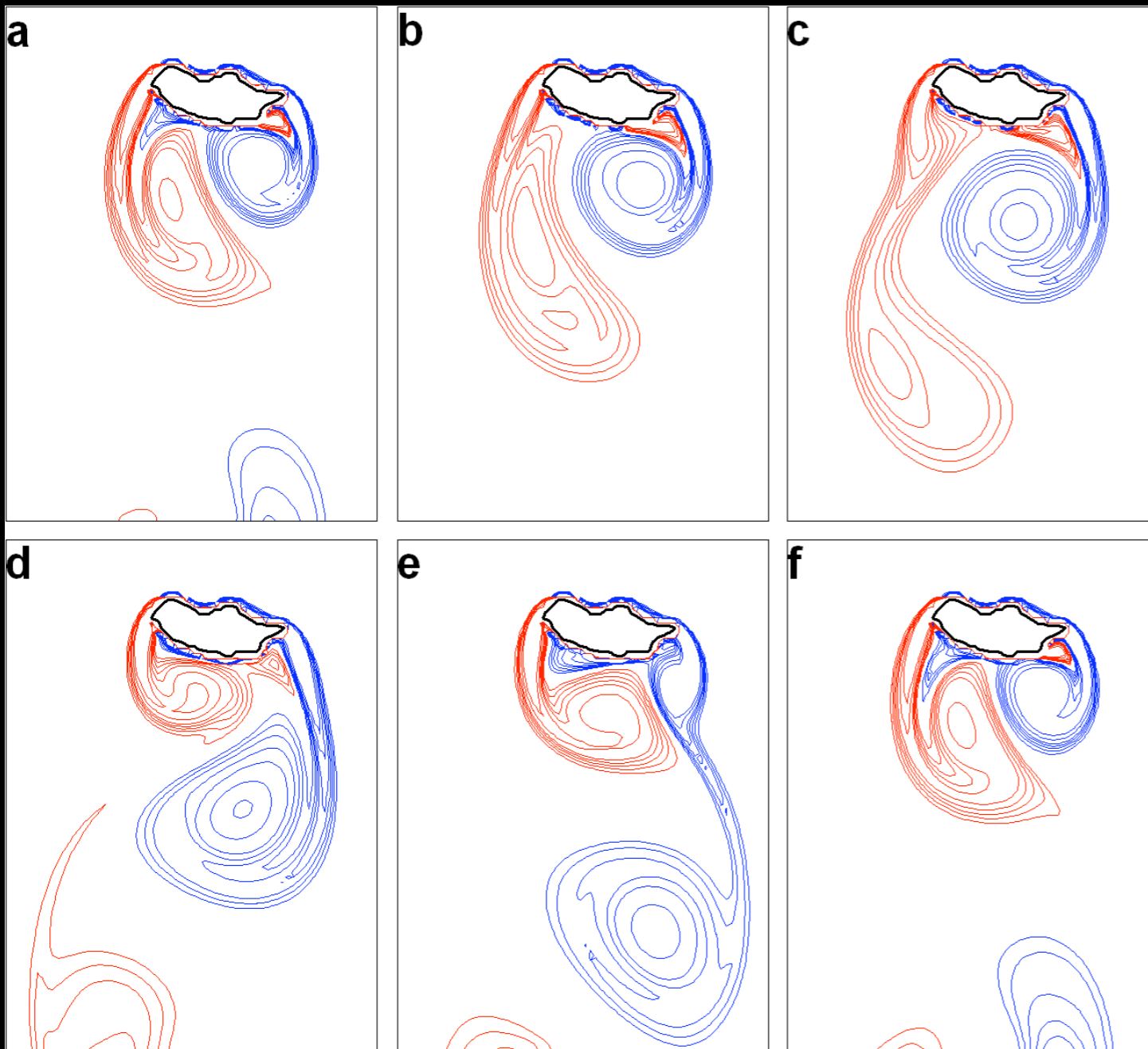




# 2D Symmetric case (Classical case)

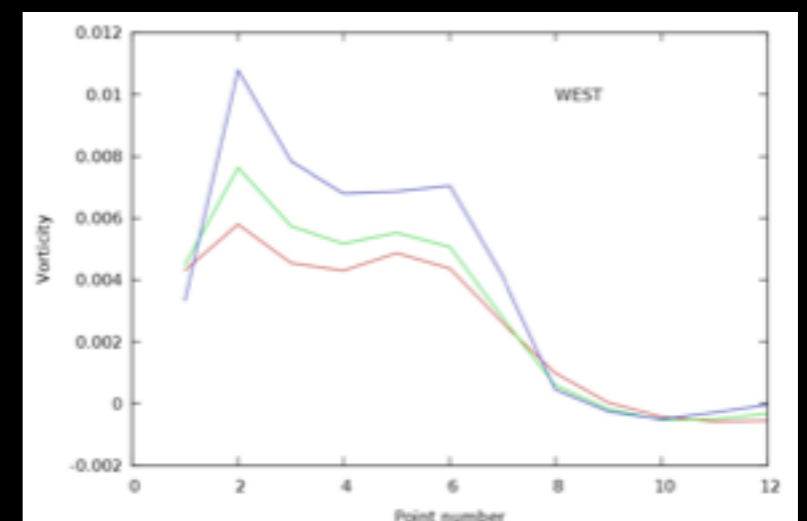
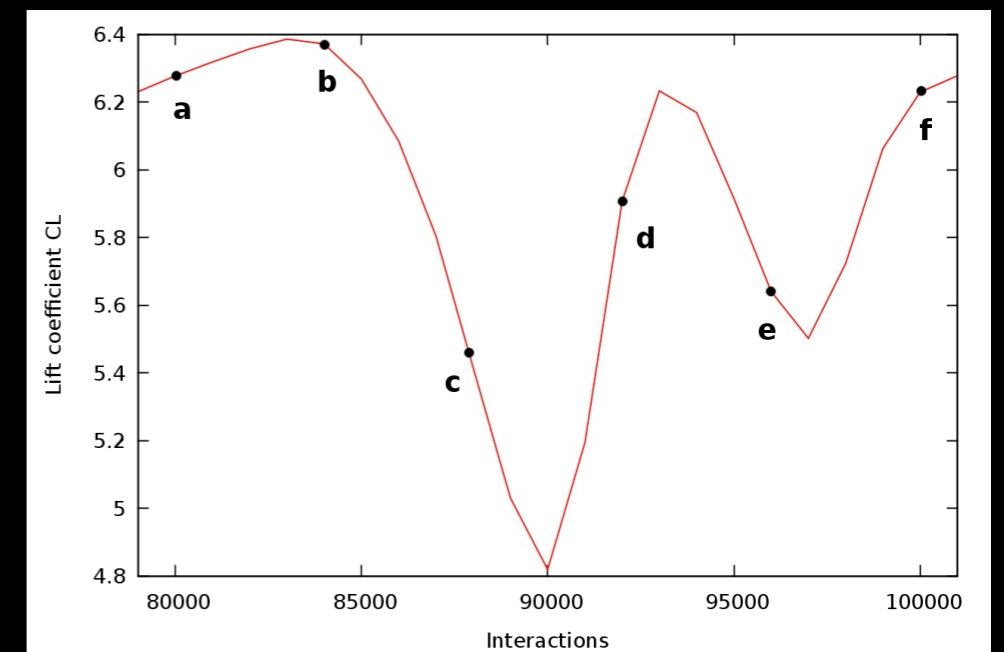
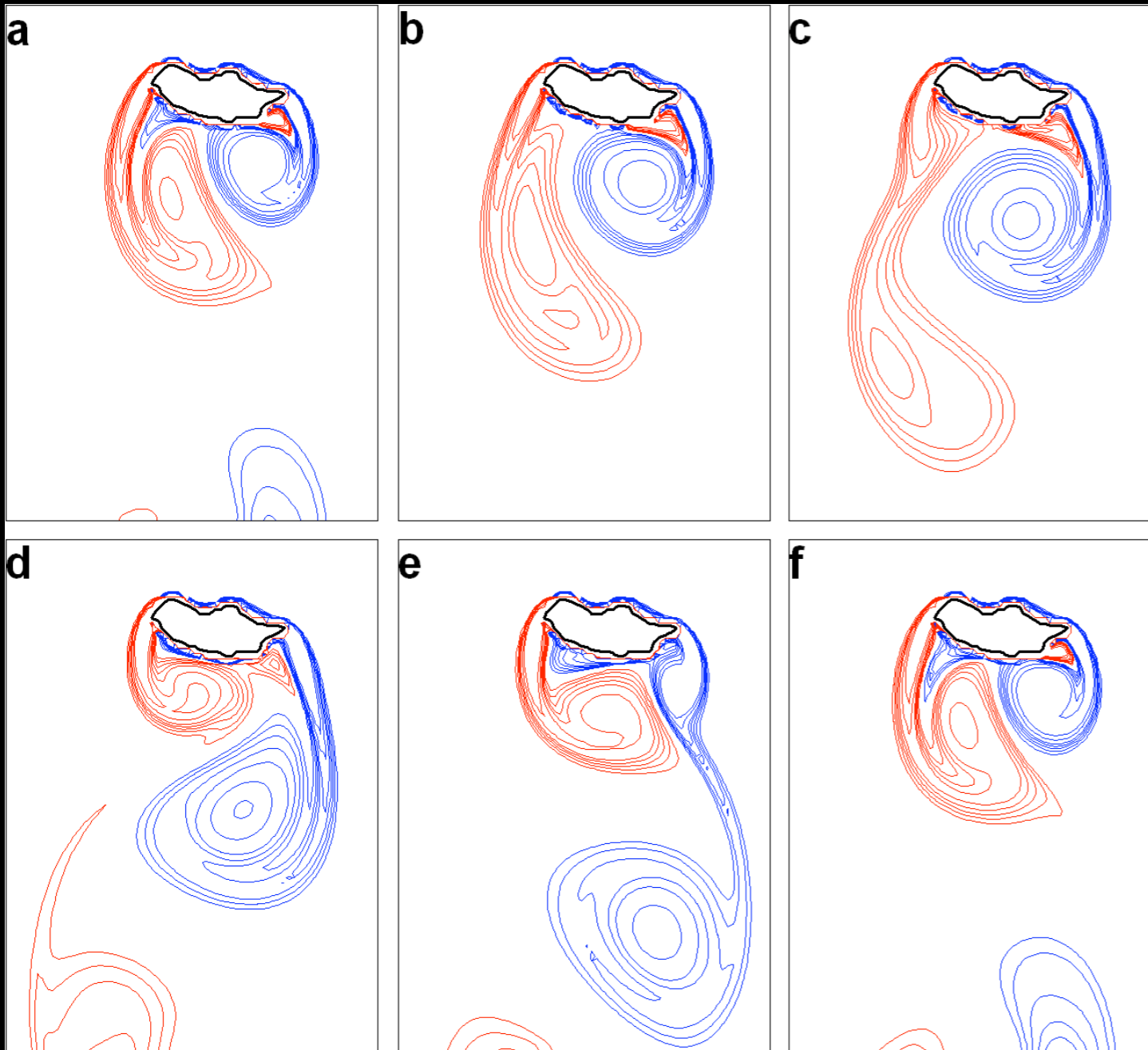


# 2D Assymmetric case

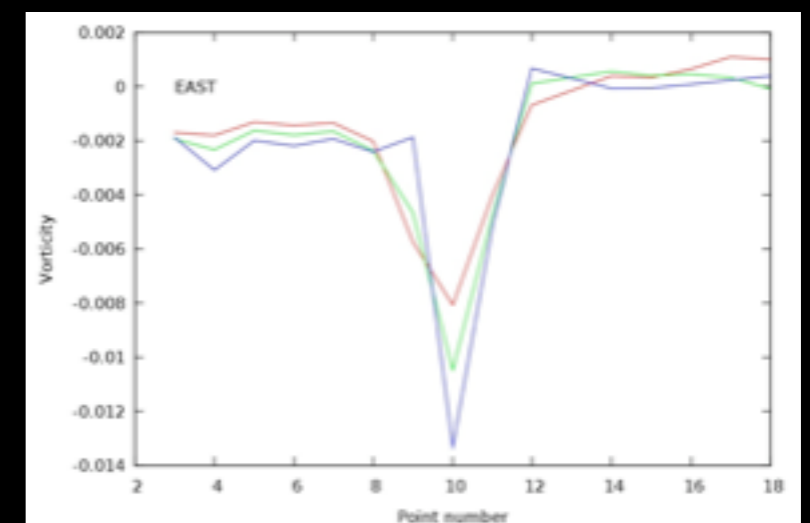
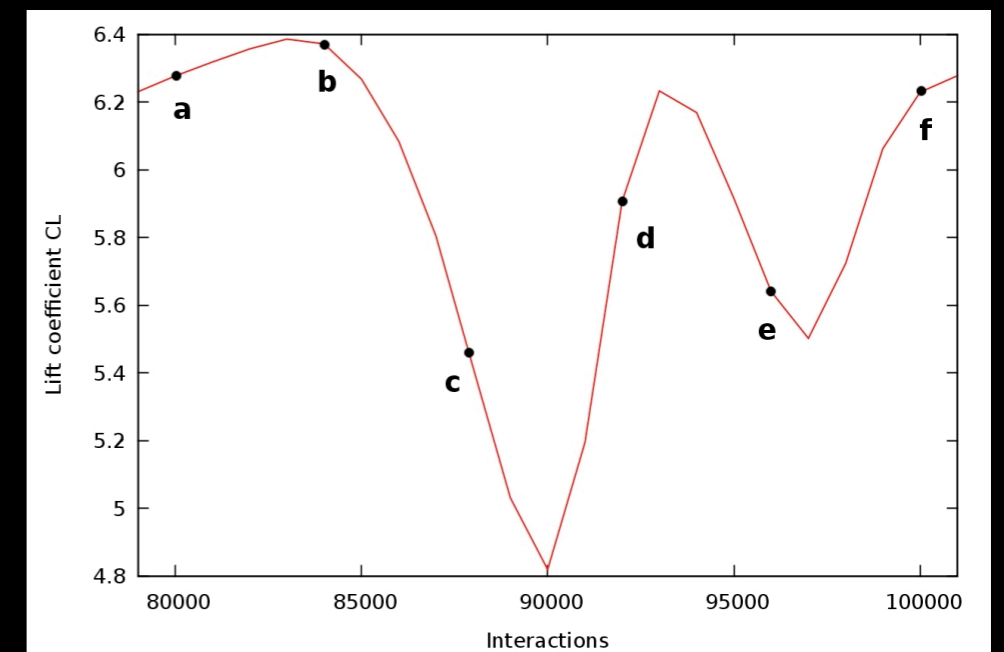
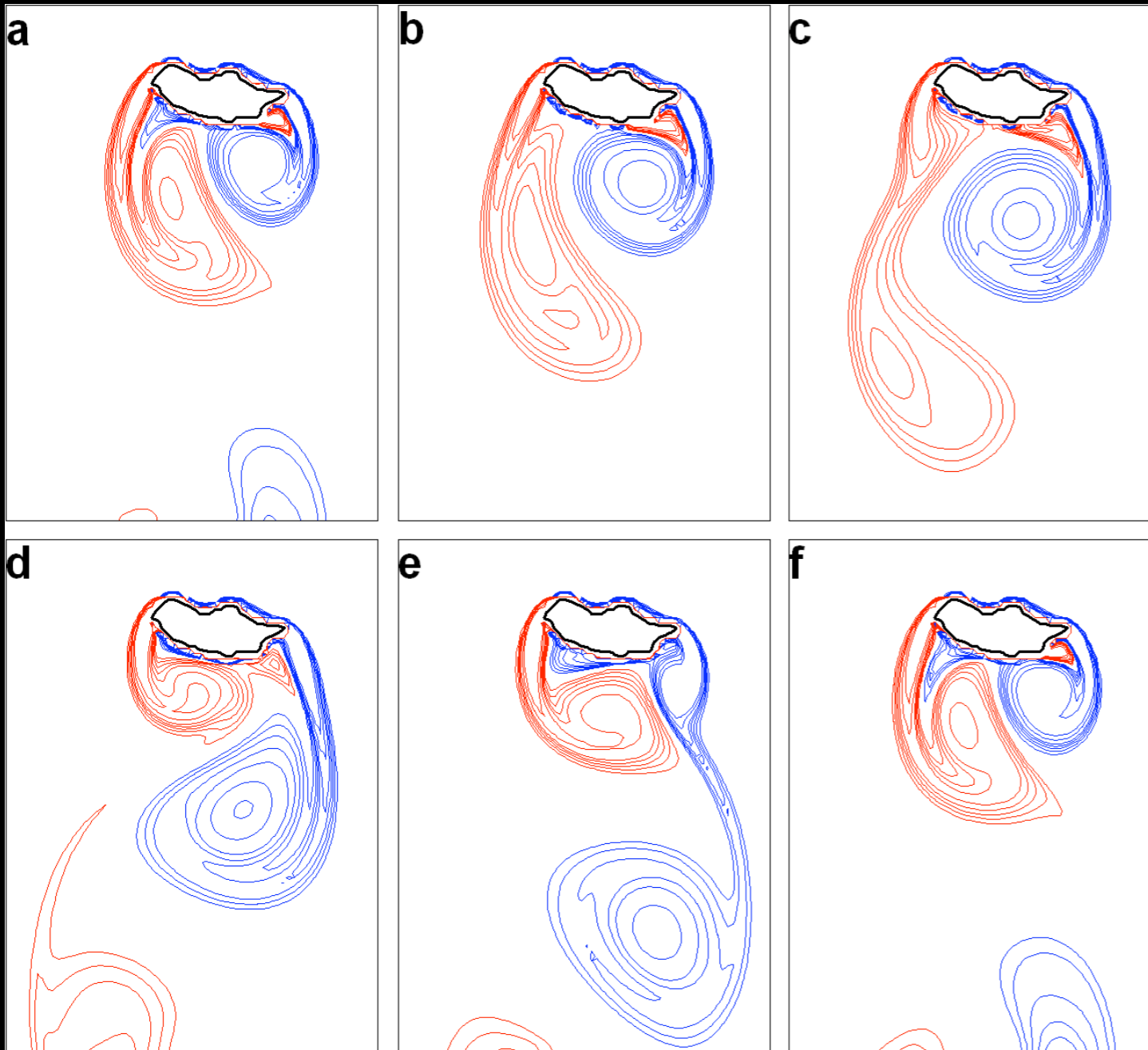


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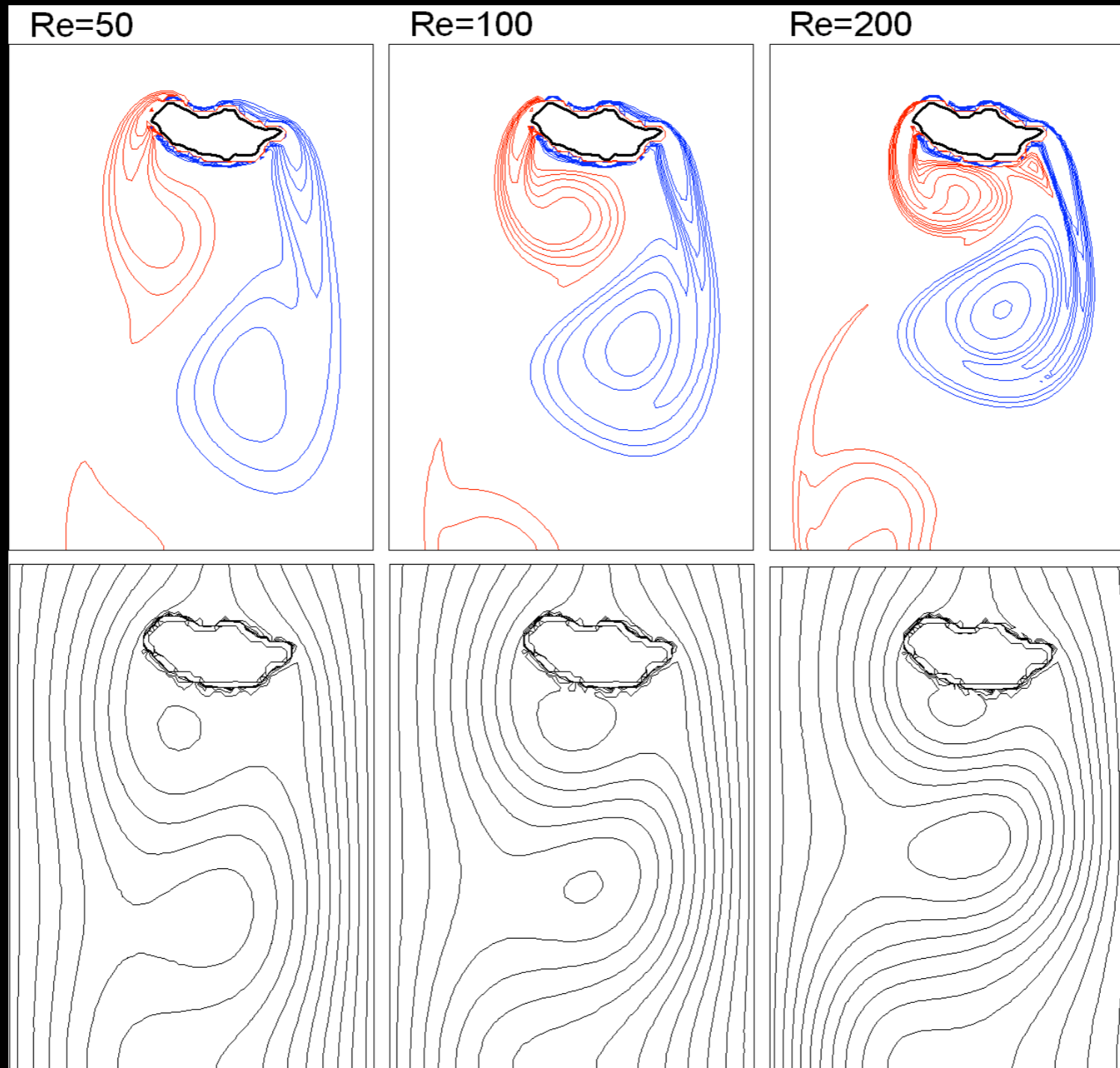
# 2D Assymmetric case



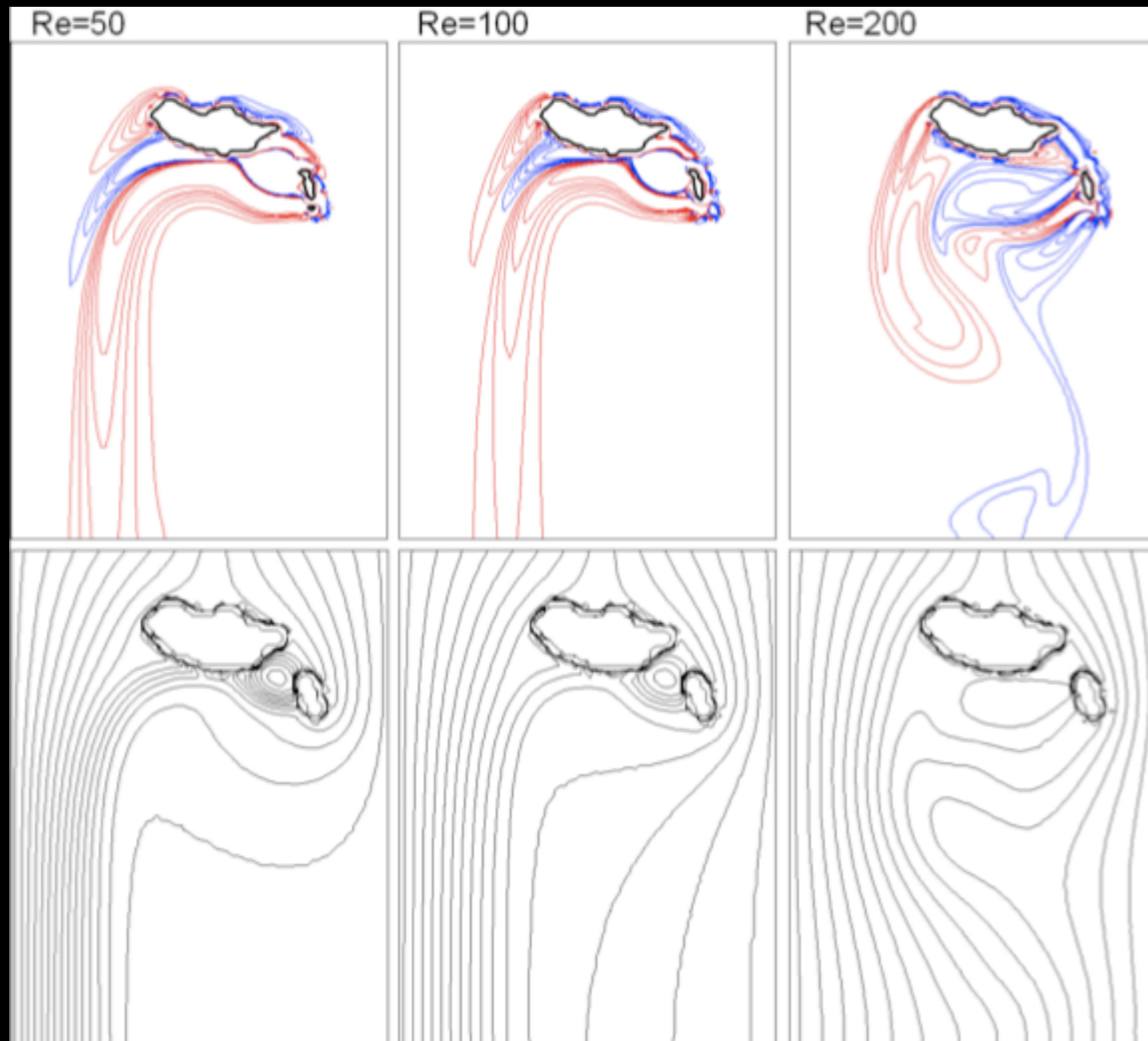
# 2D Assymmetric case



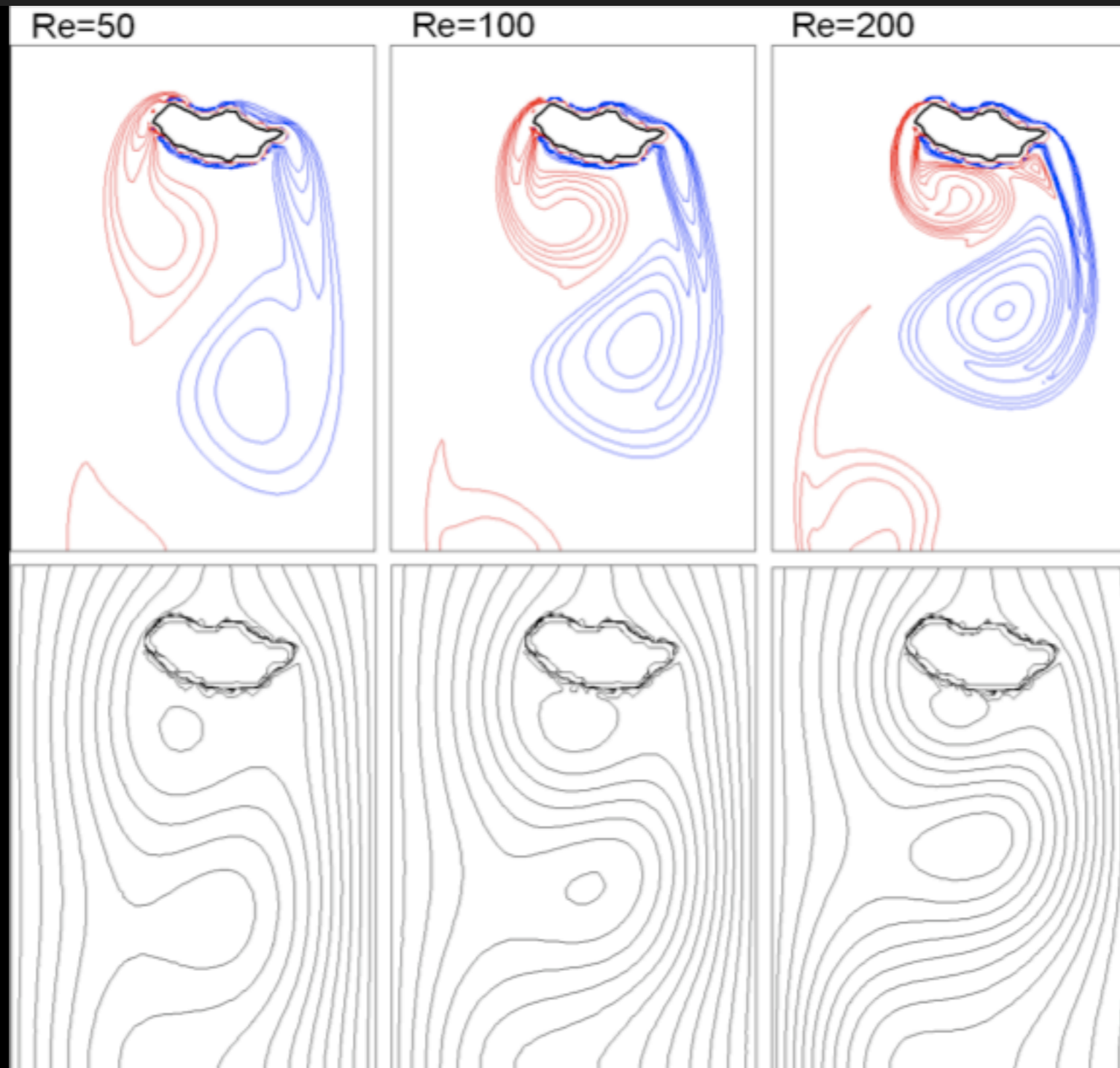
# Re study



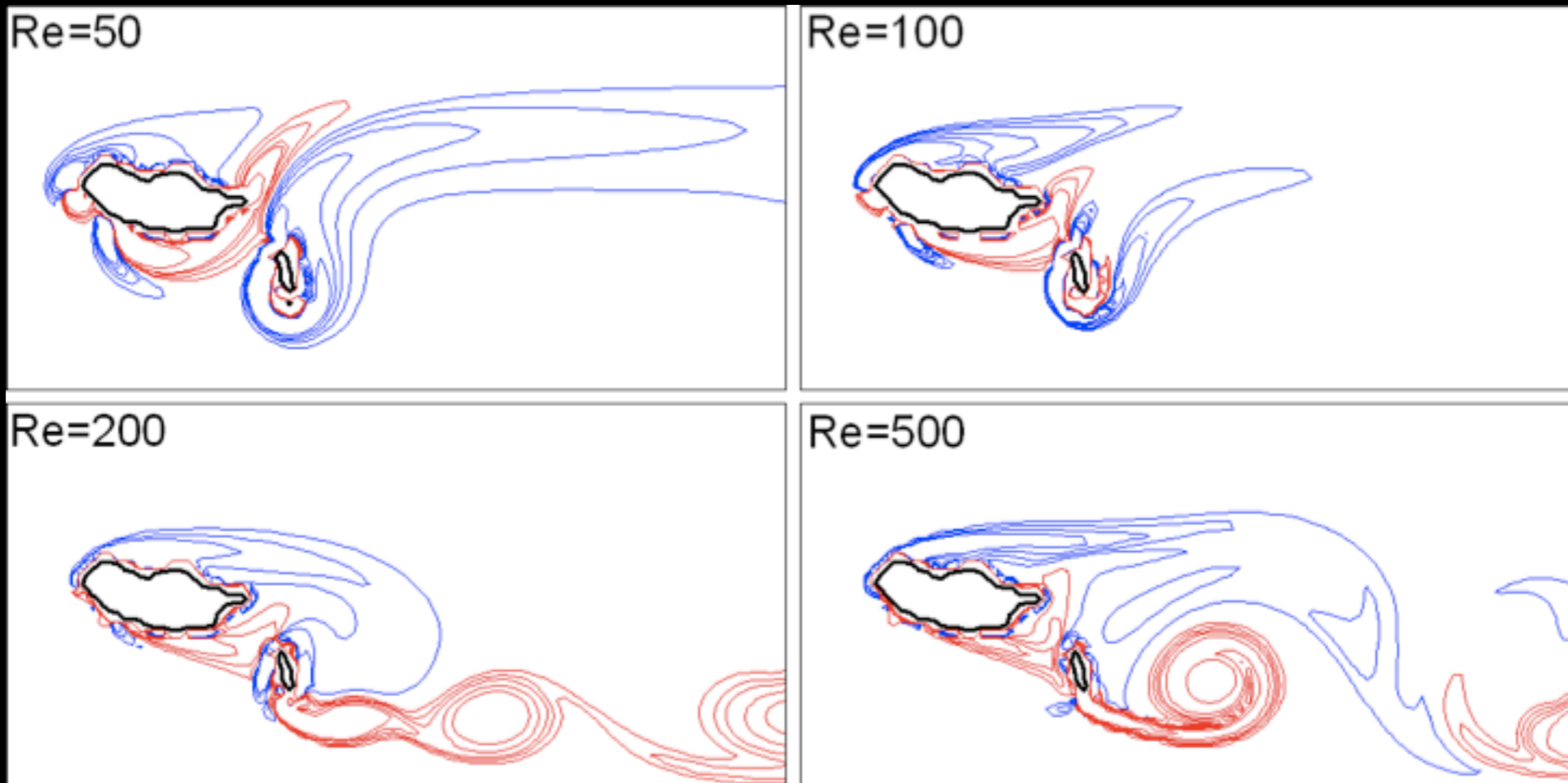
# Nearby island effect



# Nearby island effect

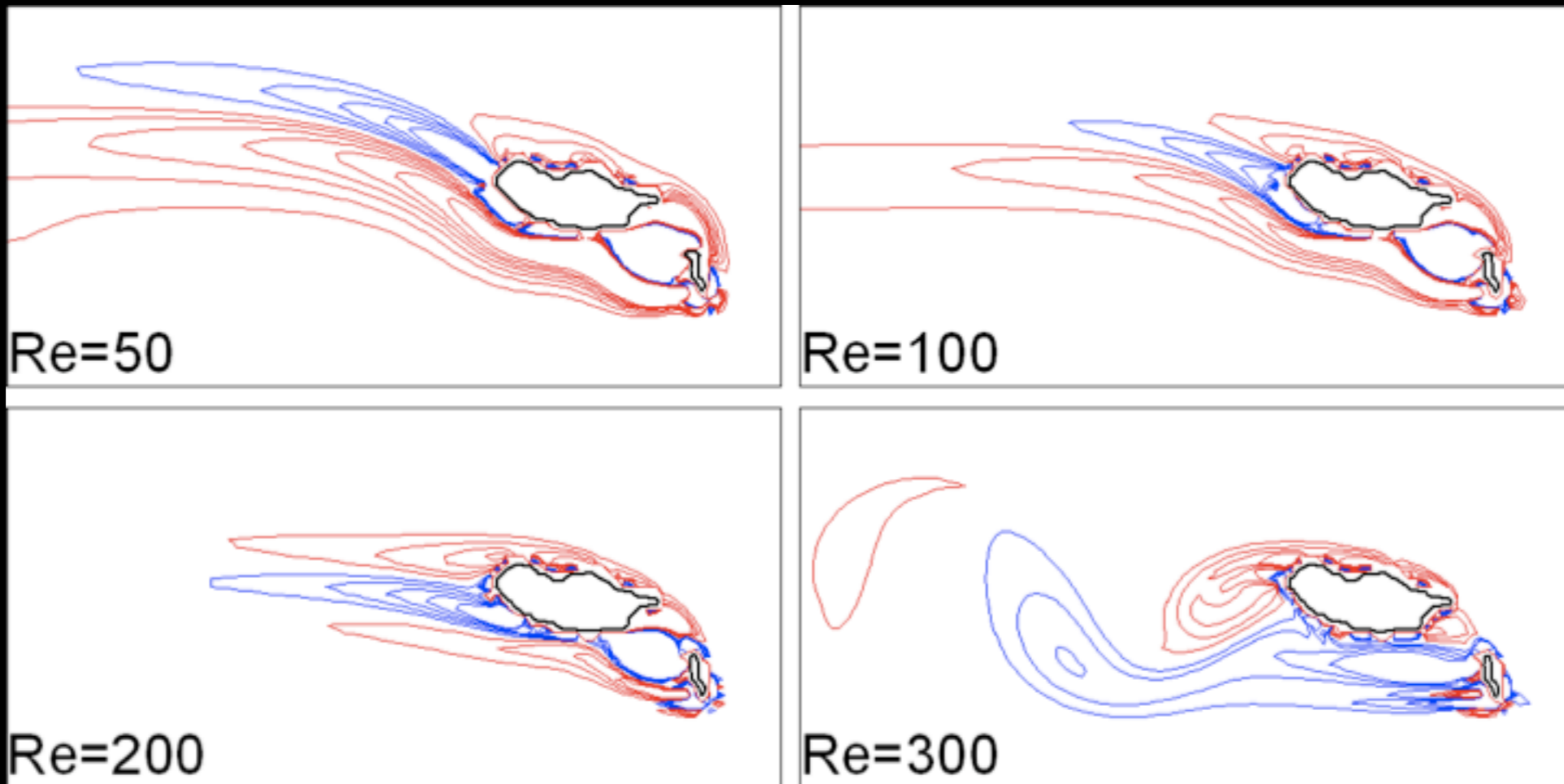


# Flow direction

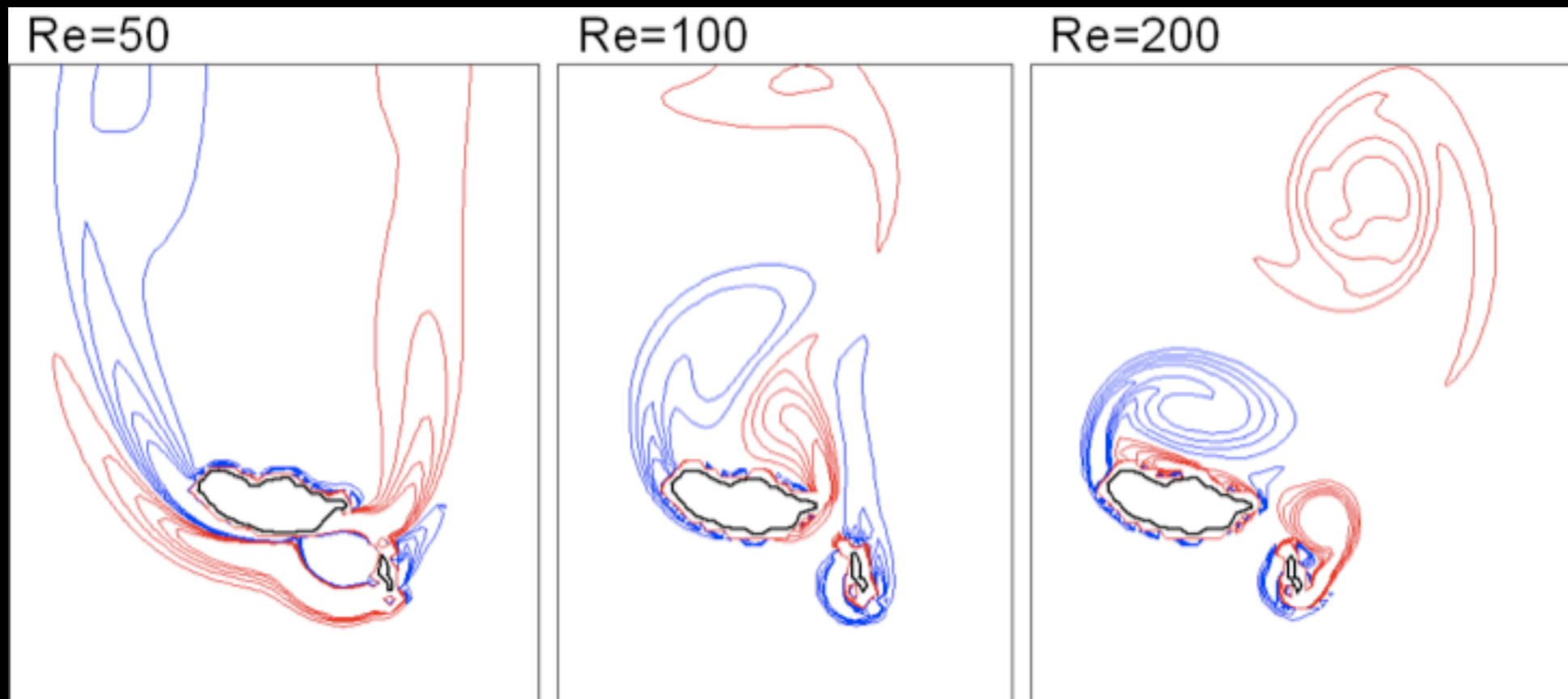




# Flow direction



# Flow direction



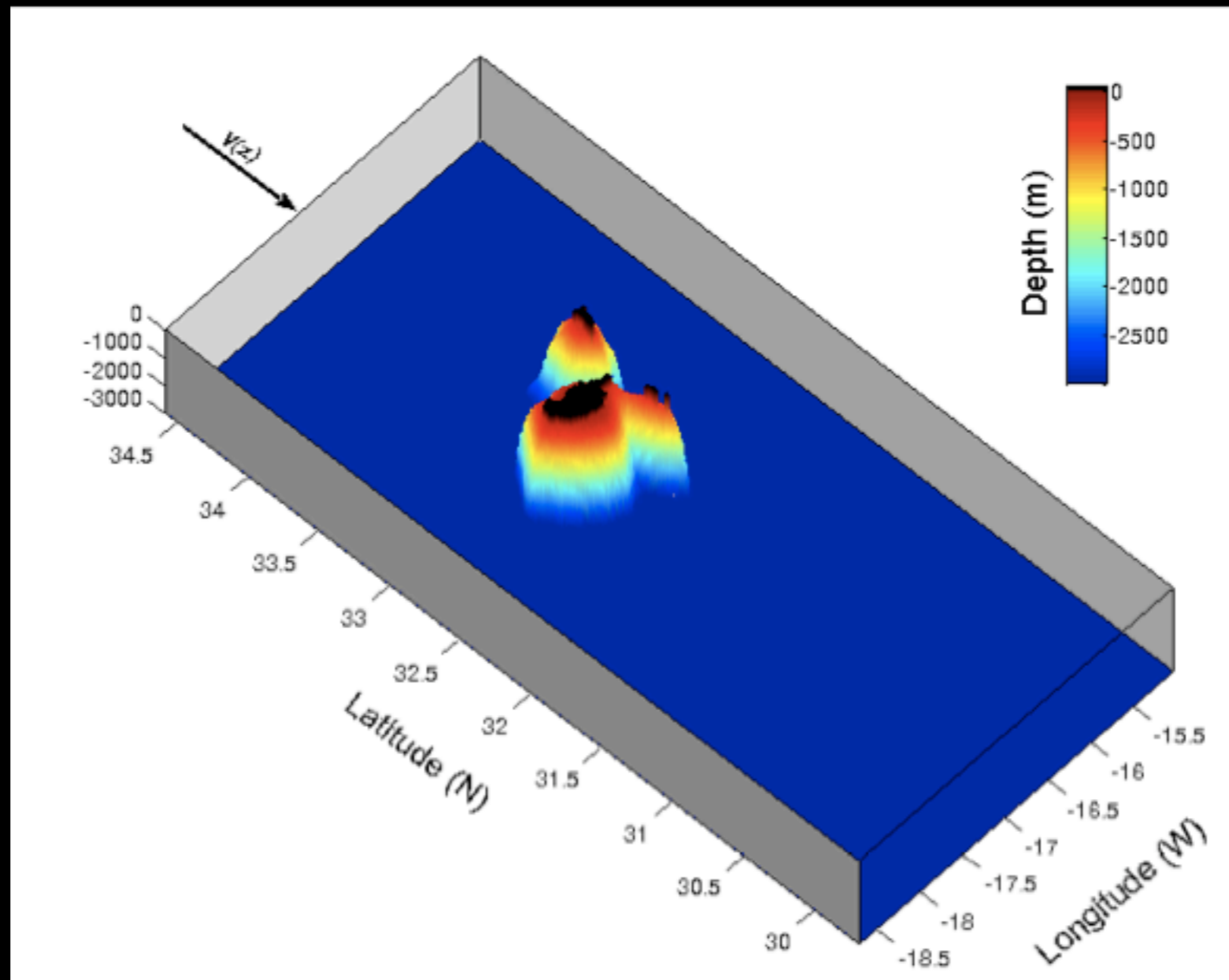
# 2D Case studies

## Summary

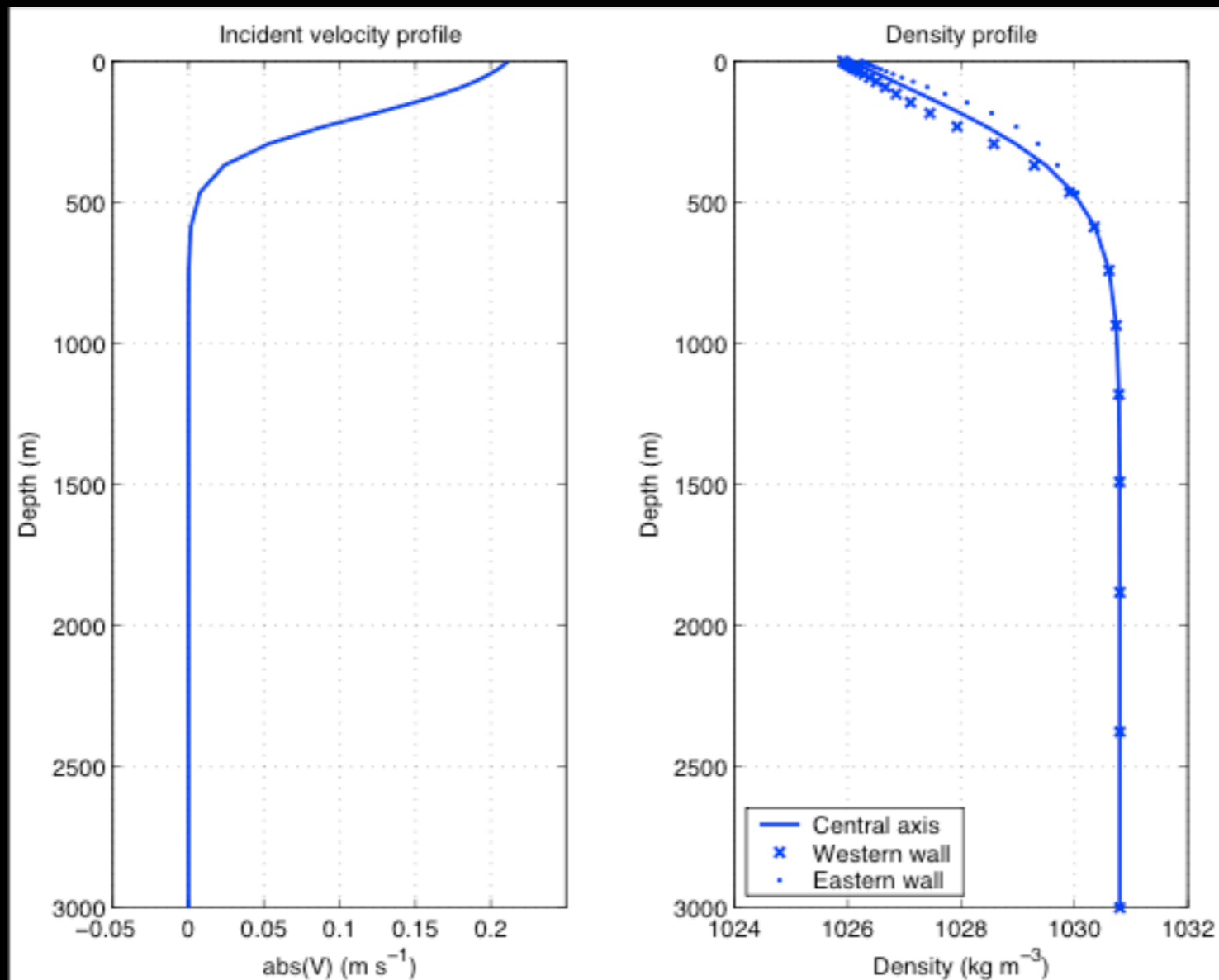
Case ( <i>islands – inflow</i> )	Re	U ( $m.s^{-1}$ )	$\varepsilon$	Eddy shedding period $T_r$
Madeira-North	50	0.088	0.02	30 days
	100	0.175	0.05	15 days
	200	0.351	0.09	7.5 days
Madeira+Desertas-North	50	0.088	0.02	no shedding; steady state at 60 days
	100	0.175	0.05	no shedding; steady state at 30.5 days
	200	0.351	0.09	6.3 days
Madeira-West	50	0.227	0.15	no shedding; steady state at 10 days
	100	0.455	0.3	no shedding; steady state at 4.6 days
	200	0.909	0.61	19 hours
	500	2.273	1.52	5.5 hours
Madeira+Desertas-West	50	0.227	0.15	no shedding; steady state at 8 days
	100	0.455	0.3	no shedding; steady state at 3.5 days
	200	0.909	0.61	8.3 hours
	500	2.273	1.52	?

Table 1: Simulation parameters;  $A_H = 100m^2.s^{-1}$ ,  $L = 57 \times 10^3m$  for North inflow cases, and  $L = 22 \times 10^3m$  for West inflow cases.

# 3D setup



# 3D setup



# ROMS setup

- **Horizontal boundary conditions**

- ✓ *North*

Meridional inflow, i.e.  $u = 0$ ,  $v(z) = \frac{c_1}{2} \left[ 1 + \tanh \left( \frac{z+h_s}{h_d} \right) \right]$ ,  $w=0$

- ✓ *South*

Numerical sponge (viscosity and diffusivity incremented linearly to southern edge of domain)

- ✓ *East and West*

Slip conditions, i.e.  $u = 0$ ;

- ✓ *Boundaries around the island*

No-slip conditions, i.e.  $\mathbf{v} = (0, 0, 0)$

- **Vertical boundary conditions**

- ✓ *Bottom ( $z=-H$ , flat)*

No-slip conditions

- ✓ *Top Free surface*

$$w = \frac{d\eta}{dt}$$

# ROMS setup

✓ Velocity:

$$u(x, y, z, t_0) = 0, \quad v(x, y, z, t_0) = v(z), \quad w(x, y, z, t_0) = 0$$

✓ Free surface elevation:

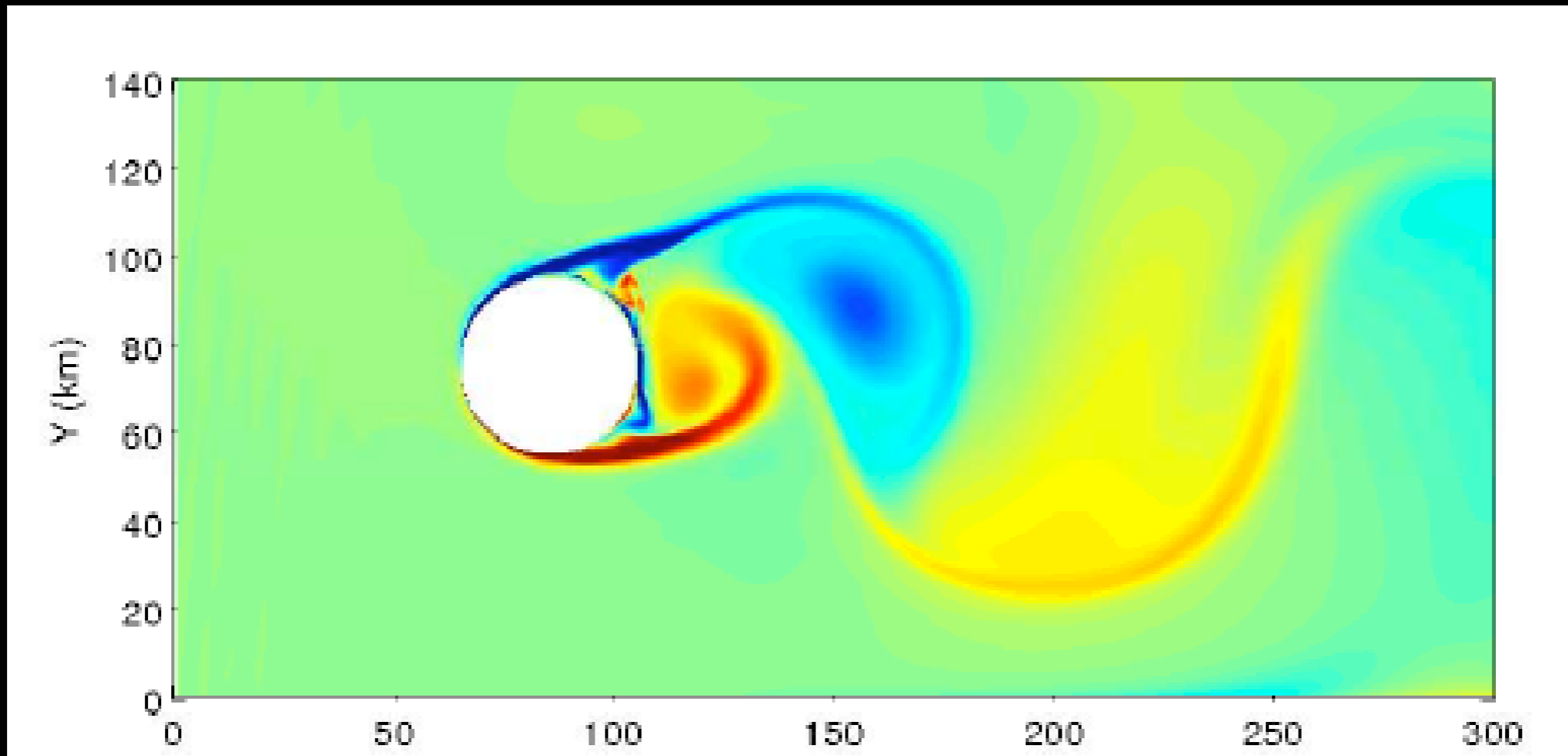
$$\eta_0(x, y, z, t) = \frac{c_1 f}{g} (x - 2x_m)$$

✓ Temperature: thermal wind balance with the initial velocity field

✓ Salinity: constant

# Working hypothesis

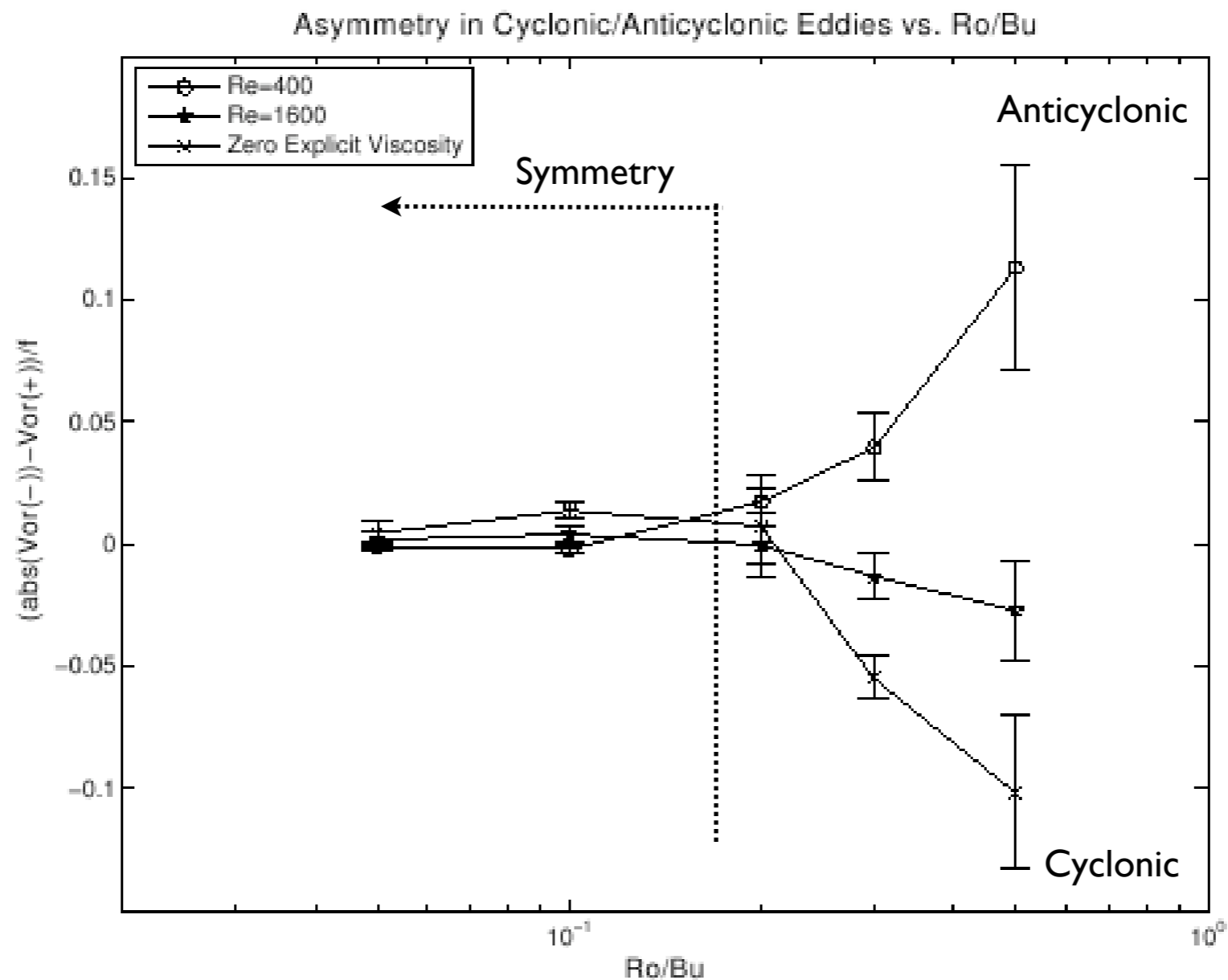
Dong et al., 2007



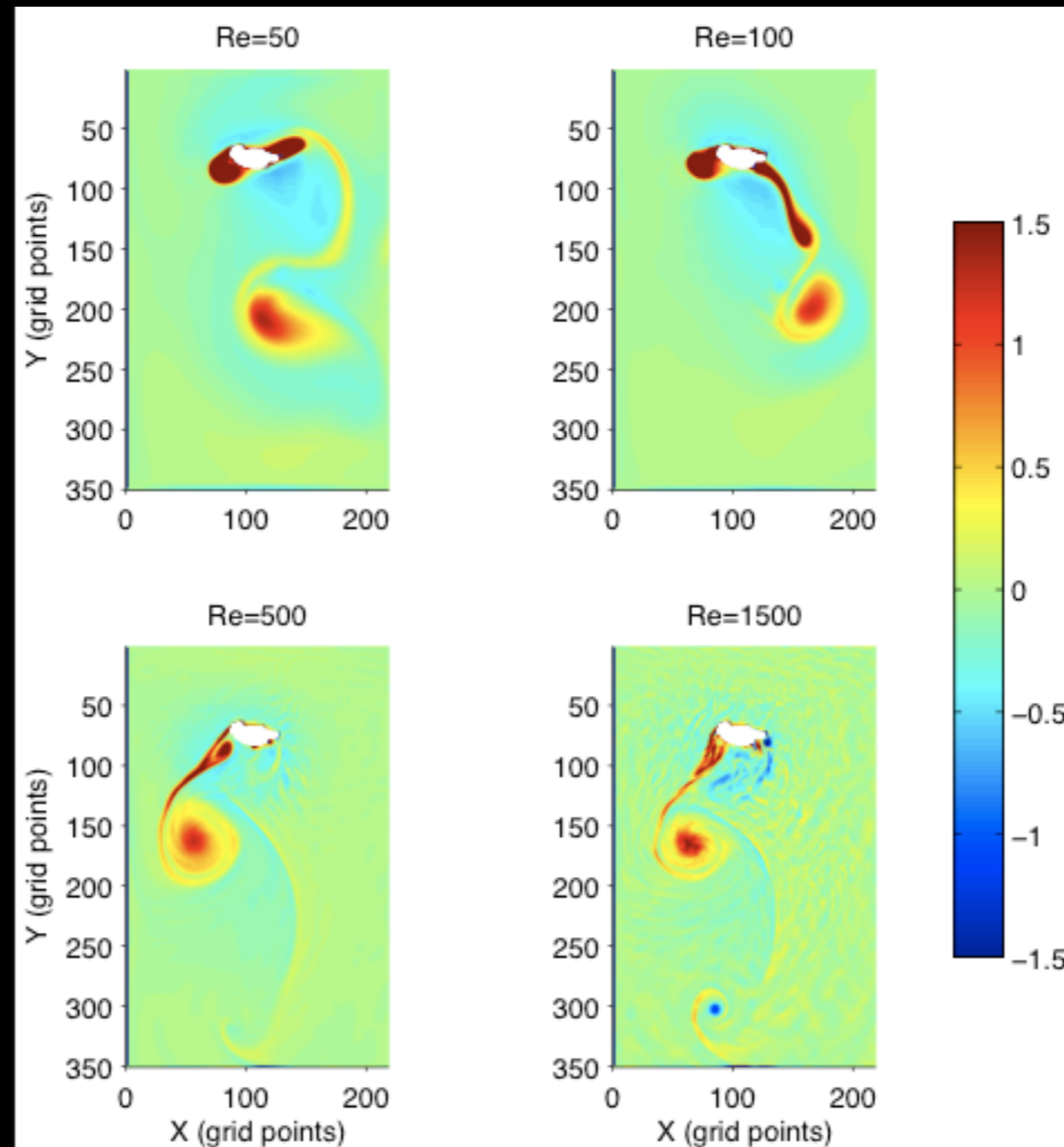


# Working hypothesis

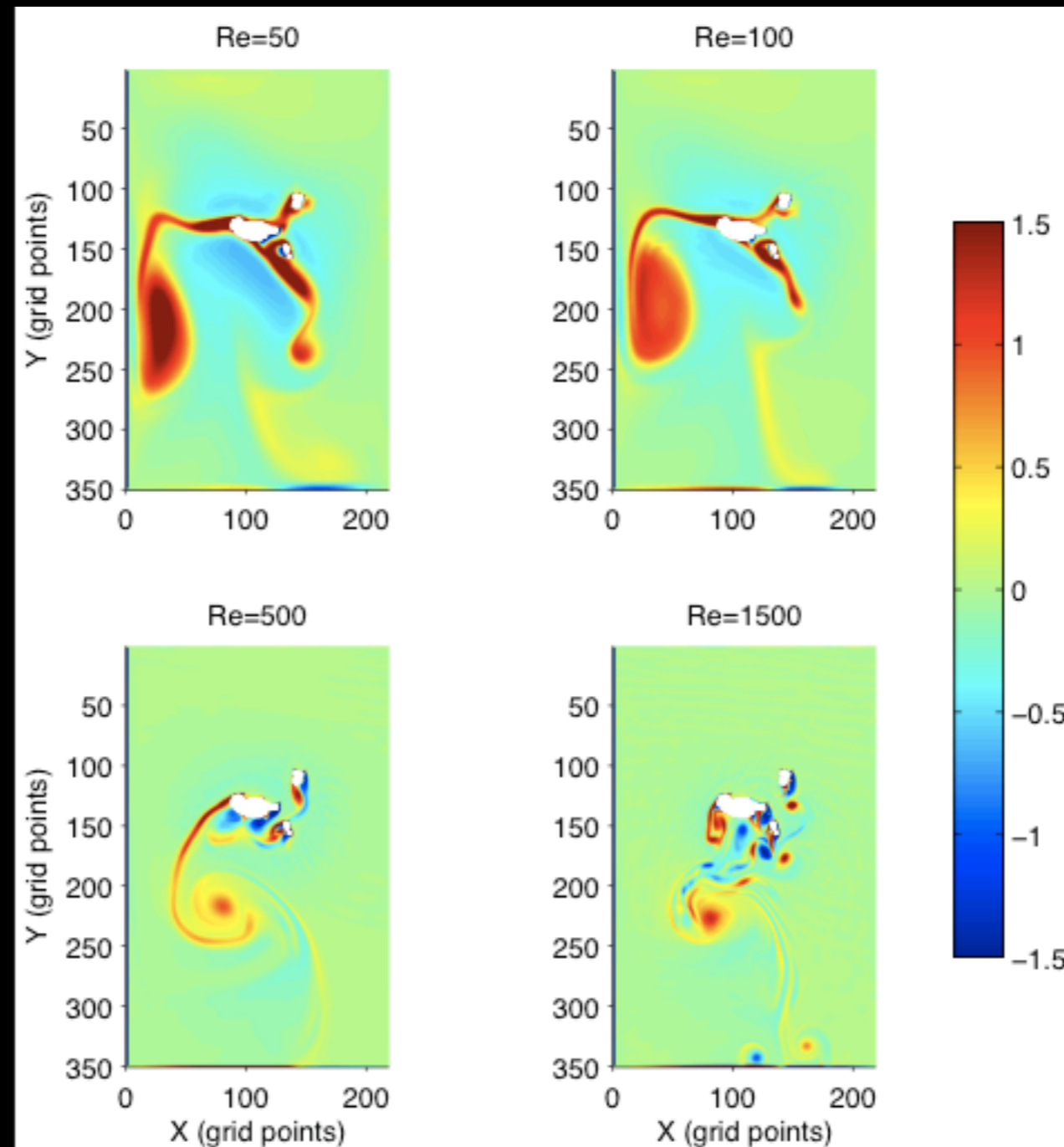
Dong et al., 2007

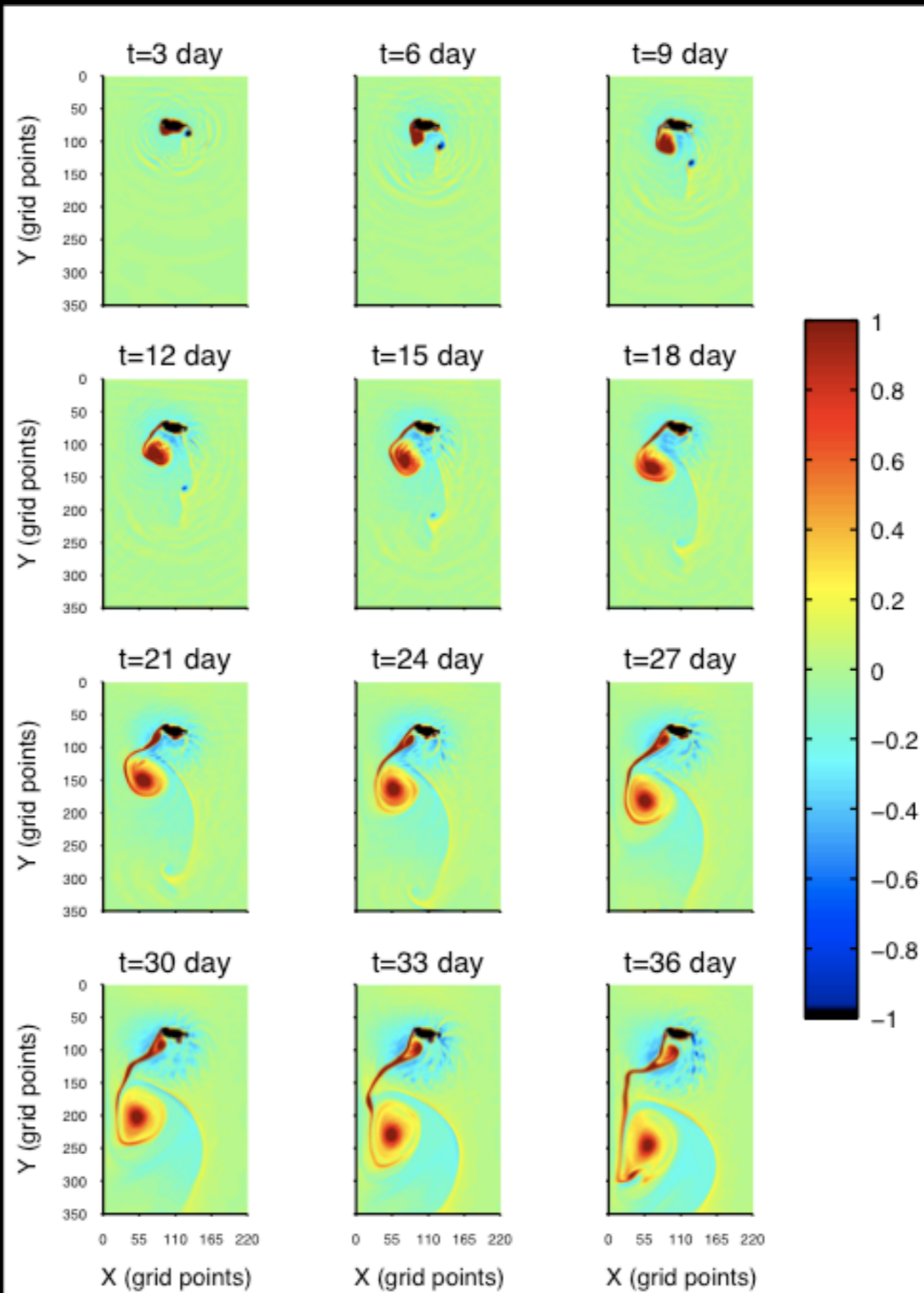


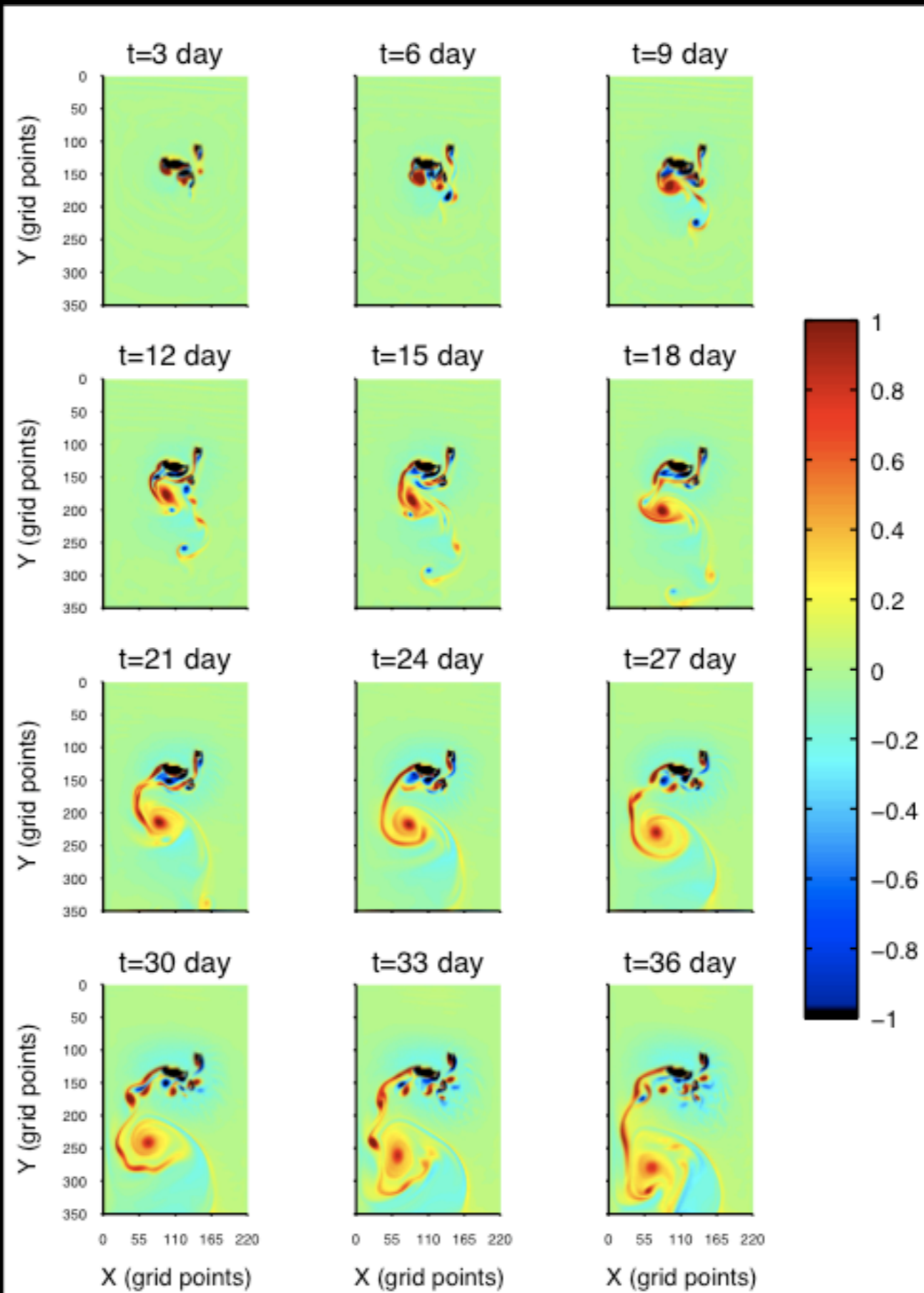
# Re sensitivity study

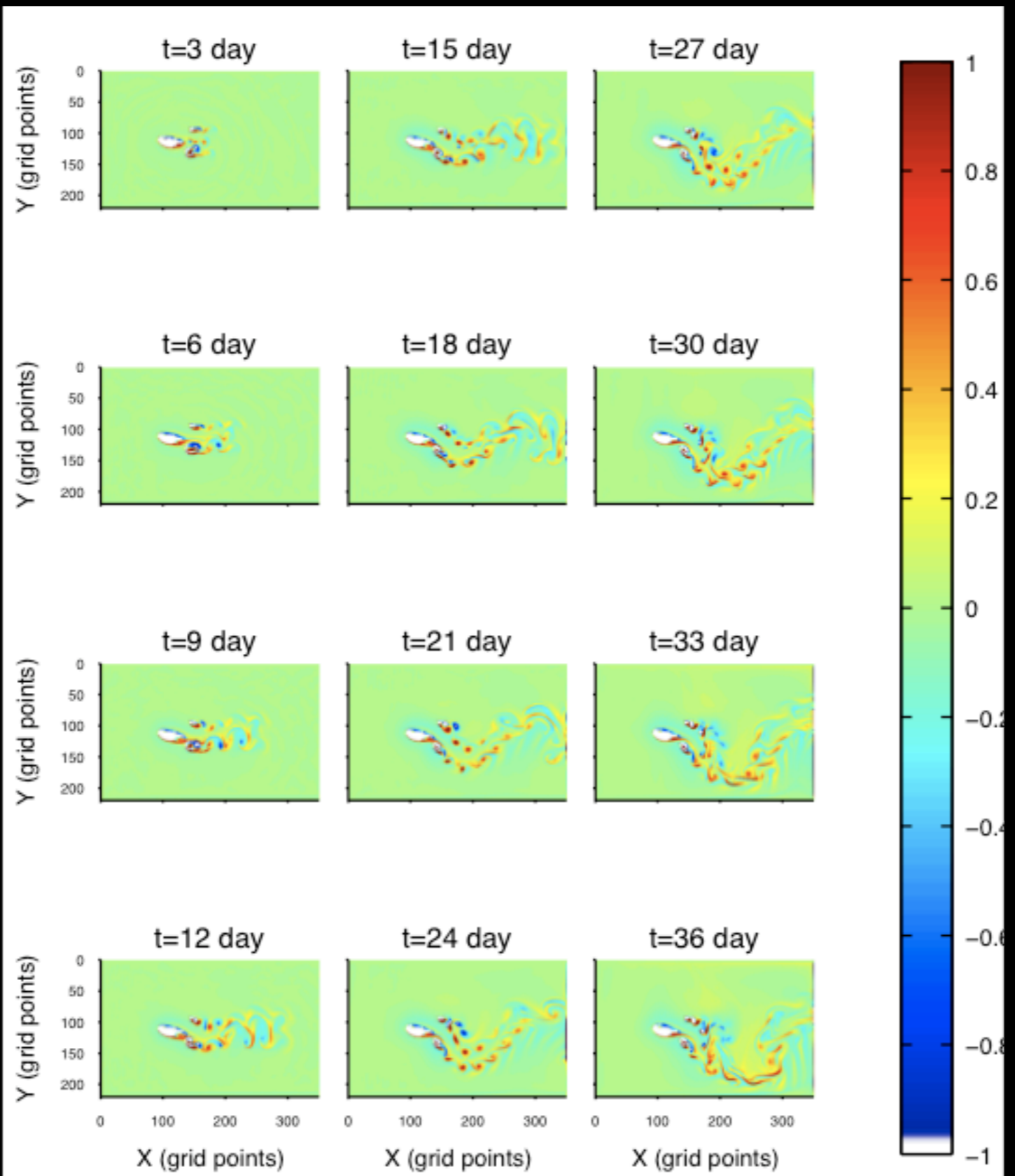


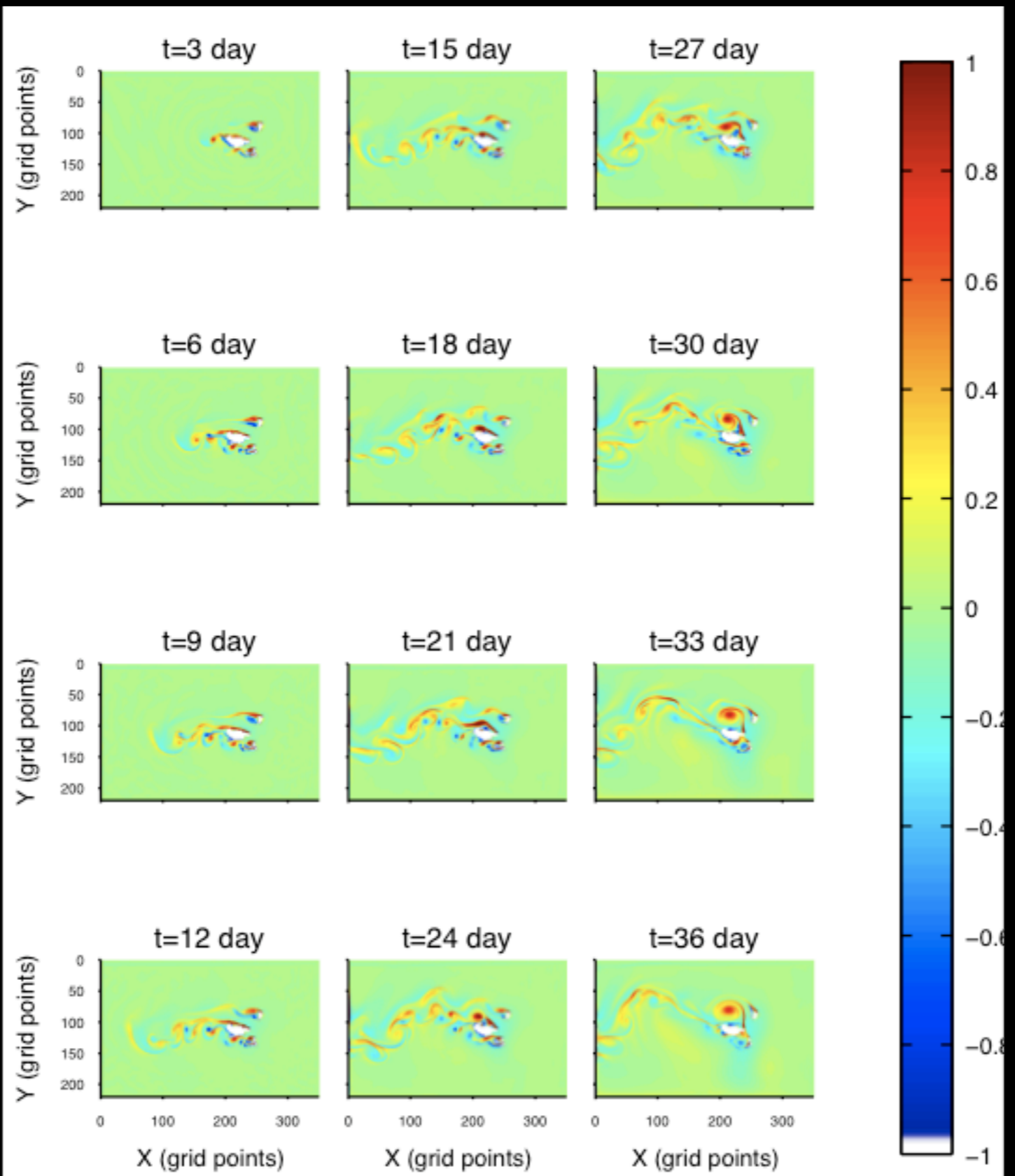
# Re sensitivity study

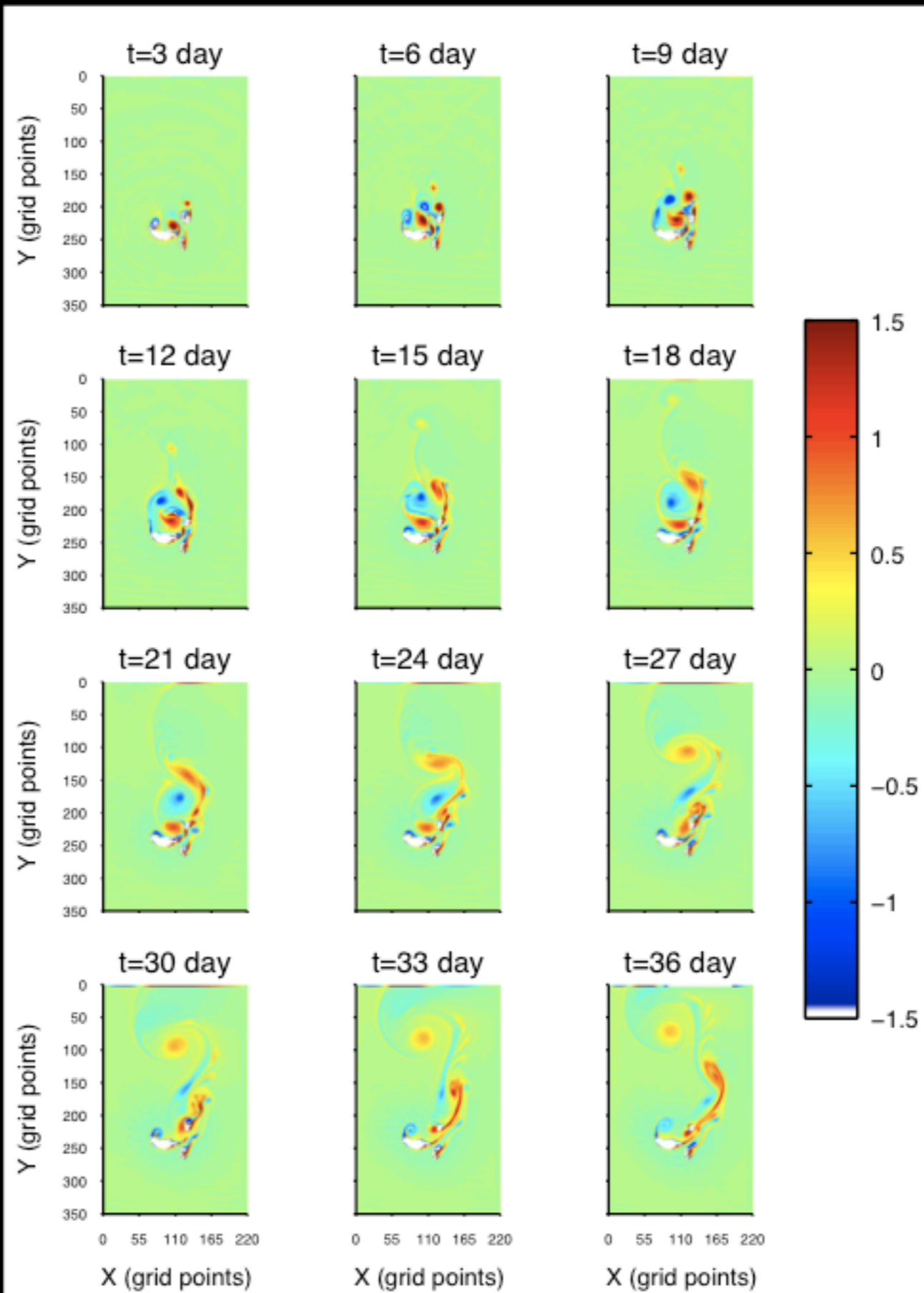






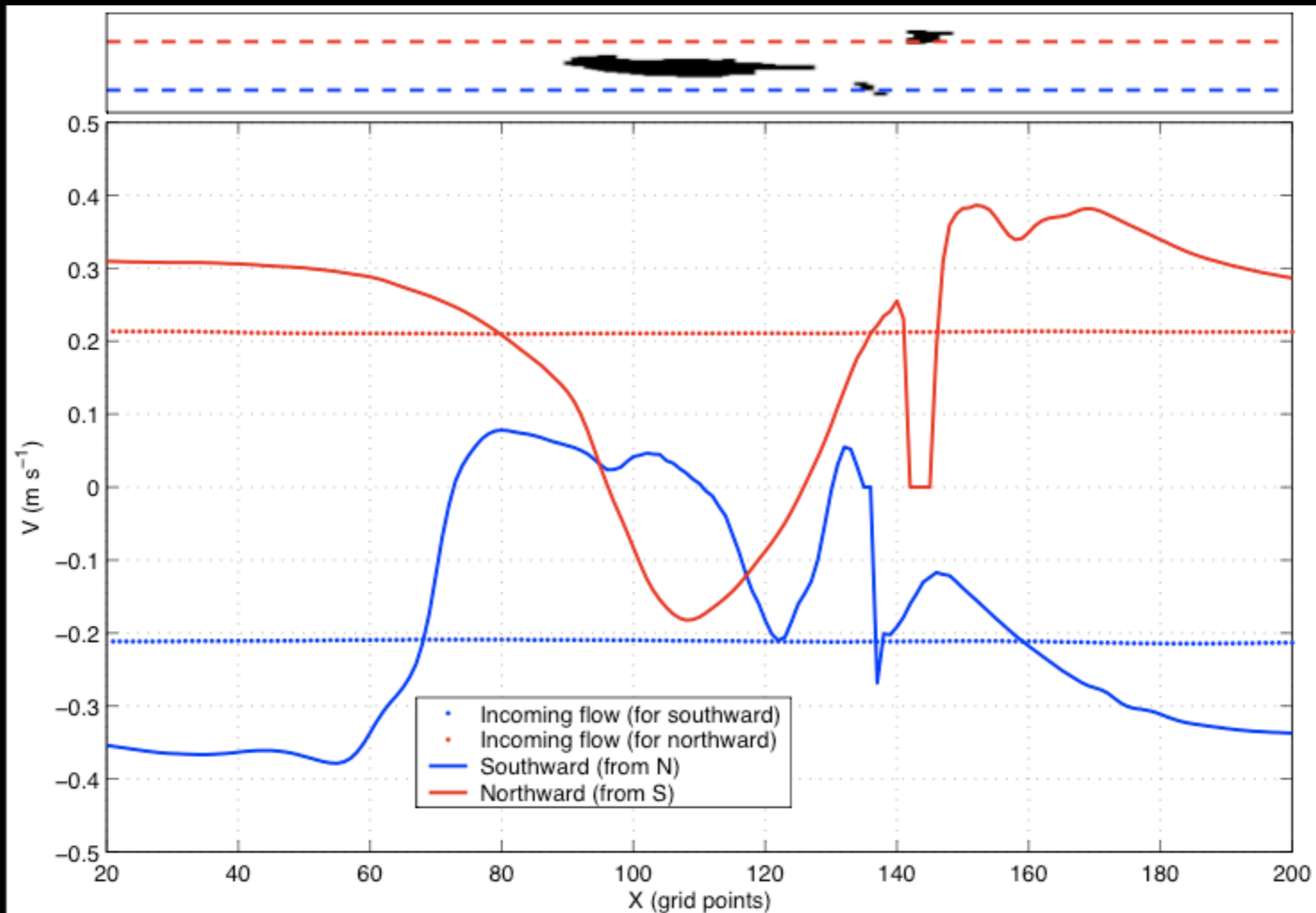




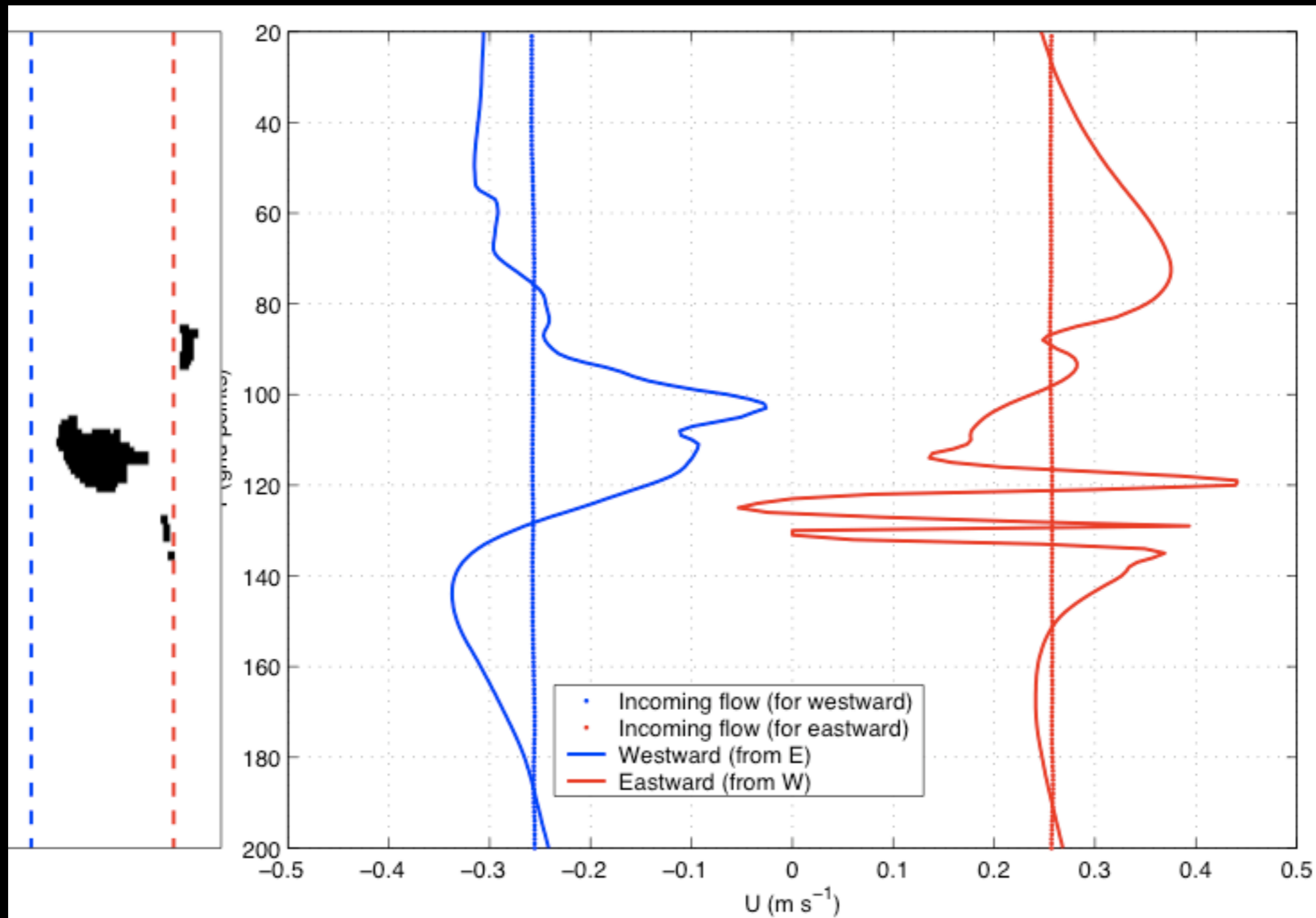




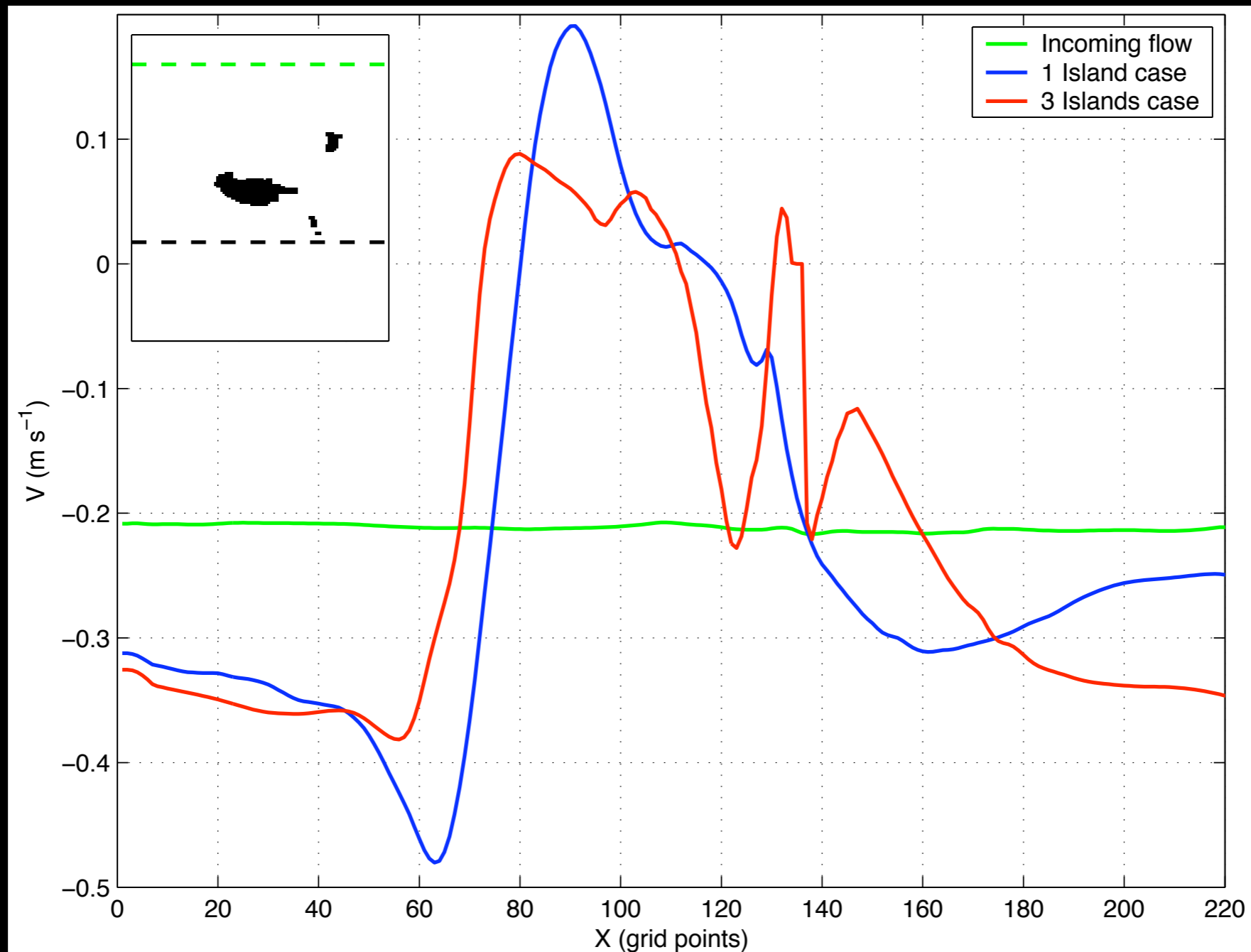
# Flow direction



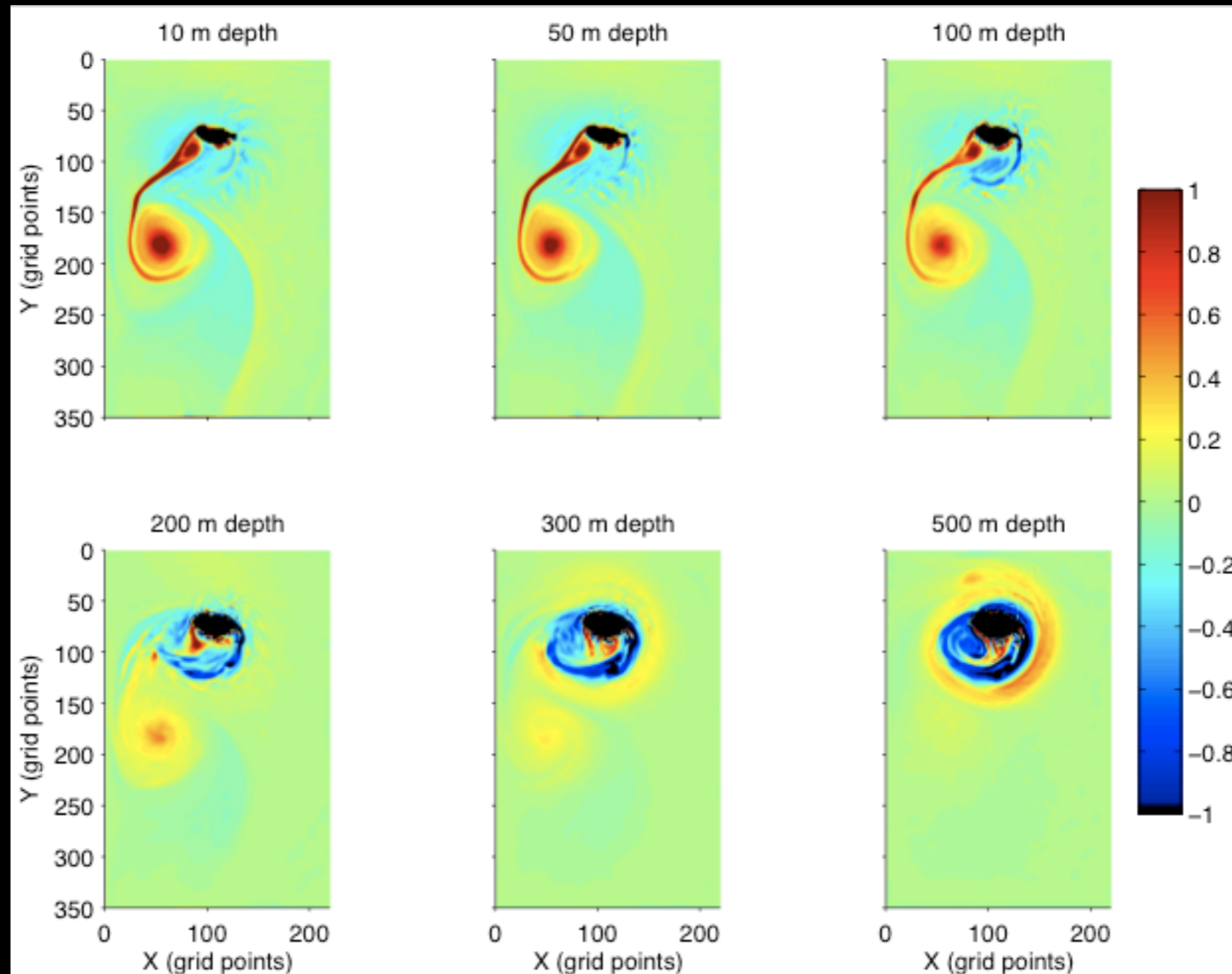
# Flow direction



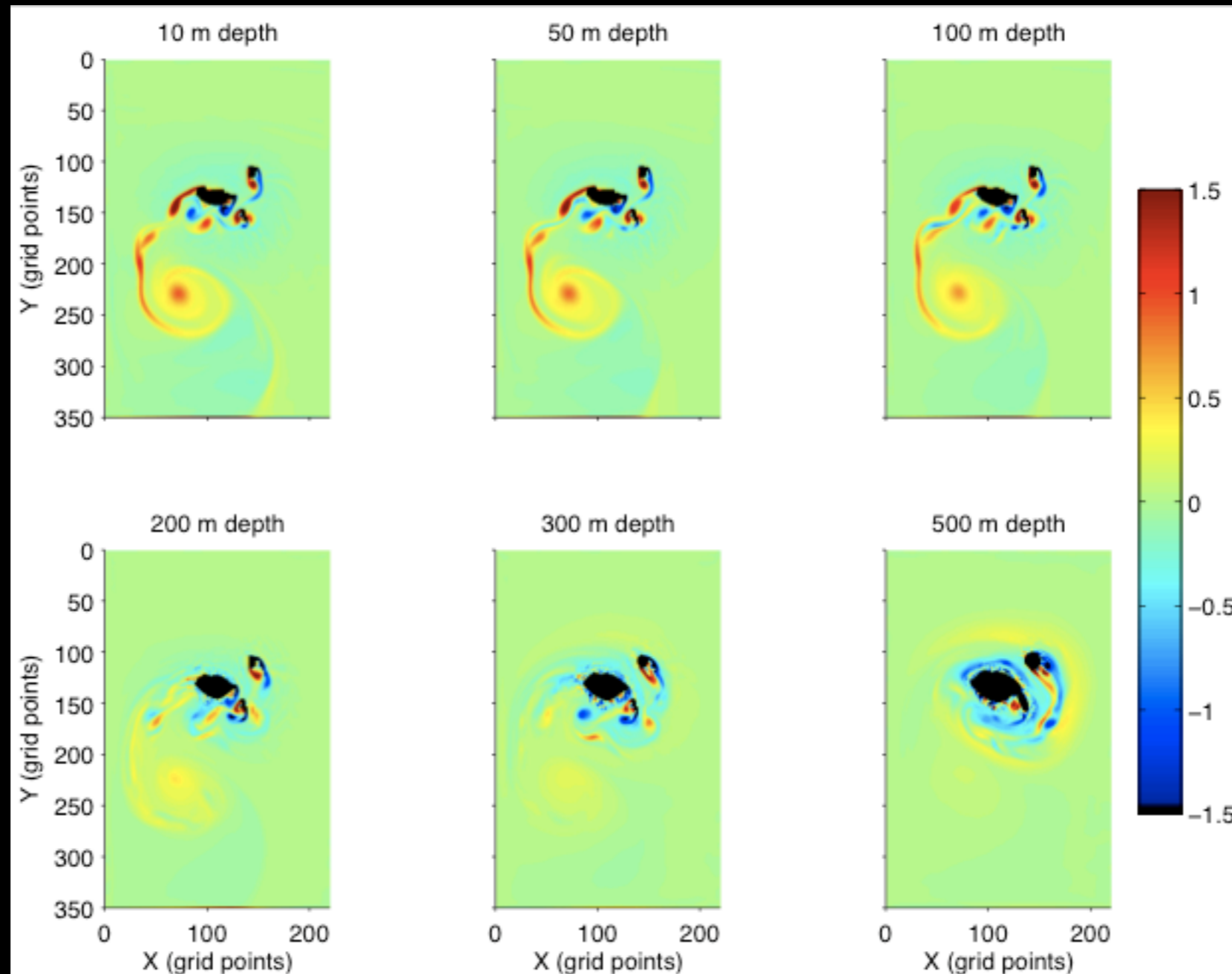
# Nearby island effect



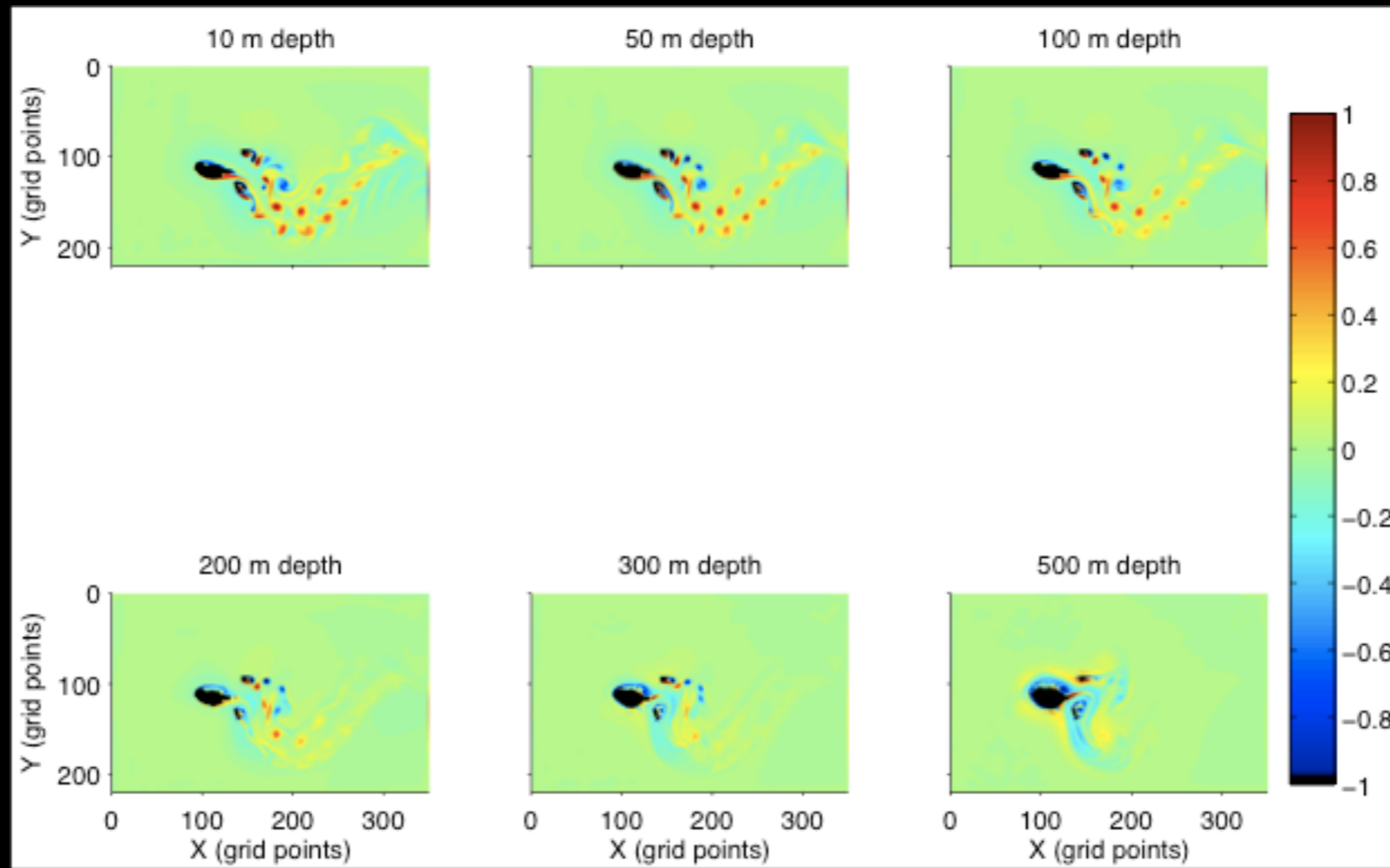
# Depth varying vorticity



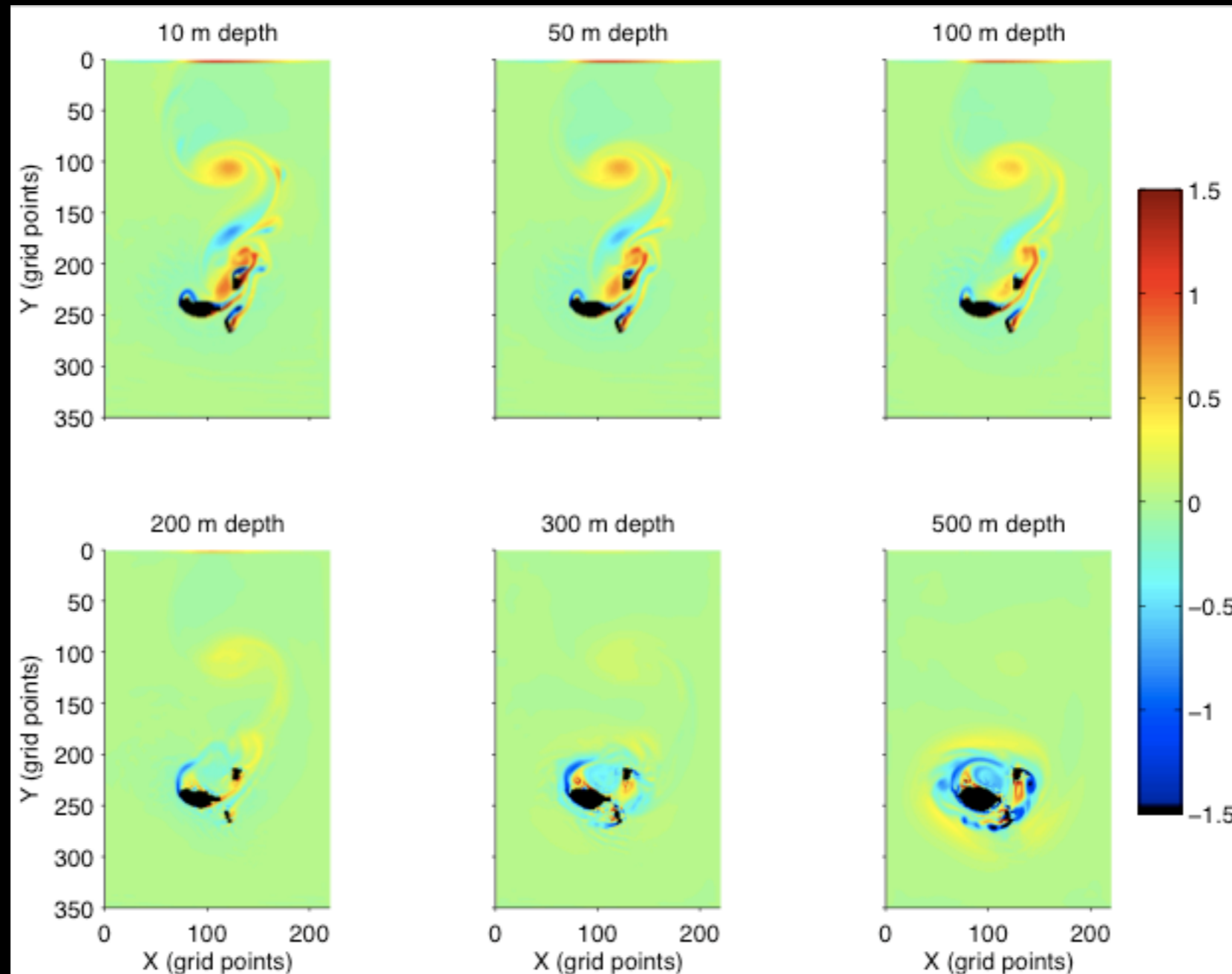
# Depth varying vorticity



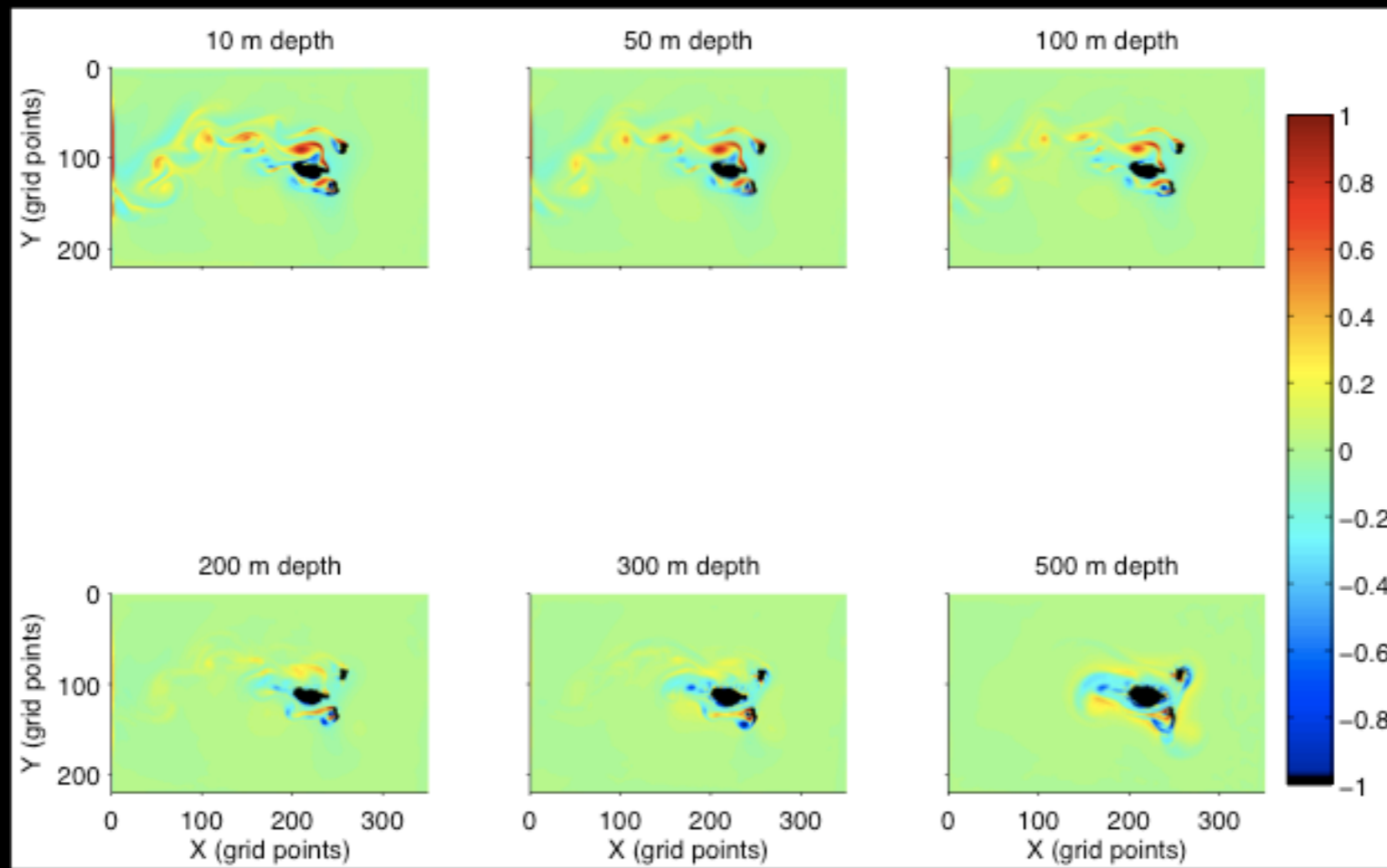
# Depth varying vorticity



# Depth varying vorticity

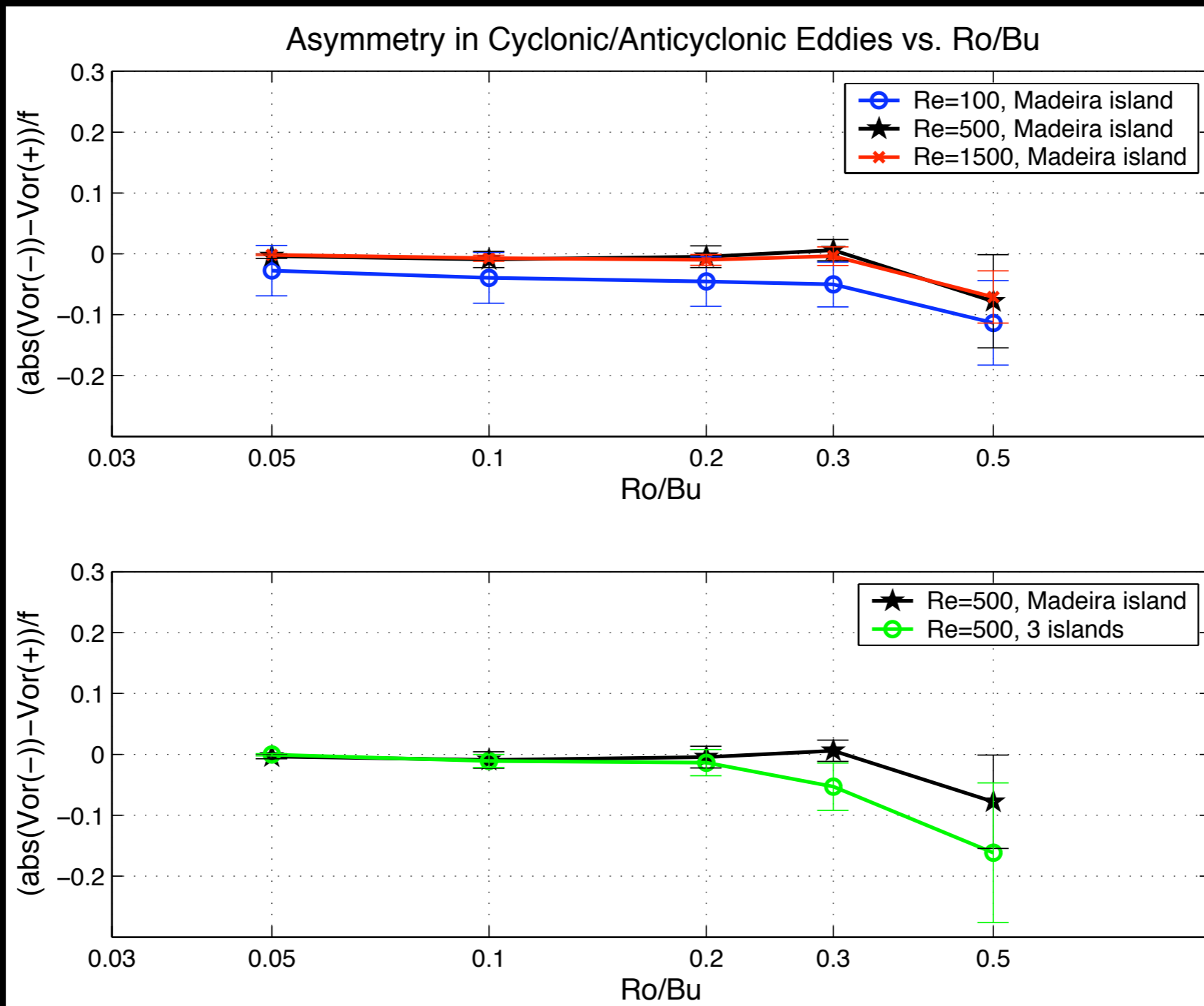


# Depth varying vorticity

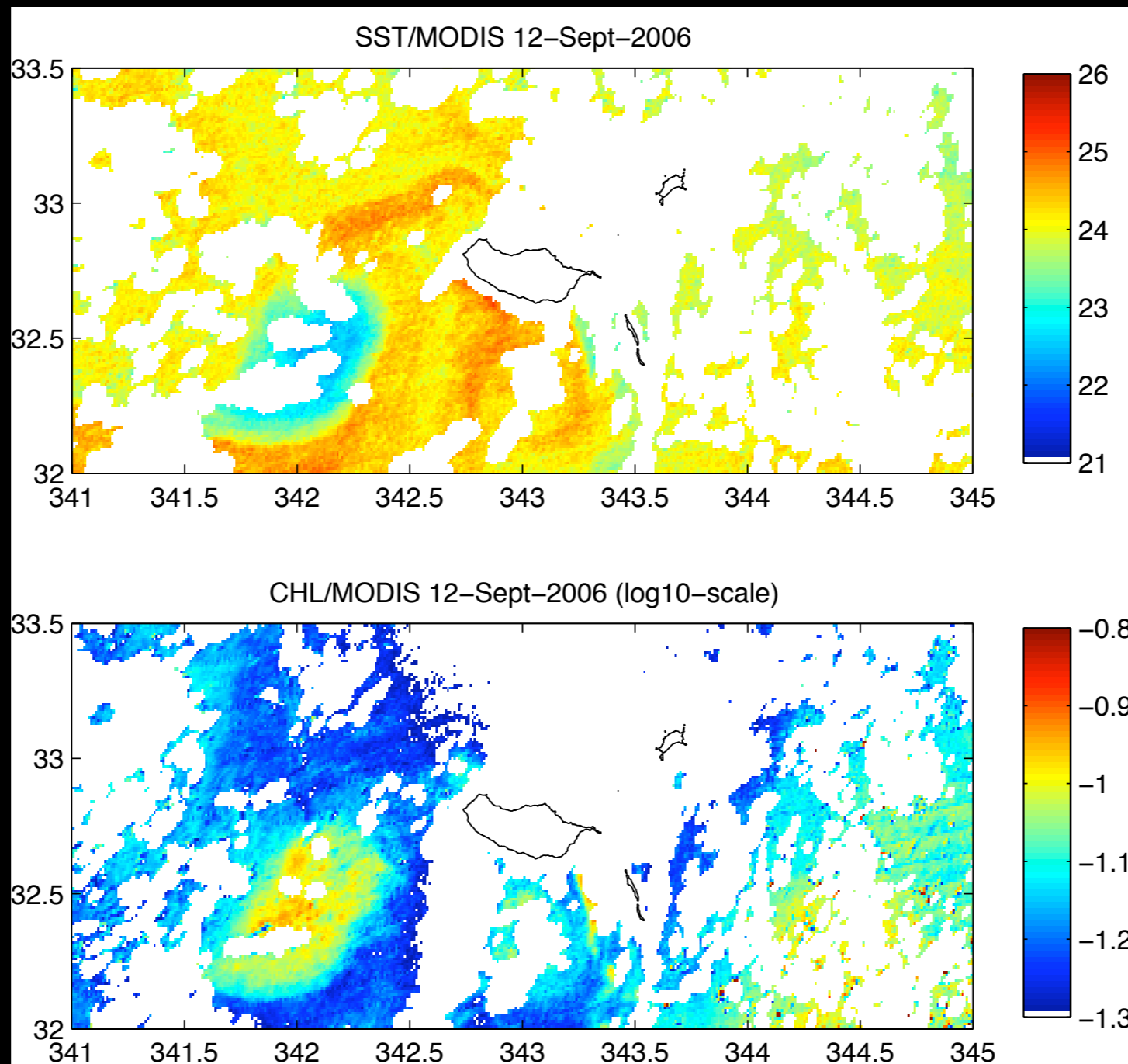




# New hypothesis (Madeira asymmetric case)



# Theory vs observations

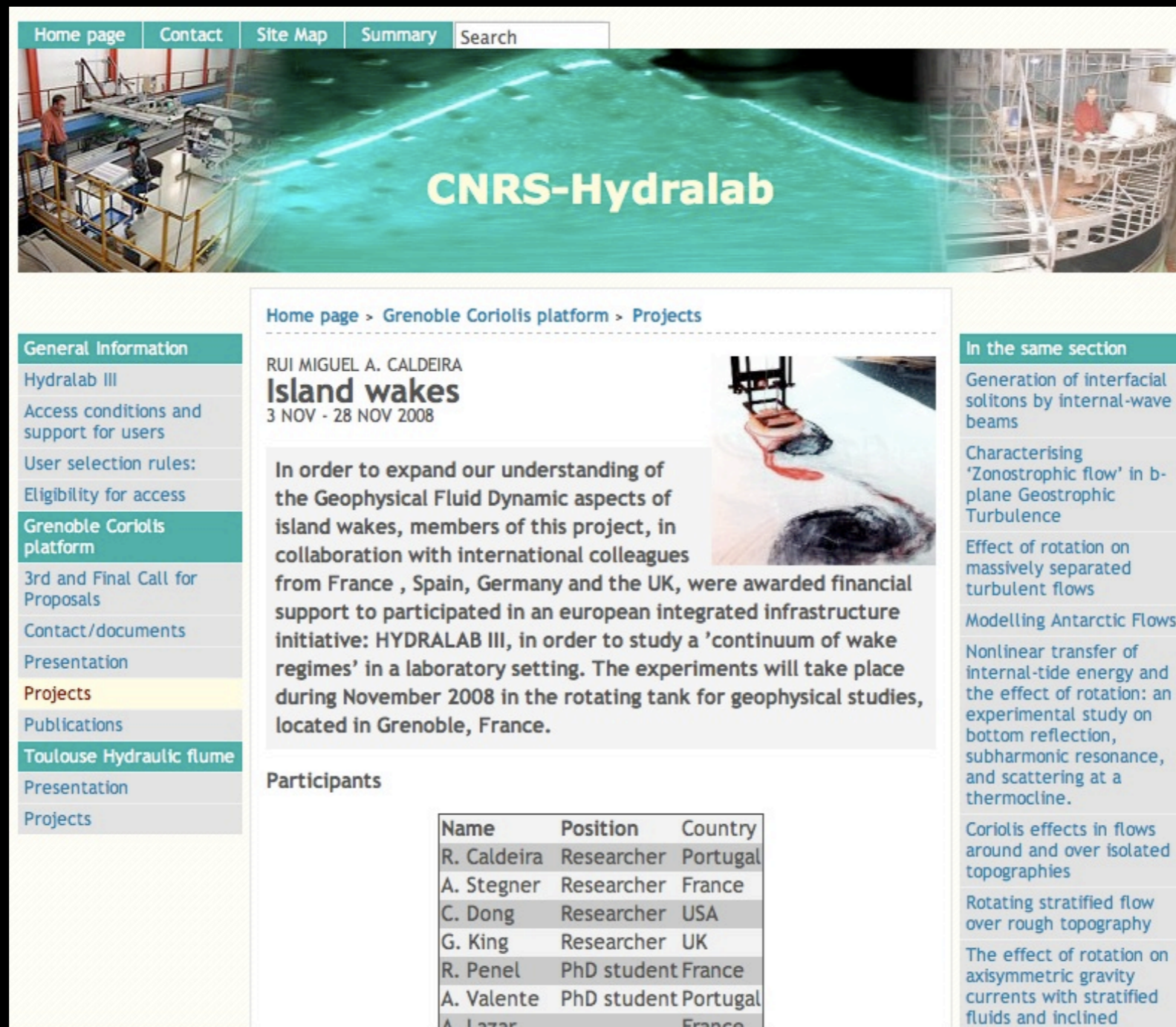


# General conclusions

- Madeira island wake differs from the classical symmetric case
- Cyclonic eddy formation dominates  
=> enhanced by stratification (3D)
- Small nearby islands (Desertas) suppress eddy shedding
- Madeira mesoscale eddy activity mixes 200-300m of surface water => DCM

# Future work...

TIRIS - Three dimensional vortex Instability at high Reynolds number around Islands



The screenshot shows the CNRS-Hydralab website. At the top, there is a navigation menu with links for Home page, Contact, Site Map, Summary, and Search. Below the menu is a large banner image of a laboratory tank with the text "CNRS-Hydralab" overlaid. The main content area is titled "Home page > Grenoble Coriolis platform > Projects". The featured project is "Island wakes" by RUI MIGUEL A. CALDEIRA, dated 3 NOV - 28 NOV 2008. The project description states: "In order to expand our understanding of the Geophysical Fluid Dynamic aspects of island wakes, members of this project, in collaboration with international colleagues from France, Spain, Germany and the UK, were awarded financial support to participate in an european integrated infrastructure initiative: HYDRALAB III, in order to study a 'continuum of wake regimes' in a laboratory setting. The experiments will take place during November 2008 in the rotating tank for geophysical studies, located in Grenoble, France." To the right of the text is a small image showing a vortex in a tank. Below the text is a "Participants" section with a table listing the names, positions, and countries of the project members. On the left side of the page is a sidebar with a "General Information" menu, and on the right side is a "In the same section" menu listing related topics.

Home page | Contact | Site Map | Summary | Search

**CNRS-Hydralab**

Home page > Grenoble Coriolis platform > Projects

RUI MIGUEL A. CALDEIRA  
**Island wakes**  
3 NOV - 28 NOV 2008

In order to expand our understanding of the Geophysical Fluid Dynamic aspects of island wakes, members of this project, in collaboration with international colleagues from France, Spain, Germany and the UK, were awarded financial support to participate in an european integrated infrastructure initiative: HYDRALAB III, in order to study a 'continuum of wake regimes' in a laboratory setting. The experiments will take place during November 2008 in the rotating tank for geophysical studies, located in Grenoble, France.

Participants

Name	Position	Country
R. Caldeira	Researcher	Portugal
A. Stegner	Researcher	France
C. Dong	Researcher	USA
G. King	Researcher	UK
R. Penel	PhD student	France
A. Valente	PhD student	Portugal
A. Lazar		France

**General Information**

- Hydralab III
- Access conditions and support for users
- User selection rules:
- Eligibility for access

**Grenoble Coriolis platform**

- 3rd and Final Call for Proposals
- Contact/documents
- Presentation
- Projects**
- Publications

**Toulouse Hydraulic flume**

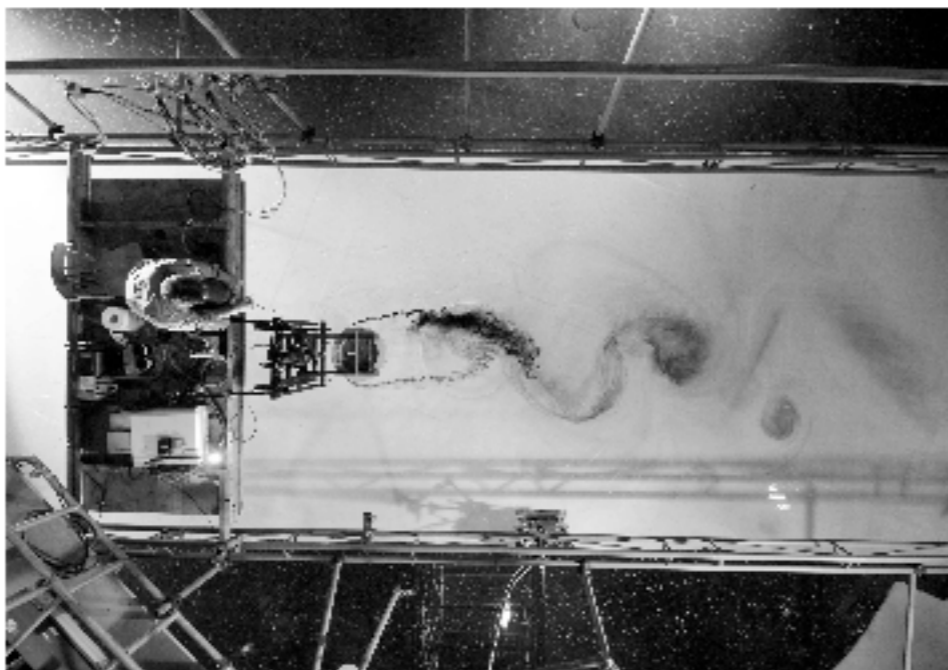
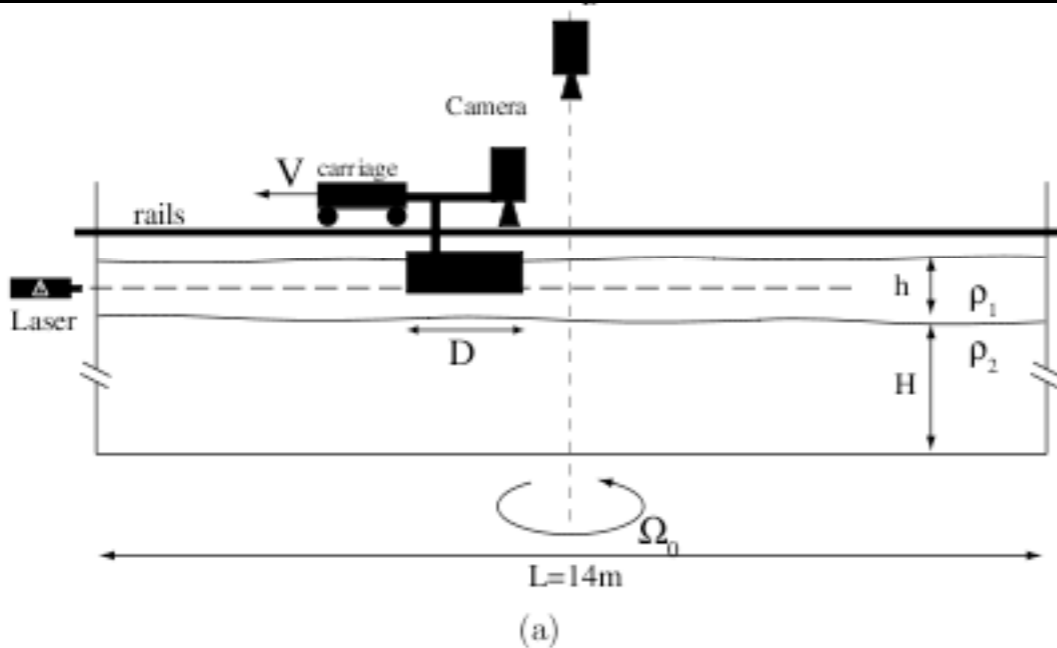
- Presentation
- Projects

**In the same section**

- Generation of interfacial solitons by internal-wave beams
- Characterising 'Zonostrophic flow' in b-plane Geostrophic Turbulence
- Effect of rotation on massively separated turbulent flows
- Modelling Antarctic Flows
- Nonlinear transfer of internal-tide energy and the effect of rotation: an experimental study on bottom reflection, subharmonic resonance, and scattering at a thermocline.
- Coriolis effects in flows around and over isolated topographies
- Rotating stratified flow over rough topography
- The effect of rotation on axisymmetric gravity currents with stratified fluids and inclined

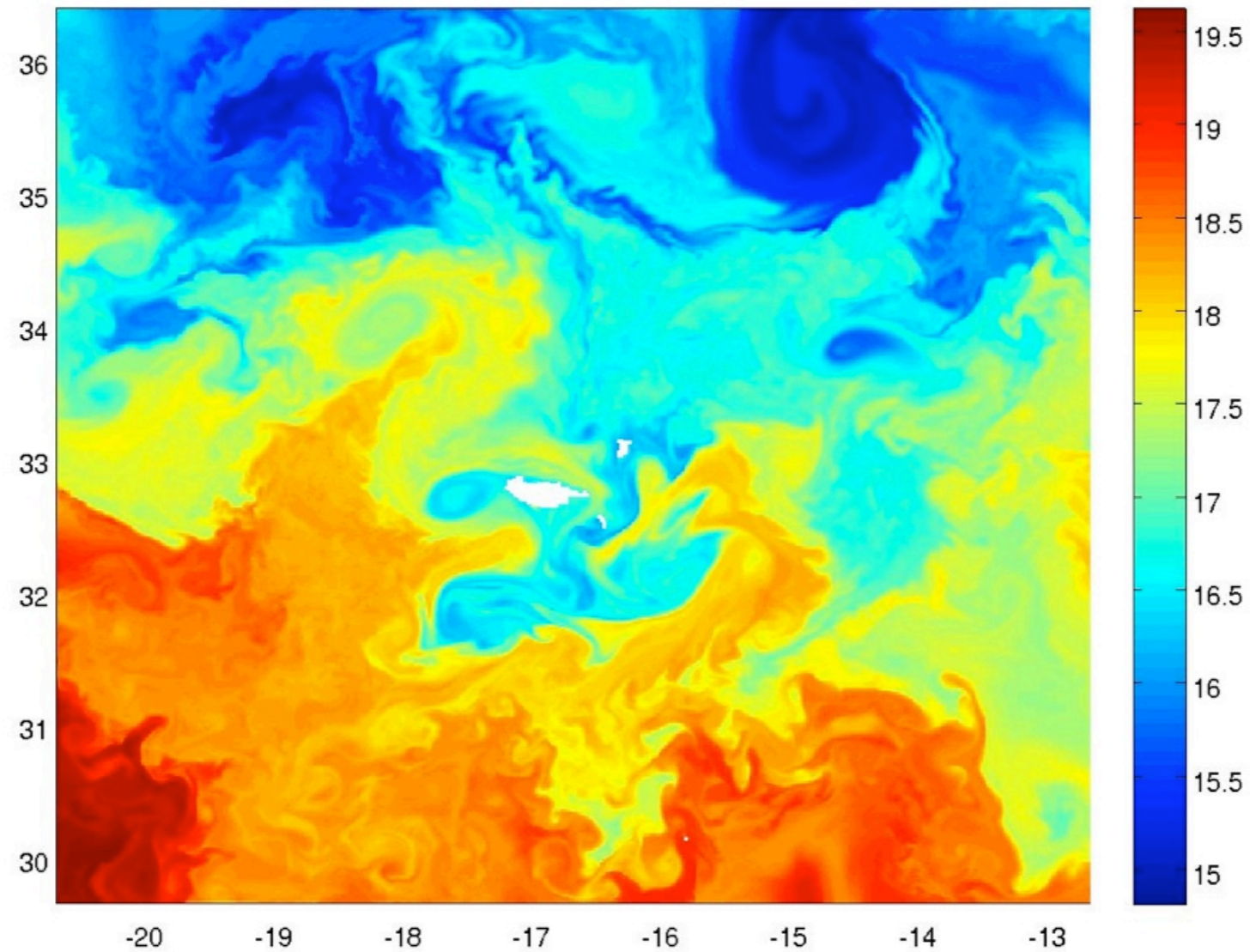
# Future work...

TIRIS - Three dimensional vortex Instability at high Reynolds number around Islands



# Future work...

High resolution (realistic) numerical modeling





# Future...

CIMAR - High Performance Computing (HPC) facility

